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FORMULATION OF NUMERICAL METHODS

USED IN THE

XYZ THREE-DIMENSIONAL POTENTIAL FLOW PROGRAM

An Engineering Report

by

WILLIAM JAMES BEARY JR.

Submitted to the Faculty of the College of Engineering Texas A&M University

in partial fulfillment of the requirements for the degree of MASTER OF ENGINEERING

May 1986

Major Subject: Ocean Engineering



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ABSTRACT

The calculation of non-lifting potential flow about arbitrary three dimensional bodies is examined in detail with specific interest in the XYZ Potential Flow program developed by the David W. Taylor Naval Ship Research and Development Center. The program uses a surface singularity distribution to solve the Neumann boundary value problem by means of a source panel method assuming a flat element with a constant source density over the area of the element. Boundary conditions are applied at control points on the elements producing a system of linear equations for the source density. When the source density is known, velocities and pressure coefficients may be calculated.

The main purpose of this paper is to present the details of the approximation of an arbitrary three dimensional body using quadrilateral elements, and to provide a detailed derivation of the exact source panel integrations in order to gain insight for future research at Texas A&M University. A variation of the Hess method of surface discretization using quadrilateral source panels is described in detail as it is used in the XYZ Potential Flow program. The exact source panel integrations are derived in detail.

A general discussion of other aspects of the program is included. Velocities and pressure coefficients for flow about a triaxial ellipsoid are calculated using the XYZ Potential Flow Program solution, and the results are compared with the analytical solution and the Hess Program solution.



ACKNOWLEDGEMENTS

The author is thankful to Janet S. Dean of the David W. Taylor Naval Ship Research and Development Center, for her generous time on the telephone explaining details of the XYZ Potential Flow program which she co-authored, and to John L. Hess of McDonnell-Douglas Corporation, who, during a valuable phone conversation, suggested references which contained information necessary to complete the closed form source panel integrations. Appreciation is also expressed to Dr. Allen H. Magnuson, who provided direction as graduate committee chairman, and to Dr. David R. Basco and Dr. Leland A. Carlson who served as committee members.



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1.0 INTRODUCTION

This paper examines two aspects of the development of the XYZ Potential Flow Program (hereafter referred to as the XYZPF Program), a FORTRAN program which uses a source panel method to approximate solutions to steady potential flow problems about arbitrary three dimensional bodies. The aspects examined in detail are (1) the description of the details of the approximation of an arbitrary three-dimensional body using quadrilateral elements, and (2) a detailed derivation of the exact source panel integrations.

The XYZPF Program was developed specifically for applications in numerical ship modelling and hydrodynamics studies at the David W.

Taylor Naval Ship Research and Development Center (NSRDC) in Bethesda, Maryland. The format of the program is based on the work of Hess and Smith (1962) in the numerical calculation of non-lifting potential flow.

A similar program is maintained by the Aerodynamics Division of the McDonnell-Douglas Corporation, referred to in this paper as the "Hess program." The XYZPF Program is a modification of what has come to be known generally as the Hess Method. The most significant modifications are improvements to the method of solving the matrix equation for the source density, and greater flexibility in the input options (Dawson and Dean 1972).

Though potential flow is a product of mathematics, and is never found in a real fluid, the results of potential flow calculations provide usable information for flow regions external to a thin boundary layer,



with little or no boundary layer separation. For such flow fields, the region outside the boundary layer may be considered to be effectively inviscid, and may be closely approximated by potential flow models.

Small viscous effects can be accounted for by "thickening" the body by the appropriate displacement thickness. Displacement thickness accounts for the region of retarded fluid flow in the boundary layer inversely proportional to the square of the free stream velocity. Downstream of the point of boundary layer separation, the potential flow model no longer applies.

Prior to the development of numerical methods, analytical solutions were generally restricted to simple analytical shapes (Kellogg 1929). The need to solve boundary value problems for arbitrary boundaries in continuum mechanics has fostered the development of numerical approximations to the integral equation expressions. While the integration methods have been well known for quite some time, only since the advent of high speed computers have many of the problems been practical to solve by numerical methods. Among the numerical methods being used are finite differences, finite elements, and the boundary element method.

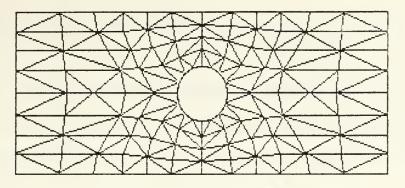
"Finite differences" and "finite elements" are numerical methods which satisfy the boundary conditions, and then approximate the solution to the governing equation in the fluid domain. These methods discretize the domain into a network of elements or cells.



Another approach is what is now known as the "Boundary Element Method," in which the governing equation is exactly satisfied in the domain, and the boundary conditions are applied through a boundary discretization method. The boundary value problem is reformulated as a boundary integral equation which is then discretized by subdividing the boundary into a finite number of surface elements. Each element is represented by an analytical function, and the source density function is integrated over the surface of each element. Two factors governing the accuracy of the boundary element method are the boundary discretization method and the source panel integration. These two factors are examined in detail in this report, as a detailed derivation of the exact source panel integration, including the development of the source panel geometry, has not previously appeared in literature.

The difference between the domain methods and the boundary methods is significant. The domain methods discretize the domain, while the boundary methods discretize the boundary. Thus, the boundary method reduces the dimension of the problem by one, as depicted in figure (1). In the application of the XYZPF Program, the problem is reduced from a three-dimensional problem in the domain to a two-dimensional problem on the boundaries. This method is well suited to problems in which the limits of the domain are infinite or difficult to define, in that the problem is applied to the boundary rather than the domain.





FINITE ELEMENT DISCRETIZATION

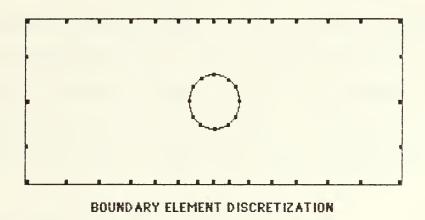


Figure 1. Discretization Methods

Just as there are many variations of domain methods, there are also a variety of boundary methods. In general, they can be classified as "indirect" or "direct" formulations. The "indirect" method assumes a continuous source distribution over the surface of the body, and a solution which satisfies both the governing equation in the domain, and the boundary conditions on the body surface. The result is an integral equation on the boundary which has the surface source density function as its unknown. By enforcing the boundary conditions at control points on the surface, a system of equations is produced by which the source density may be determined.

The "direct" method solves the velocity potential function through



an application of Green's Second Identity requiring the solution of a source distribution and a dipole distribution on the boundary. The direct method has more physical significance to the general boundary value problem, and more versatility in its application as it can be applied to Neumann problems, Dirichlet problems, or mixed boundary value problems (Brebbia 1984).

The simplicity and accuracy of the indirect method has made it attractive for many applications. The source panel method is an application of the indirect formulation of the boundary element method to the Neumann type of potential flow problem, for which the normal derivative of the potential function is prescribed on the boundary.

1.1 OBJECTIVES

The purpose of this paper is (1) to describe the details of the approximation of an arbitrary three-dimensional body using quadrilateral elements, and (2) to provide a detailed derivation of the exact source panel integrations for use in future investigations at Texas A&M University using panels of higher order geometries and source density functions. This paper is not intended to be a user's manual, though a general discussion of other aspects of the program is also included.

NSRDC Report 3892 (Dawson and Dean 1972) is a summary of the XYZPF Program for those strictly interested in its use.



2.0 HISTORICAL DEVELOPMENT

The foundations of the boundary element method were laid early in this century beginning with Fredholm in 1903 when he established the existence of solutions to the Neumann problem through a reconstruction of the problem using a discretized boundary (Kellogg 1929). The solution was determined to be the potential of a simple source distribution on a boundary with a continuous normal derivative for an infinite domain. Later works by Kellogg (1929) in potential theory demonstrated the application of the boundary integral equation method in electrostatics, heat transfer, flow in porous media, and fluid flow problems, but development was limited by the difficulty of obtaining analytical solutions. No significant advances were made until interest in boundary integral equation methods was revitalized with the advent of high speed electronic computers. Investigators were then able to discretize the boundaries and solve the integral equations numerically. This method of solution became known as the boundary element method. Early development of such numerical methods was pioneered by Hess and Smith (1962) and Jaswon and Symm (1963). Hess and Smith dealt primarily with the indirect formulation eventually leading to a solution for the three dimensional problem as described in this paper. In a parallel work, Jaswon and Symm developed a direct formulation approach to the two dimensional problem. The XYZPF Program is based primarily on the work of Hess and Smith. Hess has since developed a higher order panel method (Hess 1979) and Lefebvre modified the XYZPF Program for calculating velocity potentials for five degrees of freedom (Lefebvre 1982).



3.0 THEORETICAL DEVELOPMENT

3.1 THE POTENTIAL FLOW PROBLEM IN THREE DIMENSIONS

The governing equation for ideal (incompressible, inviscid, irrotational) flow is Laplace's equation:

$$\nabla^2 \Phi = 0 \tag{1}$$

where Φ is the velocity potential, and ∇^2 is the Laplacian operator. The XYZPF Program deals with steady, uniform flow of an ideal fluid about an arbitrary three dimensional body. The velocity components at any point within the flow field may be obtained from the negative gradient of the velocity potential, i. e.

$$\mathbf{V} = -\nabla \Phi = -\frac{\partial \Phi}{\partial x} \mathbf{i} - \frac{\partial \Phi}{\partial u} \mathbf{j} - \frac{\partial \Phi}{\partial z} \mathbf{k}$$
 (2)

The freestream flow \mathbf{V}_{∞} is defined as a uniform stream of unit magnitude.

$$|\mathbf{V}_{\infty}| = \sqrt{V_{\infty X}^2 + V_{\infty Y}^2 + V_{\infty Z}^2} = 1$$
 (3)

The key to the boundary element method is the Divergence Theorem (Green's Theorem) which relates a volume integral to an equivalent surface integral reducing the three-dimensional problem to a



two-dimensional one. The expression for Green's second identity is (Lamb 1924):

$$\iiint (\Phi \nabla^2 w - w \nabla^2 \Phi) d\Omega = \iint (w \frac{\partial \Phi}{\partial n} - \Phi \frac{\partial w}{\partial n}) d\Gamma \qquad (4)$$

in which Ω represents the integration over the three dimensional domain, and Γ represents integration over the two dimensional boundary. The partial derivatives are taken with respect to the outward normal, n. The weighting function, w, is usually chosen to be the fundamental solution for three dimensions, $w = 1/(4\pi r)$, where r is the distance from the source to an arbitrary point on the boundary.

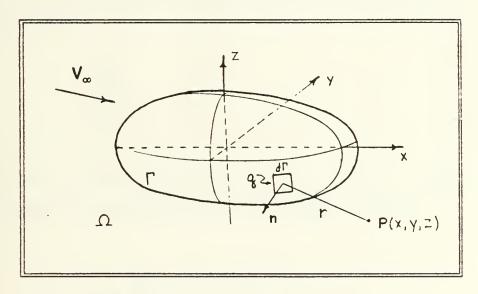


Figure 2. Potential Flow in Three Dimensions

Consider an arbitrary three-dimensional body with surface Γ , having an equation of the form F(x, y, z) = 0 where x, y, z are Cartesian coordinates of the global reference system as shown in Figure (2). The unit outward normal, \mathbf{n} , at any point on the surface is given by the gradient of the function describing the surface divided by the magnitude



of the gradient, i.e.

$$\mathbf{n} = \frac{\pm \nabla F}{|\nabla F|} \tag{5}$$

where the sign of the unit normal vector is chosen to ensure that the vector is an outward normal. The potential function Φ describing the flow field must meet the following boundary conditions:

a.
$$\nabla^2 \Phi = 0$$
 (Laplace's Equation) (6)

b. For an impermeable boundary, the velocity normal to the surface must be zero relative to the boundary (the Neumann boundary condition):

$$\left(\frac{\partial \Phi}{\partial \mathbf{n}}\right)_{\Gamma} = 0 \tag{7}$$

c. The velocity potential approaches the freestream velocity potential as the distance from the body goes to infinity:

$$\Phi \to \Phi_{\infty}$$
 as $|\mathbf{r}| \to \infty$ (8)

The total potential at any point in the domain is composed of the freestream potential and the disturbance potential due to the body,

$$\Phi = \Phi_{\infty} + \Phi \tag{9}$$



The disturbance potential, φ , satisfies the following boundary conditions:

$$a. \nabla^2 \varphi = 0 \tag{10}$$

b. From equation (7), the velocity normal to the boundary due to the disturbance and due to the onset flow must be of equal magnitude, but opposite sign. Then from equation (9)

$$\left(\frac{\partial \varphi}{\partial \mathbf{n}}\right)_{\Gamma} = \mathbf{n}(\mathbf{p}) + \mathbf{V}_{\infty} \tag{11}$$

Note that the normal vector is a function of position on the surface of the body.

c. The disturbance potential approaches zero as the distance from the body goes to infinity, i. e.

$$\phi \rightarrow 0$$
 as $|\mathbf{r}| \rightarrow \infty$ (12)

3.2 MATHEMATICAL MODEL

The disturbance potential of the body may be represented by a distribution of a source density function σ over the body surface. The potential at an arbitrary point P(x, y, z) due to the surface potential is (Kellogg 1929):



$$\psi(x, y, z) = \iint \frac{\sigma(q)}{r(P, q)} d\Gamma \tag{13}$$

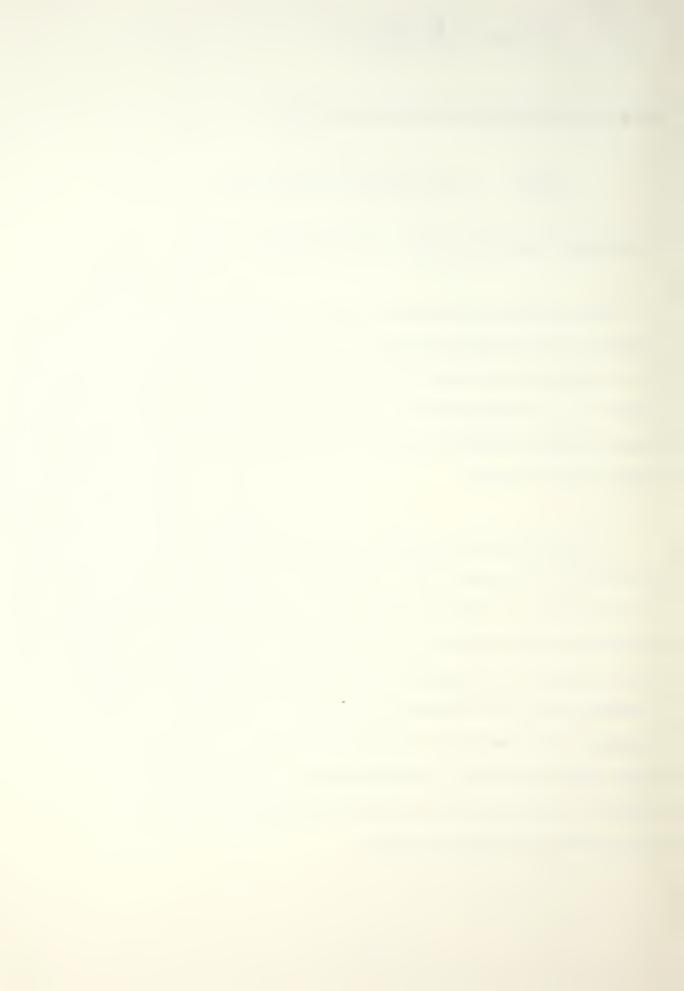
where q is the integration point on the surface, and

$$r(P,q) = \sqrt{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2}$$

is the distance from the field point P to the integration point q.

The source density distribution function must satisfy the boundary conditions for the disturbance potential. Boundary conditions (10) and (12) are automatically satisfied by the form of the integrand. However, equation (11), the velocity normal to the boundary, combined with the Neumann boundary condition, equation (7), is the key to solving the boundary integral problem.

The integrand becomes singular as the surface of the body is approached, i. e. $|\mathbf{r}|$ goes to zero. The singularity represents the local fluid flux normal to the boundary due to the local source density. The principal value of the singularity is $-2\pi\sigma(p)$, determined through a limiting process of the Gauss Flux Theorem (Kellogg 1929). The point prepresents a field point which lies on the boundary. The integral expression is now composed of the contribution of the local source density and the contribution of the source density function over the remainder of the body surface. Solving for the velocity normal to the surface yields the following expression:



$$\left(\frac{\partial \Psi}{\partial n}\right)_{\Gamma} = -2\pi\sigma(p) + \iint \frac{\partial}{\partial n} \left[\frac{\sigma(q)}{r(p,q)}\right] d\Gamma \tag{14}$$

From equation (11), this expression becomes:

$$2\pi\sigma(p) - \iint \frac{\partial}{\partial n} \left[\frac{\sigma(q)}{r(p,q)} \right] d\Gamma = -\mathbf{n}(p) \cdot \mathbf{V}_{\infty}$$
 (15)

This equation is a two dimensional Fredholm integral equation of the second kind, which ensures a unique solution, and that the diagonal elements of the system matrix will be dominant, each having a value of 2π (Kellogg 1929). Once equation (15) has been solved for the source density σ , the velocity components at any point of the flow field may be obtained by differentiating the disturbance potential function (13) with respect to the coordinate directions and adding the components of the freestream flow, \mathbf{V}_{∞} .

$$\mathbf{V}(x, y, z) = \mathbf{V}_{\infty} - \frac{\partial \Phi}{\partial x} \mathbf{i} - \frac{\partial \Phi}{\partial y} \mathbf{j} - \frac{\partial \Phi}{\partial z} \mathbf{k}$$
 (16)

The body shape does not have to be slender, axisymmetric, or simply connected, allowing for analysis of interior flow and a wide range of applications of the method. The only restriction imposed on the form of the body is that it must have a continuous normal vector.

Discontinuities in the right hand side of equation (15) will produce unwanted singularities. Thus, in the process of approximating a body which has distinct corners, where there is clearly a discontinuity in the normal vector, the corner must be replaced by a surface with some finite



where p_{∞} is the static pressure at infinity.

3.3 NUMERICAL MODEL

In order to represent the surface of a body in the domain mathematically, the body may be described by analytical expressions which may provide an exact representation of the surface. However, the types of bodies which can be adequately described by such methods are severely limited. Another way to represent the body is to use a large number of analytical expressions, each describing only a small portion of the body. Hess and Smith (1962) suggested the use of an assembly of flat quadrilateral elements to model the actual surface of the body, as shown in Figure (3). Each quadrilateral approximates a region of the surface described by points which lie on the actual surface of the body. As planar elements, these quadrilaterals are clearly analytical, and when carefully constructed, the elements can approximate arbitrary three dimensional body surfaces without restriction.

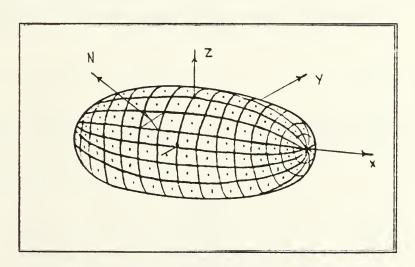


Figure 3. Approximation of the body by surface elements



curvature. However, application of this method has shown that the flow calculations give correct results for convex corners, while unrounded concavecorners may or may not produce significant error, depending on the angle produced by the corner (Hess and Smith 1962).

Because of the method of approximation, the calculation of flow velocities on the body surface are restricted to the points at which the boundary conditions were applied. Velocities at points other than those must be obtained by interpolation. Direct calculation of velocities at the edge of an element yields infinite velocities.

With the solution of the system of linear equations for the source densities, the flow velocities at any point in the domain may be obtained from equation (16), and pressure coefficients are then computed from the velocities using a form of the Bernoulli equation:

$$P(t) = \frac{p}{p} + \frac{1}{2} |\mathbf{V}|^2 + \frac{\partial \Phi}{\partial t}$$
 (17)

where P(t) is a constant independent of position. In the XYZPF Program, the flow is steady. Therefore, equation (17) can be reduced to

$$p + \frac{1}{2} \rho |\mathbf{V}|^2 = constant \tag{18}$$

and the pressure field can be expressed in terms of a dimensionless pressure coefficient $C_{\rm D}$ as:

$$C_{p} = \frac{p - p_{\infty}}{\frac{1}{2} p |\mathbf{V}_{\infty}|^{2}} = 1 - \frac{|\mathbf{V}|^{2}}{|\mathbf{V}_{\infty}|^{2}}$$
(19)



The XYZPF Program uses the discretization procedure described by Hess and Smith (1962) with some minor modifications. The three dimensional body surface may be described using a large number of plane quadrilateral elements, each assumed to have a constant source density over the area of each element. Regions of the body requiring higher resolution for sharp curvature or anticipated velocity gradients will require a higher concentration of elements.

Because the plane quadrilateral elements cannot fit edge to edge on a rounded surface, small gaps in the panel approximation contribute to the error of the approximation. However, the error due to the gaps is negligible when compared with the error of the basic model, that is, using flat panels to approximate a curved surface. Triangular elements have been suggested in an attempt to eliminate the gaps (Levy 1959), but the increased accuracy is so small that it may not justify the additional work of organizing the triangular elements in lieu of the simpler quadrilaterals (Hess and Smith 1966). The method presented is valid for an polygonal element with any number of sides.

Equation (15) can now be decomposed into a summation of integrals, each representing the contribution of one element of the body surface. The unknown source density can be taken outside the integral, since it is assumed to be a constant over each element. The integration is performed over the area of the source element, and the boundary condition equation (11) is then enforced at a single point p in each remaining element. By performing this operation at each element of the



surface, a system of linear equations is generated which is equal in number to the number of surface elements and the number of unknown source densities. Equation (15) can now be approximated by the matrix equation (Dawson and Dean 1972):

$$\sigma_{i} = \sum_{j} \sigma_{j} C_{ij} + V_{i}$$

$$C_{ij} = \frac{1}{2\pi} \iint_{j} \frac{\partial}{\partial n_{i}} \left[\frac{1}{r_{ij}} \right] dA$$

$$C_{ii} = 0$$

$$V_{i} = -\frac{1}{2\pi} \left[n_{i} \cdot V_{\infty} \right]$$
(20)

It is important to note that the influence coefficients C_{ij} and C_{ii} are functions of geometry only, and once computed, need not be recomputed for analysis of several different flows. From the solution of equation (20) on the discretized surface, equation (13) may be applied at any point in the domain. Then, the velocity at an arbitrary field point P(x, y, z) in the domain may be determined from equation (16). With the velocity known, the pressure coefficient is determined from equation (19).



4.0 ORGANIZATION OF THE PROGRAM

The XYZPF Program is actually composed of seven independent programs, referred to as sections PF1 through PF7, each of which builds on data generated from a previous section. This type of organization allows the user the flexibility of rerunning portions of the program using different flow parameters without having to go through the time consuming process of recalculating the influence coefficient matrix, which is dependent only on the geometry of the body. While the NSRDC program is very similar to the Hess program, there are also some significant differences. The following list of differences is taken from NSRDC Report 3892 (Dawson and Dean 1972):

- (1) The input to XYZ PF is arranged to facilitate the preparation of input for a series of problems in which only one part of the body is changed. Also, a number of checks are made on the input to help detect errors.
- (2) An option was added for the recomputation of the source density and velocities for only part of the body when only small changes are made. This option also provides for the use of the solution of one problem as an initial guess for the solution of another problem.
- (3) The matrix of influence coefficients is computed column by column instead of row by row. This column arrangement was used for the original LARC computer version because it required much less high speed memory. The computation is also about 10% faster this way than with the row-by-row arrangement.
 - (4) A simultaneous displacement iterative scheme is used to solve



the matrix coefficient for the source density. The scheme is slower than the successive displacement (Gauss-Seidel) scheme used in the Hess program, but it can be carried out using the matrix column by column instead of row by row.

(5) When possible, an extrapolation procedure is used to reduce the number of iterations required for convergence. One such method is the Richardson extrapolation.

The methods used in the XYZPF Program will be discussed in detail in the following sections.



5.0 DETAILS OF THE SURFACE APPROXIMATION

5.1 PREPARATION OF THE INPUT

Section PF1 is set up to read and store the input data, and to examine the cornerpoints of the quadrilaterals to detect obvious errors in the input. Because of the number of points which may have to be entered for a complex geometry, the user input is a major source of program error, and this first look for input errors will save lot of run time in the program as a whole. If Section PF1 detects major errors in the input, the program will not continue with the calculation of the coefficient matrix, but will stop and identify the grid location of the error. Minor errors may not cause the program to stop, but will be noted in the output.

One of the major advantages to this program is in the organization of the input data. The surface is input in sections so that small portions of the input geometry may be changed without having to recalculated the points for the entire surface. The program also takes advantage of symmetry to minimize the input effort. Only the portion of the body which has no redundancy needs to be entered point by point. The remainder of the body is reflected across the planes of symmetry by the program to complete the surface representation.

The surface is represented by a set of points in three-dimensional space which lie on the actual surface, and which will later be used to define the plane quadrilateral source elements. These points are defined in the global reference system. The points on the surface should be



selected in such a way as to provide an accurate representation of the surface with the fewest number of points possible. Portions of the surface which are highly curved will require a larger number of points to provide adequate resolution. Additionally, portions of the surface in which the flow field is expected to change rapidly will require a large number of points to accurately determine the flow field in that region. Some familiarity with fluid dynamics will provide a somewhat intuitive approach to properly distributing the elements. Elements should change gradually in size from areas of high concentration to those of just a few large elements, changing no more than 50 percent in size between adjacent elements (Hess and Smith 1966). The accuracy is only as good as that provided by the largest element in a particular area. The use of quadrilateral elements facilitates the use of known analytical equations and body contours to determine the input points.

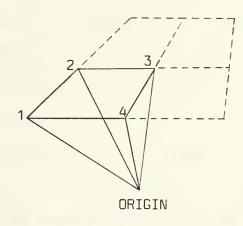


Figure 4. The 3D quadrilateral element in global coordinates

For the purposes of this program, the body surface is represented by a large number of plane quadrilateral elements as shown in figure (3), each of which is assumed to have a constant value of source density over the area of the element. Each element is defined by four input points



which lie on the actual surface as shown in figure (4). Since each input point can be used as a corner for up to four elements, there is no need to enter the same point four separate times. The input points are organized in groups of four to form the quadrilateral element, and each point may also be associated with adjacent quadrilaterals. This is accomplished through the use of a two dimensional coordinate system in which the user assigns a pair of integers, m and n, to each point which identifies the "row" and the "column" in which it lies. A column of points will be given a common value of n, and each point in that column will have a unique value of m corresponding to the row in which the point lies. The orientation of these "coordinate" integers determines the direction of the outward normal for each element. Looking from the flow field toward the section of elements, if the values of m are increasing upward, the values of n must increase to the right. Increasing m and n can point in any direction with respect to the global reference system. In fact, the orientation can change from one section to another. However, any other relationship between m and n will produce an incorrect normal vector. Once assigned, the values of m and n also serve to identify the element for which the corresponding point is a corner. The four points which form a quadrilateral element are two points of one column, or n line, with consecutive m numbers, and two points of the next higher n line with the same m numbers as the previous two points. Thus, the element m, n is composed of the points identified by (m, n), (m+1, n), (m, n+1), and (m+1, n+1).



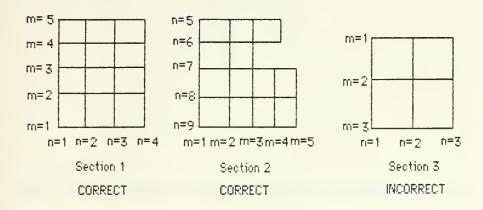


Figure 5. Quadrilateral index numbers

Each section of the body surface is formed by specifying a set of corner points corresponding to the m, n pairs for all of the quadrilaterals of the section. The user will sequentially assign an m number to the points for each n line, and also number the n lines for the section points entered. The first point in each n line will always have m = 1. The n lines are also numbered sequentially, but the value of n is not reset for each new section. The sequence of n numbers runs through all the sections as shown in figure (5). Points on a particular row or column do not have to be strictly colinear. By forming nearly triangular elements, a rounded planform can be approximated without conflicting with the numbering convention, as shown in figure (6).



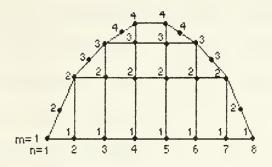


Figure 6. Approximating a thin region with rounded planform (Hess & Smith 1962)

By entering data in sections, small changes in geometry can be performed without having to reenter all the points associated with the body surface. This feature is unique to the XYZPF Program, and offers a great deal of flexibility in design work. However, with the added flexibility comes more restrictions on both the input of the original geometry and on any modifications. There are four important restrictions on the input which are required to provide quadrilateral elements in groups of four to facilitate geometry calculations (Dawson and Dean 1972):

- (1) There must be an even number of elements in both the m and n directions in each section of the body.
- (2) The common corner point of a group of four elements must not coincide with any other corner point. The sides between the elements serve to define the local coordinate system, and serve as the axis of rotation when the surface is flattened for numerical differentiation of



the velocity potential.

- (3) Each set of four elements must have at least seven distinct corner points to allow the elements to more closely conform to a curved surface. This also allows for convergence of N-lines or M-lines as may occur, for example, at the leading edge of an ellipsoid. Thus, only two of the four quadrilateral may degenerate into triangles by having two of their corner points coincide. This does not necessarily eliminate the possibility of more than two "triangular" elements since the adjacent sides of a quadrilateral may be colinear as shown in figure (6).
- (4) The normal vectors between two adjacent quadrilaterals in a group of four must be less than 90 degrees and preferably less than 45 degrees. If a sharp edge is required, it should be a concavecorner with respect to the flow field, and the input should be arranged so that the edge is along an outside boundary of the groups of four, and not through the center.

When making small changes to the original geometry, the number of elements used in a new section must be the same as the number used in the original section unless the part being changed is at the end of the input data. Section configurations may be selected by natural divisions, as a matter of convenience to more easily handle large numbers of points, or as a tool to take advantage of symmetry.

In setting up input data to use planes of symmetry, it is important to note that the XYZPF Program has certain restrictions on the choice of



symmetry planes. The user only has the option to select the number of symmetry planes. The planes which will be used as symmetry planes are preselected by the program to optimize the calculation procedure.

Therefore, knowing this, the preparation of input data must consider the following restrictions imposed by the program (Dean and Dawson 1972).

If only one plane of symmetry is used, the plane of symmetry is the y = 0 plane of the global coordinate system. As such, all the y coordinates of the input points must be of the same sign, i. e., all positive or all negative. If the body is closed and intersects the plane of symmetry, the points touching the plane, i. e., corresponding to y = 0, must also be entered with the input points.

If two planes of symmetry are used, the planes of symmetry are the y = 0 plane and the z = 0 plane in the global coordinate system. Again, the y coordinates of all input points must have the same sign, positive or negative, and the z coordinates of all points must be of the same sign, positive or negative without regard to the sign of y. If the body surface intersects one or both of the planes of symmetry, the points which lie in the plane, i. e., those corresponding to y = 0 or z = 0, must also be entered with the input points.

If three planes of symmetry are used, clearly the planes are the reference planes of the global coordinate system. As with the previous cases, all the x coordinates of the input points must be of the same sign, and similarly for the y and z coordinates. If any part of the body intersects any of the planes of symmetry, the points which lie in that



plane, i. e., x = 0, y = 0 or z = 0, must also be entered with the input points.

5.2 SOURCE PANEL GEOMETRY

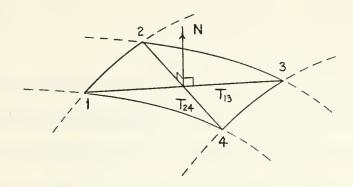


Figure 7. The outer normal to the quadrilateral element

With the surface points identified by the location numbers, m and n, and arranged in accordancewith program requirements, calculation of various aspects of the source panel geometry and formation of the plane quadrilateral element is the next step in the numerical integration process. Formation of all of the planar elements is identical, so the following discussion of source panel geometry will deal with only one characteristic element. The four corner points forming the basic quadrilateral are numbered in a clockwise direction from 1 to 4 as shown in figure (7). It does not matter which corner point is identified with the number 1 subscript, but the remaining points must be numbered consecutively in a clockwise direction when observed from the flow field in order to ensure an outward directed normal vector. These subscripts will be used to identify the corner points for the remainder of this discussion. For this example, the points will be identified as follows:



| Position Numbers | Global Coordinates |
|------------------|-----------------------|
| m, n | X_1 , Y_1 , Z_1 |
| m+1, n | X_2 , Y_2 , Z_2 |
| m+1, n+1 | X_3 , Y_3 , Z_3 |
| m, n+1 | X_4 , Y_4 , Z_4 |

In forming the plane quadrilateral elements, the corner points, which are generally not coplanar, are used to form the local coordinate system, relative to the element. Recalling that the cross product of two vectors yields a vector solution which is perpendicular to both of the original vectors, the normal to the element may be obtained from the cross product of the diagonals of the element.

$$N = T_{24} \times T_{13}$$
 (21)

where T_{13} is the vector from point 1 to point 3, and T_{24} is the vector from corner point 2 to point 4. The unit normal is then:

$$\mathbf{n} = \frac{T_{24} \times T_{13}}{|T_{24} \times T_{13}|} \tag{22}$$

This unit normal now represents the first of the three local coordinate directions, this one in the ζ direction. The side of the quadrilateral from point 2 to point 3 is then used to obtain the second coordinate vector.



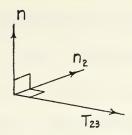


Figure 8. The second local coordinate vector

$$N_2 = n \times T_{23} \tag{23}$$

and the unit vector

$$\mathbf{n}_2 = \frac{\mathbf{N}_2}{|\mathbf{N}_2|} \tag{24}$$

Similarly, the third local coordinate vector is obtained from the crossproduct of \mathbf{n}_2 and \mathbf{n} , the result of which is a unit vector.

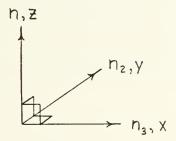


Figure 9. The third local coordinate vector

$$\mathbf{n}_3 = \mathbf{n}_2 \times \mathbf{n} \tag{25}$$

The unit vectors \mathbf{n}_3 , \mathbf{n}_2 , and \mathbf{n} form an orthonormal basis and define the local coordinate system for the element in the ξ , η , and ζ directions



respectively. Other methods of obtaining an orthonormal basis could be used just as well, and would make no difference to the remaining computations. The origin of the local coordinate system would most correctly be located at the "null point," the point at which the velocity potential has no contribution to the tangential velocity component on the source element. The null point is the point in each quadrilateral element where the normal velocity boundary condition is applied. However, with the exception of long, thin quadrilaterals, the physical difference between the null point and the centroid of the quadrilateral is not significant. The XYZPF Program will print a warning in the output when a quadrilateral is long and thin enough to jeopardize the accuracy of the approximation in that region. By locating the origin of the local coordinate system at the centroid, rather than at the null point, the difficult process of locating the null point for each element can be eliminated, later calculations of the multipole expansion can be simplified, and the boundary conditions can be applied at the centroid without contributing significant error to the approximation (Hess and Smith 1966). Therefore, the origin for each local coordinate system is located at the centroid for the respective element.



5.3 LOCATING THE CENTROID

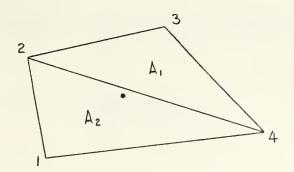


Figure 10. Locating the centroid of the quadrilateral

The centroid of the element may be calculated by first dividing the area of the quadrilateral into two triangular areas, the triangles being separated by the line from point 2 to point 4. The area A_1 of the triangle defined by corner points 2, 3, and 4 is

$$A_1 = \frac{1}{2} | T_{24} \times T_{23} | \tag{26}$$

Similarly, the area A_2 of the triangle defined by corner points 1, 2, and 4 is

$$A_2 = \frac{1}{2} |T_{12} \times T_{14}| \tag{27}$$

In the global coordinate system, the X component of the centroid is given by

$$\overline{X} = \frac{A_1 \overline{X}_1 + A_2 \overline{X}_2}{A_1 + A_2} \tag{28}$$

where X_1 and X_2 are the averages of the X components of the corner points of each triangle. Substituting the values for X_1 and X_2 :



$$\overline{X} = \frac{\frac{1}{3} A_1 (X_2 + X_3 + X_4) + \frac{1}{3} A_2 (X_1 + X_2 + X_4)}{A_1 + A_2}$$

$$= \frac{1}{3} \left[\frac{(A_1 + A_2) X_2 + (A_1 + A_2) X_4 + A_1 X_3 + A_2 X_1}{A_1 + A_2} \right]$$

$$= \frac{1}{3} \left[\frac{X_2 + X_4 + \frac{A_1 X_3 + A_2 X_1}{A_1 + A_2}}{A_1 + A_2} \right]$$
(29)

Similarly

$$\nabla = \frac{1}{3} \left[Y_2 + Y_4 + \frac{A_1 Y_3 + A_2 Y_1}{A_1 + A_2} \right]$$
 (30)

$$\overline{Z} = \frac{1}{3} \left[Z_2 + Z_4 + \frac{A_1 Z_3 + A_2 Z_1}{A_1 + A_2} \right]$$
 (31)

5.4 COORDINATE TRANSFORMATION

Now that the local coordinate system is formed and properly located at the centroid of the element, the global coordinates of the corner points (X, Y, Z) are transformed to local coordinates (ξ , η , ζ) through the components of the reference vectors of the local coordinate system as follows:

$$\begin{bmatrix} \mathbf{n}_{3_{\times}} & \mathbf{n}_{3_{y}} & \mathbf{n}_{3_{z}} \\ \mathbf{n}_{2_{\times}} & \mathbf{n}_{2_{y}} & \mathbf{n}_{2_{z}} \\ \mathbf{n}_{\times} & \mathbf{n}_{y} & \mathbf{n}_{z} \end{bmatrix} \begin{bmatrix} \times - \overline{\times} \\ y - \overline{y} \\ z - \overline{z} \end{bmatrix} = \begin{bmatrix} \dot{\xi} \\ \eta \\ \dot{\zeta} \end{bmatrix}$$
(32)



The corner points are projected into the plane of the quadrilateral element by setting the ζ components to zero. The original diagonal vectors, T_{13} and T_{24} , will be on opposite sides of the resulting plane. The plane quadrilateral element is now completely defined. The program will sweep through all of the input elements using the assigned location numbers, and repeat this process for each element.

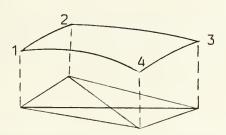


Figure 11. Forming the plane quadrilateral element

5.5 MOMENTS OF INERTIA

The calculation of the moments of inertia for each element are performed for use in the computation of the velocity coefficients using the quadrupole method. Any calculus text will give the moments of inertia of a planar section with a constant unit density about the origin to be:

$$I_{xx} = \iint_{A} \xi^2 d\xi d\eta$$
 (33)

$$I_{gg} = \iint_{\Lambda} \eta^2 \, d\xi \, d\eta \tag{34}$$

$$I_{yy} = \iint_{A} \eta^{2} d\xi d\eta \qquad (34)$$

$$I_{xy} = \iint_{A} \xi \eta d\xi d\eta \qquad (35)$$



For the triangular region defined by the corner points 2, 3, and 4,

$$I_{xx} = \frac{A}{12} \left[(\xi_2 + \xi_3)^2 + (\xi_3 + \xi_4)^2 + (\xi_4 + \xi_2)^2 \right]$$
 (36)

$$I_{yy} = \frac{A}{12} \left[(\eta_2 + \eta_3)^2 + (\eta_3 + \eta_4)^2 + (\eta_4 + \eta_2)^2 \right]$$
 (37)

$$I_{xy} = \frac{A}{12} \left[(\xi_2 + \xi_3)(\eta_2 + \eta_3) + (\xi_3 + \xi_4)(\eta_3 + \eta_4) + (\xi_4 + \xi_2)(\eta_4 + \eta_2) \right]$$
(38)

Similar equations can be generated for the triangular region defined by the corner points 1, 2, and 4. The moment of inertia for the entire quadrilateral is the sum of the corresponding expressions for each of the triangles. The resulting equations are:

$$I_{xx} = \frac{A}{12} \left[(\xi_2 + \xi_3)^2 + (\xi_3 + \xi_4)^2 + (\xi_4 + \xi_2)^2 \right]$$

$$+ \frac{A}{12} \left[(\xi_1 + \xi_2)^2 + (\xi_2 + \xi_4)^2 + (\xi_4 + \xi_1)^2 \right]$$
(39)

$$I_{yy} = \frac{A}{12} \left[(\eta_2 + \eta_3)^2 + (\eta_3 + \eta_4)^2 + (\eta_4 + \eta_2)^2 \right]$$

$$+ \frac{A}{12} \left[(\eta_1 + \eta_2)^2 + (\eta_2 + \eta_4)^2 + (\eta_4 + \eta_1)^2 \right]$$
(40)

$$I_{xy} = \frac{A}{12} \left[(\xi_2 + \xi_3)(\eta_2 + \eta_3) + (\xi_3 + \xi_4)(\eta_3 + \eta_4) + (\xi_4 + \xi_2)(\eta_4 + \eta_2) \right]$$

$$+ \frac{A}{12} \left[(\xi_1 + \xi_2)(\eta_1 + \eta_2) + (\xi_2 + \xi_4)(\eta_2 + \eta_4) + (\xi_4 + \xi_1)(\eta_4 + \eta_1) \right]$$



6.0 THE MATRIX OF INFLUENCE COEFFICIENTS

with the quadrilaterals completely formed, the next step is to calculate the velocities induced by the elements at the centroids of all the other elements. The total number of elements forming the surface will be represented by N. Let the source element be the (j)th element, and the element for which the velocity components are to be calculated at the centroid is the (i)th element. It does not matter how the (i)th elements are arranged in relation to each other as the sequence progresses. However, the sequence must be consistent as the calculations proceed from one source element to another. This program sweeps through the (i)th elements in the order of their location numbers, m and n. For each consecutive n line, the elements are swept in order of increasing m numbers.

The result of the induced velocity calculations for the elements with unit source densities is an N by N square matrix of the values of induced velocities at each element, known also as the "matrix of influence coefficients." The XYZ potential flow program calculates the coefficients column by column, while the Hess program calculates them row by row. The advantage of one over the other depends on the method of later solving the matrix for the source densities. In calculating the influence coefficients, twenty-five quantities which describe the geometry of the source element are required to adequately calculate the induced velocity at the centroid of the (i)th element. These quantities include the coordinates of the centroid in the global coordinate system, the elements of the coordinate transformation matrix, the local



coordinates of the corner points, the maximum diagonal, the area, and the second moments of the quadrilateral element. Additionally, the Hess program uses the coordinates of the null point, making a total of twenty-eight quantities for that method (Hess and Smith 1962).

When calculating row by row, the first (i)th element is selected, containing the "null" point, and the influence coefficients are computed for all of the (j)th elements in sequence before proceeding to the (i+1)th element. This procedure requires the twenty-five quantities for each (i)th element to be available for calculation of the influence coefficient. Because each of the N (i)th elements is used N times with this procedure, calculating the geometric quantities or retrieving the values from low speed memory would be very time consuming, since the calculations or memory access would need to be performed N² times. Therefore, it is more practical to have the values available in high speed memory, although large matrices may exceed the storage capacity of high speed memory, imposing a limit on the number of elements which can be used. The advantage to the row-by-row calculation is that solution of the resulting matrix by the Gauss-Seidel reduction method does not require transposing the matrix, which would be another time consuming process (Hess and Smith 1962).

Another alternative is calculation of the influence coefficients column by column. This method calculates the influence coefficients by sweeping all the (i)th elements for each (j)th element before proceeding to the (j+1)th element. Therefore, the twenty-five geometric quantities are retrieved from low speed storage only once for each (j)th element,



for a total of N times. This procedure is not limited by the capacity of high speed memory, and calculation of the coefficient matrix is approximately 10% faster than the row-by-row method (Dawson and Dean 1972). This is the calculation method used by the XYZ Potential Flow Program.

An influence coefficient represents the combined effects on one element of the velocity potentials of all the other elements comprising the body surface. For the quadrilateral element with a unit source density in the xy-plane, from equation (13), the potential at point P(x, y, z) due to the element is

$$\phi = \iint_{A} \frac{1}{r} dA = \iint_{A} \frac{d\xi d\eta}{\sqrt{(x - \xi)^{2} + (y - \eta)^{2} + z^{2}}}$$
(42)

The integrand, 1/r, can be expanded in a series about the origin in powers of ξ and η . Each term of the series will contain the product of some powers of ξ and η with a corresponding derivative of 1/r₀, where r₀ is the distance of the field point P from the quadrilateral origin.

$$r_0 = \sqrt{x^2 + y^2 + z^2}$$

and let

$$w = \frac{1}{r_0}$$

Then the series expansion through the second order term is (Hess and Smith 1962):



$$\varphi = Aw - (M_X w_X + M_U w_U) + 1/2(I_{XX} w_{XX} + 2I_{XY} w_{XY} + I_{YY} w_{YY}) + \dots$$
 (43)

The subscripts, x and y, used with w represent the respective partial derivatives. This series represents the multipole expansion of the velocity potential, since each term can be interpreted as a point singularity of a particular order. The first term is the potential at point P due to a point source of strength A located at the origin. The second term is the sum of two dipoles of strengths M_{χ} and M_{U} located at the origin, oriented along the x and y axis respectively. The choice of the centroid of the quadrilateral as the origin of the local coordinate system causes the first moments, M_x and M_H , to be zero. Therefore, the dipole terms dissappear, and are not dealt with anywhere in the program. The third term is the sum of three quadrupoles of strengths 1xx, 1xy, and 1yy located at the origin. Kellogg (1929) shows that this second order approximation is absolutely and uniformly convergent, and Hess and Smith (1962) show that convergence is rapid enough with an increase in r_0 that certain further approximations may be made without significant error at large distances r_0 from the source quadrilateral.

Hess and Smith (1962) presented a comparison of velocities calculated using the exact formulas, a simple point source, and a second order approximation. The comparisons were based on the ratio of the distance r_0 , between the centroid of the source quadrilateral and the field point P, to the length of the maximum dimension t, of the source quadrilateral, typically the maximum diagonal. The non-dimensional ratio is then r_0/t . The results show that sufficient accuracy is maintained



while using a simple point source at ratios of $(r_0/t) \ge 4$, using the second order source and quadrupole solution for the range $2.45 \le (r_0/t) < 4$, and using the exact solution for ratios of $(r_0/t) < 2.45$. In any case, the error goes to infinity as the field point approaches the edge of the quadrilateral where calculations indicate an infinite velocity. The XYZ Potential Flow Program uses a monopole source for $(r_0/t) > 4$, the source – quadrupole formulae for $2 < (r_0/t) \le 4$, and the exact formulae for $(r_0/t) \le 2$. Hess and Smith (1962) reported a maximum error of 0.001 in approximating any velocity component using the above criteria.



7.0 DERIVATION OF THE EXACT SOURCE PANEL INTEGRATION

From equations (2) and (42), the components of the velocity at the field point P(x, y, z) due to the source quadrilateral are:

$$V_{x} = -\frac{\partial \phi}{\partial x} = \iint_{\Delta} \frac{(x - \xi) d\xi d\eta}{r^{3}}$$
 (44)

$$V_{y} = -\frac{\partial \varphi}{\partial y} = \iint_{\Delta} \frac{(y - \eta) d\xi d\eta}{r^{3}}$$
 (45)

$$V_z = -\frac{\partial \varphi}{\partial z} = \iint_{\Delta} \frac{z \, d\xi \, d\eta}{r^3} \tag{46}$$

Equations (44), (45) and (46) are evaluated by expressing each of the integrals as the sum of four terms, each term representing the effect of one side of the quadrilateral (Hess and Smith 1962). This method can also be generalized for polygonal elements with any number of sides. The potential function for each side of the quadrilateral is the combined potentials of semi-infinite strips whose boundaries are the side of the quadrilateral and two semi-infinite lines parallel to either the x or y axis. When observed from the domain, and the sides are traversed in a clockwise direction, the source strip on the right will have a source density of $\sigma = +1/2$ and the source strip on the left will have a source density of $\sigma = -1/2$ as shown in figure (12). When the sides are recombined to form the quadrilateral, the source densities outside the quadrilateral cancel each other, and the source densities within the quadrilateral combine to form a source density of $\sigma = +1$. This will be



true for a planar element with any number of sides and in any relative orientation within the plane.

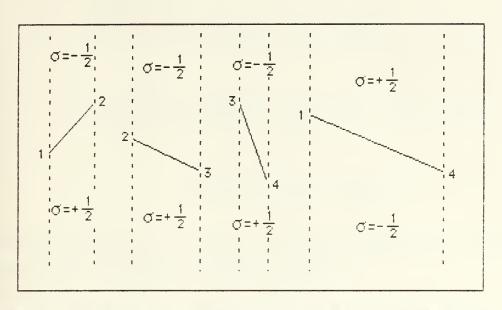


Figure 12. Fundamental potential functions for sides of a quadrilateral (Hess & Smith 1962)

7.1 THE Y VELOCITY COMPONENT

From equation (45), the velocity component V_y is found by summing the four terms representing the contributions of the sides of the quadrilateral. For the side from point (ξ_1, η_1) to point (ξ_2, η_2) , the contribution is expressed as the integral over the area of the semi-infinite strips with the source densities of $\sigma = +1/2$ and $\sigma = -1/2$ rather than the unit source density of equation (45).

$$V_{y_{12}} = \int_{\xi_1}^{\xi_2} d\xi \left[\frac{1}{2} \int_{-\infty}^{\eta_{12}} - \frac{1}{2} \int_{\eta_{12}}^{\infty} \right] \frac{(y - \eta) d\eta}{r^3}$$
 (47)

$$V_{y_{12}} = \frac{1}{2} \int_{\xi_1}^{\xi_2} d\xi \left[\int_{-\infty}^{\tau_{l_{12}}} - \int_{\tau_{l_{12}}}^{\infty} \right] \frac{(y - \tau_l) d\tau_l}{[(x - \xi)^2 + (y - \tau_l)^2 + z^2]^{3/2}}$$



Integrating with respect to η:

$$\begin{aligned} V_{y_{12}} &= \frac{1}{2} \int_{\xi_{1}}^{\xi_{2}} d\xi \, \left\{ \frac{1}{[(x-\xi)^{2} + (y-\eta)^{2} + z^{2}]^{\frac{1}{2}}} \Big|_{\eta_{12}} \right. \\ &- \frac{1}{[(x-\xi)^{2} + (y-\eta)^{2} + z^{2}]^{\frac{1}{2}}} \Big|_{-\infty} - \frac{1}{[(x-\xi)^{2} + (y-\eta)^{2} + z^{2}]^{\frac{1}{2}}} \Big|_{\infty} \\ &+ \frac{1}{[(x-\xi)^{2} + (y-\eta)^{2} + z^{2}]^{\frac{1}{2}}} \Big|_{\eta_{12}} \end{aligned}$$

The terms evaluated at $\eta = +\infty$ and $\eta = -\infty$ cancel, and the terms evaluated at $\eta = \eta_{12}$ add to obtain the following expression:

$$V_{y_{12}} = \frac{1}{2} \int_{\xi_{1}}^{\xi_{2}} \frac{2 d\xi}{[(x - \xi)^{2} + (y - \eta)^{2} + z^{2}]^{\frac{1}{2}}}$$

$$V_{y_{12}} = \int_{\xi_{1}}^{\xi_{2}} \frac{d\xi}{r}$$
(48)

Equation (48) is changed to a function of arclength s by the relation

$$\frac{d\xi}{ds} = \frac{\xi_2 - \xi_1}{\sqrt{(\xi_2 - \xi_1)^2 + (\eta_2 - \eta_1)^2}} = \frac{\xi_2 - \xi_1}{d_{12}}$$
(49)

where d_{12} is the length of the side of the quadrilateral from (ξ_1, η_1) to (ξ_2, η_2) as shown in figure (13).



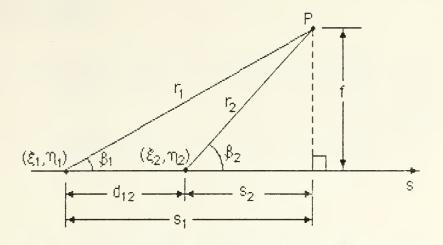


Figure 13. The potential due to a finite line source (Hess & Smith 1962)

Substituting equation (49) into equation (48)

$$V_{g_{1g}} = \frac{\xi_2 - \xi_1}{d_{12}} \int_0^{d_{1g}} \frac{ds}{r}$$
 (50)

From figure (13), it can be seen that, in terms of arclength s, the distance r from point P to any point on the line from point 1 to point 2 is given by

$$r = \sqrt{f^2 + (s_1 - s)^2}$$

Substituting into equation (50) yields

$$V_{y_{12}} = \frac{\xi_2 - \xi_1}{d_{12}} \int_0^{d_{12}} \frac{ds}{\sqrt{f^2 + (s_1 - s)^2}}$$

$$= \frac{\xi_2 - \xi_1}{d_{12}} \int_0^{d_{12}} \frac{ds}{\sqrt{f^2 + (s - s_1)^2}}$$
(51)



Evaluating the integral

$$V_{g_{12}} = \frac{\xi_2 - \xi_1}{d_{12}} \log \left[(s - s_1) + \sqrt{f^2 + (s - s_1)^2} \right]_0^{d_{12}}$$

$$= \frac{\xi_2 - \xi_1}{d_{12}} \left\{ \log \left[(d_{12} - s_1) + \sqrt{f^2 + (d_{12} - s_1)^2} \right] - \log \left[(-s_1) + \sqrt{f^2 + (-s_1)^2} \right] \right\}$$

$$= \frac{\xi_2 - \xi_1}{d_{12}} \left\{ \log (r_2 - s_2) - \log (r_1 - s_1) \right\}$$

$$= \frac{\xi_2 - \xi_1}{d_{12}} \log \frac{(r_2 - s_2)}{(r_1 - s_1)}$$
(52)

The quantities r_1 , r_2 , s_1 , and s_2 used in equation (52) are as shown in figure (13). Equation (52) is singular when $r_1 = s_1$, which occurs when the field point P is located anywhere along the line defined by the side of the quadrilateral. This singularity may be removed by using the law of cosines (Hess and Smith 1962).

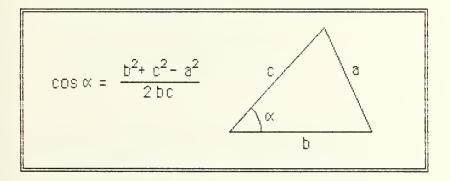


Figure 14. The law of cosines



From equation (52)

$$V_{y_{12}} = \frac{\xi_2 - \xi_1}{d_{12}} \log \frac{r_2(1 - \cos \beta_2)}{r_1(1 - \cos \beta_1)}$$
 (53)

where β_1 and β_2 are the interior angles shown in figure (13). Applying the law of cosines to figure (13)

$$\cos \beta_1 = \frac{r_1^2 + d_{12}^2 - r_2^2}{2 r_1 d_{12}}$$
 (54)

$$\cos \beta_2 = -\frac{r_2^2 + d_{12}^2 - r_1^2}{2r_2d_{12}} = \frac{r_1^2 - d_{12}^2 - r_2^2}{2r_2d_{12}}$$
 (55)

From equations (54) and (55):

$$\frac{r_2(1-\cos\beta_2)}{r_1(1-\cos\beta_1)} = \frac{r_2\left[1-\frac{{r_1}^2-{d_{12}}^2-{r_2}^2}{2{r_2}{d_{12}}}\right]}{r_1\left[1-\frac{{r_1}^2+{d_{12}}^2-{r_2}^2}{2{r_1}{d_{12}}}\right]}$$

$$= \frac{r_2 \left[\frac{2r_2d_{12} - r_1^2 + d_{12}^2 + r_2^2}{2r_2d_{12}} \right]}{r_1 \left[\frac{2r_1d_{12} - r_1^2 - d_{12}^2 + r_2^2}{2r_1d_{12}} \right]}$$

$$= \frac{2r_2d_{12} - r_1^2 + d_{12}^2 + r_2^2}{2r_1d_{12} - r_1^2 - d_{12}^2 + r_2^2} = \frac{(r_2 + d_{12})^2 - r_1^2}{-(r_1 - d_{12})^2 + r_2^2}$$

$$= \frac{[(r_2 + d_{12}) + r_1][(r_2 + d_{12}) - r_1]}{[r_2 + (r_1 - d_{12})][r_2 - (r_1 - d_{12})]} = \frac{r_1 + r_2 + d_{12}}{r_1 + r_2 - d_{12}}$$
(56)



Substituting equation (56) into equation (53) yields the final form of the exact equation of the y component of the velocity induced by the side of the quadrilateral from point 1 to point 2:

$$V_{y_{12}} = \frac{\xi_2 - \xi_1}{d_{12}} \log \frac{r_1 + r_2 + d_{12}}{r_1 + r_2 - d_{12}}$$
 (57)

Equation (57) is applied to the remaining sides of the quadrilateral simply by substituting the appropriate point numbers for the corner points of each side. The total contribution of the quadrilateral to the y component of the velocity is the sum of the four terms representing the contributions of each of the sides. The y component of the velocity at the field point P is now given by:

$$V_{y} = \frac{\hat{\xi}_{2} - \hat{\xi}_{1}}{d_{12}} \log \frac{r_{1} + r_{2} + d_{12}}{r_{1} + r_{2} - d_{12}} + \frac{\hat{\xi}_{3} - \hat{\xi}_{2}}{d_{23}} \log \frac{r_{2} + r_{3} + d_{23}}{r_{2} + r_{3} - d_{23}} + \frac{\hat{\xi}_{4} - \hat{\xi}_{3}}{d_{34}} \log \frac{r_{3} + r_{4} + d_{34}}{r_{3} + r_{4} - d_{24}} + \frac{\hat{\xi}_{1} - \hat{\xi}_{4}}{d_{41}} \log \frac{r_{4} + r_{1} + d_{41}}{r_{4} + r_{1} - d_{41}}$$
(58)

7.2 THE X VELOCITY COMPONENT

A similar derivation process is used to produce the equation for the x component of the velocity induced by the side of the quadrilateral from point 1 to point 2. The semi-infinite source strips are constructed parallel to the x axis, and the order of integration is reversed.



The x component of the velocity at the field point P due to the quadrilateral is given by:

$$V_{x} = \frac{\eta_{2} - \eta_{1}}{d_{12}} \log \frac{r_{1} + r_{2} + d_{12}}{r_{1} + r_{2} - d_{12}} + \frac{\eta_{3} - \eta_{2}}{d_{23}} \log \frac{r_{2} + r_{3} + d_{23}}{r_{2} + r_{3} - d_{23}} + \frac{\eta_{4} - \eta_{3}}{d_{34}} \log \frac{r_{3} + r_{4} + d_{34}}{r_{3} + r_{4} - d_{24}} + \frac{\eta_{1} - \eta_{4}}{d_{41}} \log \frac{r_{4} + r_{1} + d_{41}}{r_{4} + r_{1} - d_{41}}$$
(59)

7.3 THE Z VELOCITY COMPONENT

The z component of the velocity at the field point P due to the quadrilateral is obtained in a similar fashion, using semi-infinite source strips, this time parallel to the y axis. From equation (46), the fundamental velocity potential of the semi infinite source strips is integrated in a manner similar to that used to obtain equation (47), and the z component of the velocity due to the side from (ξ_1, η_1) to (ξ_2, η_2) is given by

$$V_{z_{12}} = \int_{\xi_1}^{\xi_2} d\xi \left[\frac{1}{2} \int_{-\infty}^{\tau_{l_{12}}} - \frac{1}{2} \int_{\tau_{l_{12}}}^{\infty} \right] \frac{z d\eta}{r^3}$$
 (60)

$$V_{z_{12}} = \frac{z}{2} \int_{\xi_{1}}^{\xi_{2}} d\xi \left[\int_{-\infty}^{\tau_{l_{12}}} - \int_{\tau_{l_{12}}}^{\infty} \right] \frac{d\eta}{(x - \xi)^{2} + (y - \eta)^{2} + z^{2}}^{3/2}$$

Performing the integration with respect to η, the integral

$$\int \frac{d\eta}{[(x-\xi)^2+(y-\eta)^2+z^2]^{\frac{3}{2}}}$$



fits the integral form

$$-\int \frac{dF}{[C^2 + F^2]^n} = \frac{-1}{2C^2(n-1)} \left[\frac{F}{[C^2 + F^2]^{n-1}} + (2n-3) \int \frac{dF}{[C^2 + F^2]^{n-1}} \right]$$

where

$$C^2 = (x - \xi)^2 + z^2$$

 $F = (y - \eta)$
 $dF = -d\eta$
 $n = 3/2$

Then, from equation (60)

$$\begin{split} V_{z_{12}} &= -\frac{z}{2} \int_{\xi_{1}}^{\xi_{2}} d\xi \left\{ \frac{(y-\eta)}{[(x-\xi)^{2}+z^{2}][(x-\xi)^{2}+(y-\eta)^{2}+z^{2}]^{\frac{1}{2}}} \Big|_{\eta_{12}} \right. \\ &- \frac{(y-\eta)}{[(x-\xi)^{2}+z^{2}][(x-\xi)^{2}+(y-\eta)^{2}+z^{2}]^{\frac{1}{2}}} \Big|_{-\infty} \\ &- \frac{(y-\eta)}{[(x-\xi)^{2}+z^{2}][(x-\xi)^{2}+(y-\eta)^{2}+z^{2}]^{\frac{1}{2}}} \Big|_{\infty} \\ &- \frac{(y-\eta)}{[(x-\xi)^{2}+z^{2}][(x-\xi)^{2}+(y-\eta)^{2}+z^{2}]^{\frac{1}{2}}} \Big|_{\infty} \end{split}$$

Again, the terms evaluated at $+\infty$ and $-\infty$ cancel and the terms evaluated at η_{12} add to obtain the following expression:

$$V_{z_{12}} = -z \int_{\xi_{1}}^{\xi_{2}} \frac{(y - \eta_{12}) d\xi}{[(x - \xi)^{2} + z^{2}][(x - \xi)^{2} + (y - \eta_{12})^{2} + z^{2}]^{\frac{1}{2}}}$$
(62)



Without a convenient substitution with which to integrate equation (62), the integration is performed directly. Recognizing that along the line defined by the side of the quadrilateral from (ξ_1, η_1) to (ξ_2, η_2) , η_{12} may be expressed as a function of ξ :

$$\eta_{12} = m_{12} \ \xi + b_{12} \tag{63}$$

where the slope of the side, m₁₂ is given by

$$m_{12} = \frac{\eta_2 - \eta_1}{\xi_2 - \xi_1} \tag{64}$$

and b_{12} may be determined knowing that $\eta_{12}=\eta_1$ when $\xi=\xi_1$.

$$b_{12} = \frac{\xi_2 \eta_1 - \xi_1 \eta_2}{\xi_2 - \xi_1} \tag{65}$$

Substituting equation (63) into equation (62) yields

$$V_{z_{12}} = -z \int_{\xi_1}^{\xi_2} \frac{(y - m_{12}\xi - b_{12}) d\xi}{[(x - \xi)^2 + z^2][(x - \xi)^2 + (y - m_{12}\xi - b_{12})^2 + z^2]^{\frac{1}{2}}}$$
(66)

Define the quantities

$$q_{12} = y - b_{12} - m_{12}x \tag{67}$$

$$U = X - \xi \tag{68}$$

Then
$$du = -d\xi$$
 (69)

$$y - b_{12} - m_{12}\xi = m_{12}u + q_{12}$$
 (70)



By a change of variable, equation (66) is now expressed as a function of u:

$$V_{z_{12}} = z \int_{x-\xi_1}^{x-\xi_2} \frac{(m_{12}u + q_{12}) du}{[u^2 + z^2][u^2 + (m_{12}u + q_{12})^2 + z^2]} y_2$$
 (71)

$$=z\int_{x-\xi_{1}}^{x-\xi_{2}} \frac{(m_{12}u+q_{12}) du}{[u^{2}+z^{2}][(m_{12}^{2}+1)u^{2}+2m_{12}q_{12}u+q_{12}^{2}+z^{2}]} \frac{1}{2}$$
(72)

which fits the form of

$$\int \frac{(Lu + M) du}{(Au^2 + 2Bu + C)\sqrt{(au^2 + 2bu + C)}}$$
(73)

where

From Hardy (1944), this integral form may be integrated by the substitution

$$u = \frac{\mu t + \nu}{t + 1} \tag{74}$$

where μ and υ satisfy

$$a\mu v + b(\mu + v) + c = 0$$
 (75)

$$A\mu v + B(\mu + v) + C = 0$$
 (76)

- and are the roots of the equation

$$(aB - bA)\xi^2 - (cA - aC)\xi + (bC - cB) = 0$$
 (77)



Substituting the appropriate values into equation (75), the roots of the quadratic equation are

$$\mu = -\frac{q_{12}}{m_{12}} \tag{78}$$

$$v = \frac{m_{12} z^2}{q_{12}} \tag{79}$$

It can be verified that these values satisfy equations (75) and (76).

Substituting equations (78) and (79) into equation (74)

$$u = \frac{\frac{m_{12}z^2}{q_{12}} - \frac{q_{12}t}{m_{12}}}{t + 1}$$
 (80)

$$du = \begin{bmatrix} -\frac{q_{12}t}{m_{12}} - \frac{m_{12}z^2}{q_{12}} \\ (t+1)^2 \end{bmatrix} dt$$
 (81)

By substitution and a change of variable, equation (72) becomes a function of the parameter t. After simplification, the integral now fits the form of

$$K \left(\frac{dt}{(\alpha t^2 + 8) \sqrt{(\delta t^2 + \delta)}} \right)$$
 (82)

where

$$K = -(m_{12}^{6}q_{12}z^{4} + 2m_{12}^{4}q_{12}^{3}z^{2} + q_{12}^{5}m_{12}^{2})$$

$$\approx = q_{12}^{4} + m_{12}^{2}q_{12}^{2}z^{2}$$



$$\beta = m_{12}^{4}z^{4} + m_{12}^{2}q_{12}^{2}z^{2}$$

$$\delta = q_{12}^{4} + m_{12}^{2}q_{12}^{2}z^{2}$$

$$\delta = m_{12}^{6}z^{4} + m_{12}^{4}z^{4} + 2m_{12}^{4}q_{12}^{2}z^{2} + m_{12}^{2}q_{12}^{4} + m_{12}^{2}q_{12}^{2}z^{2}$$

Equation (82) can be rationalized by the substitution

$$V = \frac{t}{\sqrt{gt^2 + g^2}}$$
 (83)

from which it can be shown that

$$t^2 = \frac{v^2 \delta}{1 - v^2 \delta} \tag{64}$$

$$dt = \left[\frac{\delta}{(1 - v^2 \%)^3} \right]^{\frac{1}{2}} dv$$
 (85)

Substituting equations (84) and (85) into equation (82) and simplifying yields the integral in terms of the parameter v:

$$K \int \frac{dt}{(\alpha t^2 + \beta) \sqrt{(\delta t^2 + \delta)}} = K \int \frac{dv}{\beta + (\alpha \delta - \beta \delta) v^2}$$
(86)

which fits the form

$$\int \frac{dv}{a^2 + b^2 v^2} = \frac{1}{ab} \tan^4 \frac{bv}{a}$$
 (87)

where
$$a^2 = \beta$$

 $b^2 = (\infty \delta - \beta \delta)$



Performing the integration

$$K \int \frac{dv}{\beta + (\alpha \delta - \beta \delta)v^2} = \frac{K}{\sqrt{\beta(\alpha \delta - \beta \delta)}} tan^{-1} \left[v \sqrt{\frac{\alpha \delta - \beta \delta}{\beta}} \right]$$
(88)

From equations (80), (83), and the expressions for α , β , δ , and δ from equation (82), and after a considerable amount of algebraic manipulation and simplification, equation (88) becomes

$$\frac{K}{\sqrt{\beta(\alpha\delta - \beta\delta)}} \tan^{-1} \left[\sqrt{\frac{\alpha\delta - \beta\delta}{\beta}} \right]$$

$$= -\frac{1}{z} \tan^{-1} \left[\frac{m_{12}z^2 - q_{12}u}{z\sqrt{z^2 + u^2 + (m_{12}u + q_{12})^2}} \right]$$
(89)

From equations (63) and (67), equation (89) becomes

$$-\frac{1}{z} \tan^{-1} \left[\frac{m_{12} z^2 - q_{12} u}{z \sqrt{z^2 + u^2 + (m_{12} u + q_{12})^2}} \right]$$

$$= -\frac{1}{z} \tan^{-1} \left[\frac{m_{12} (u^2 + z^2) - (y - \eta_{12}) u}{z \sqrt{u^2 + (y - \eta_{12})^2 + z^2}} \right]$$
 (90)



Finally, applying these results to equation (71)

$$\begin{aligned} V_{z_{12}} &= z \int_{x-\xi_{1}}^{x-\xi_{2}} \frac{(m_{12}u + q_{12}) du}{[u^{2} + z^{2}][u^{2} + (m_{12}u + q_{12})^{2} + z^{2}]^{\frac{1}{2}}} \\ &= -tan^{-1} \left[\frac{m_{12}(u^{2} + z^{2}) - (y - \eta_{12}) u}{z \sqrt{u^{2} + (y - \eta_{12})^{2} + z^{2}}} \right]_{x-\xi_{1}}^{|x-\xi_{2}|} \\ &= tan^{-1} \left[\frac{m_{12}((x - \xi_{1})^{2} + z^{2}) - (y - \eta_{12})(x - \xi_{1})}{z \sqrt{(x - \xi_{1})^{2} + (y - \eta_{12})^{2} + z^{2}}} \right] \\ &- tan^{-1} \left[\frac{m_{12}((x - \xi_{2})^{2} + z^{2}) - (y - \eta_{12})(x - \xi_{2})}{z \sqrt{(x - \xi_{2})^{2} + (y - \eta_{12})^{2} + z^{2}}} \right] \end{aligned}$$
(91)

Recall that when $x = \xi_1$, $y = \eta_1$ and when $x = \xi_2$, $y = \eta_2$. Then, for the sake of a more compact equation, define the following quantities:

$$e_1 = (x - \xi_1)^2 + z^2$$
 $e_2 = (x - \xi_2)^2 + z^2$
 $h_1 = (y - \eta_1)(x - \xi_1)$ $h_2 = (y - \eta_2)(x - \xi_2)$

The quantities r_1 and r_2 are as shown in figure (12), where

$$r_1 = \sqrt{(x - \xi_1)^2 + (y - \eta_1)^2 + z^2}$$
 $r_2 = \sqrt{(x - \xi_2)^2 + (y - \eta_2)^2 + z^2}$

Substituting these quantities into equation (91) yields the exact z component of velocity due to the side from point (ξ_1,η_1) to (ξ_2,η_2) in the form used by the XYZ Potential Flow Program:

$$V_{Z_{12}} = \tan^{-1} \left[\frac{m_{12} \varepsilon_1 - h_1}{z r_1} \right] - \tan^{-1} \left[\frac{m_{12} \varepsilon_2 - h_2}{z r_2} \right]$$
 (92)



The total z component of the velocity at the field point P(x, y, z) due to the quadrilateral element is the sum of the four sides:

$$V_{Z} = \tan^{-1} \left[\frac{m_{12}e_{1} - h_{1}}{z r_{1}} \right] - \tan^{-1} \left[\frac{m_{12}e_{2} - h_{2}}{z r_{2}} \right]$$

$$+ \tan^{-1} \left[\frac{m_{23}e_{2} - h_{2}}{z r_{2}} \right] - \tan^{-1} \left[\frac{m_{23}e_{3} - h_{3}}{z r_{3}} \right]$$

$$+ \tan^{-1} \left[\frac{m_{34}e_{3} - h_{3}}{z r_{3}} \right] - \tan^{-1} \left[\frac{m_{34}e_{4} - h_{4}}{z r_{4}} \right]$$

$$+ \tan^{-1} \left[\frac{m_{41}e_{4} - h_{4}}{z r_{4}} \right] - \tan^{-1} \left[\frac{m_{41}e_{1} - h_{1}}{z r_{1}} \right]$$

$$(93)$$



8.0 APPROXIMATIONS OF THE INDUCED VELOCITY

8.1 QUADRUPOLE METHOD

As previously mentioned, as the ratio of (r_0/t) exceeds the value of 2, then certain approximations may be made which greatly reduce the calculation effort otherwise required by the exact method. In the range of $2 < (r_0/t) \le 4$, the XYZ Potential Flow Program uses the second order approximation of the potential described by equation (43). With the origin at the centroid of the quadrilateral, the first moments are zero, and the second order approximation is

$$\varphi = Aw + (1/2)(I_{xx}w_{xx} + 2I_{xy}w_{xy} + I_{yy}w_{yy})$$
(94)

where the first term is a point source of strength A, the second term is composed of three quadrupoles of strengths I_{xx} , I_{xy} , and I_{yy} located at the local origin, and the subscripts on w indicate the partial derivatives of w with respect to those variables as before. The quantity A is the area of the element, and the terms I_{xx} , I_{xy} , and I_{yy} are the respective moments of inertia of the source element given by equations (39), (40), and (41). To obtain the velocity components at the field point, equation (94) is differentiated with respect to the coordinate directions giving:



$$V_{x} = -\frac{\partial \Psi}{\partial x} = -\left[AW_{x} + \frac{1}{2}I_{xx}W_{xxx} + I_{xy}W_{xxy} + \frac{1}{2}I_{yy}W_{xyy}\right]$$
(95)

$$V_y = -\frac{\partial \phi}{\partial y} = -\left[AW_y + \frac{1}{2}I_{xx}W_{xxy} + I_{xy}W_{xyy} + \frac{1}{2}I_{yy}W_{yyy}\right]$$
 (96)

$$V_z = -\frac{\partial \Phi}{\partial z} = -\left[AW_z + \frac{1}{2} I_{xx} W_{xxz} + I_{xy} W_{xyz} + \frac{1}{2} I_{yy} W_{yyz}\right]$$
 (97)

Recalling that
$$w = \frac{1}{\sqrt{x^2 + u^2 + z^2}} = \frac{1}{r_0}$$

the derivatives of w, as expressed by Hess and Smith (1962) and as used in the XYZPF program, are

$$W_{x} = -x r_{0}^{-3}$$

$$W_{y} = -y r_{0}^{-3}$$

$$W_{z} = -z r_{0}^{-3}$$
(99)

$$W_{xxx} = 3x(3p + 10x^{2}) r_{0}^{-7}$$
 $W_{xxy} = 3y p r_{0}^{-7}$
 $W_{xyy} = 3x q r_{0}^{-7}$
 $W_{yyy} = 3y(3q + 10y^{2}) r_{0}^{-7}$
 $W_{xxz} = 3z p r_{0}^{-7}$
 $W_{xyz} = -15xyz r_{0}^{-7}$
 $W_{yyz} = 3z q r_{0}^{-7}$

where

$$p = y^2 + z^2 - 4x^2$$
$$q = x^2 + z^2 - 4u^2$$



8.2 MONOPOLE METHOD

When the ratio of (r_0/t) is greater than 4, then the quadrilateral may be approximated by a simple source corresponding to the first term of equation (43). Then the velocity components at the field point due to the quadrilateral are given by

$$V_{x} = -\frac{\partial \Psi}{\partial x} = -AW_{x} \tag{101}$$

$$V_{y} = -\frac{\partial \phi}{\partial y} = -Aw_{y} \tag{102}$$

$$V_z = -\frac{\partial \Psi}{\partial z} = -AW_z \tag{103}$$

where the partial derivatives of w are those given in equation (99).



9.0 SOLVING THE MATRIX EQUATION FOR SOURCE DENSITY

9.1 JACOBI'S ITERATIVE METHOD

From equation (20), the matrix equation may be solved for the constant source density σ_i for each element which satisfies the boundary condition equation (11). Equation (20) suggests the use of Jacobi's iterative method of matrix solution in the form

$$\sigma_{i}^{(m+1)} = V_{i} + \sum_{\substack{j=1\\ i \neq i}}^{N} C_{ij} \sigma_{j}^{(m)}, i = 1, 2, ..., N$$
(104)

where N is the number of elements composing the body surface, and m is the number of iterations completed. A partial sum of equation (104) is computed for each of the ith elements before proceeding to the next jth element. The iteration is complete when the summation of equation (104) includes all of the jth elements. Because the values of the source densities at all of the elements are recomputed before any of them are used in the iteration, this method is also called the simultaneous displacement method (Ralston 1965). This is contrasted with the Gauss-Seidel iterative method used in the Douglas program. In the Gauss-Seidel method, as each new σ_i is computed, it is used immediately in the iteration process for calculation of $\sigma_{(i+1)}$. This is also known as the successive displacement method and is expressed as



$$\sigma_{i}^{(m+1)} = V_{i} + \sum_{j=1}^{i-1} C_{ij} \sigma_{j}^{(m+1)} + \sum_{j=i+1}^{N} C_{ij} \sigma_{j}^{(m)}$$

$$i = 1, 2, ..., N$$
(105)

Though the Gauss-Seidel iterative method is faster, the Jacobi iteration method was selected for use in the XYZPF program in order to be able to perform the iterations column by column, since the coefficient matrix is also computed column by column, and the matrix does not have to be transposed for solution.

When the (m+1)th iteration is complete, the values of the source densities are compared with those of the (m)th iteration and the differences summed for all of the elements. The total difference between successive iterations is then compared to a convergence criteria input by the user. If the difference is less than the convergence criteria, then the matrix solution is complete and the values of the source densities are stored for later use in computing velocities and pressure coefficients. If the convergence criteria is not met, then the iteration process is repeated. After every five iterations, if the convergence criteria is still not met, then an extrapolation is attempted in order to accelerate the convergence. The XYZ Potential Flow Program uses a Richardson extrapolation method, a numerical procedure which uses two approximate results to obtain a third approximation which is closer to the exact solution (Ralston 1965).



9.2 RICHARDSON EXTRAPOLATION

The Richardson extrapolation assumes that the iterative process is convergent. For the iterative solutions S_0 , S_1 , and S_2 , where S_0 is the most recent approximation and S_2 the oldest, the solution is convergent if

$$\frac{S_0 - S_1}{S_1 - S_2} = \lambda < 1 \tag{106}$$

While a Richardson-type extrapolation can take may forms, the XYZPF program uses a procedure developed from the following approximations (Dawson and Dean 1972). If there is only one dominant eigenvalue and a sufficient number of iterations have been completed, the iterative solutions may be approximated by

$$S_0 \approx S_f + E \lambda^m$$

$$S_1 \approx S_f + E \lambda^{m-1}$$

$$S_2 \approx S_f + E \lambda^{m-2}$$

$$S_i \approx S_f + E \lambda^{m-i}$$
(107)

where S_f is the true solution

 λ is the eigenvalue

E is the eigenfunction

m is the number of completed iterations

Define the linear combination which, from equation (107), may be



approximated as

$$A S_0 + (1 - A) S_1 \approx S_f + E \lambda^{n-1} (A \lambda + 1 - A)$$
 (108)

The value of A may be chosen such that

$$(A\lambda + 1 - A) = 0 \tag{109}$$

Then, from equations (108) and (109)

$$AS_0 + (1 - A)S_1 \approx S_f$$
 (110)

where the expression on the left converges to the exact solution. From equations (106) and (109)

$$\lambda = \frac{S_0 - S_1}{S_1 - S_2} = 1 - \frac{1}{A} \tag{111}$$

Solving for A,

$$A = \frac{S_2 - S_1}{S_0 - 2S_1 + S_2} = \frac{S_2 - S_1}{D}$$
 (112)

Since the value of A generally changes from element to element, a weighted average of A is used in the extrapolation, where

$$\overline{A} = \frac{\sum_{i=1}^{N} (S_2(i) - S_1(i)) (sign of D(i))}{\sum_{i=1}^{N} D(i)}$$
 (113)

Equation (113) is recomputed after every fifth iteration. If the difference between the new value and the old value is less than 0.02, then the solution is extrapolated. From equation (110), the extrapolated solution is

$$S^* = \overline{A} S_0 + (1 - \overline{A}) S_1$$
 (114)



When there are two dominant eigenvalues, then the iterative solutions may be approximated by

$$S_i \approx S_f + E_1 \lambda_1^{m-i} + E_2 \lambda_2^{m-i}$$
 (115)

where S_f is the true solution λ_1 and λ_2 are the eigenvalues E_1 and E_2 are the eigenfunctions E_1 is the number of completed iterations

Define the linear combination which, from equation (115), may be approximated as

$$B_{2} S_{0} + B_{1} S_{1} + (1 - B_{1} - B_{2}) S_{2}$$

$$\approx S_{f} + E_{1} \lambda_{1}^{m-2} [B_{2} \lambda_{1}^{2} + B_{1} \lambda_{1} + (1 - B_{1} - B_{2})]$$

$$+ E_{2} \lambda_{2}^{m-2} [B_{2} \lambda_{2}^{2} + B_{1} \lambda_{2} + (1 - B_{1} - B_{2})]$$
(116)

The values of B_1 and B_2 may be determined for which the eigenvalues λ_1 and λ_2 are roots of the quadratic equation

$$B_2 \lambda^2 + B_1 \lambda + (1 - B_1 - B_2) = 0$$
 (117)

Then, from equation (116)

$$B_2 S_0 + B_1 S_1 + (1 - B_1 - B_2) S_2 \approx S_f$$
 (118)



where the left side of the equation (118) converges to the exact solution. Using equation (115) and eliminating terms containing E_2 :

$$(S_{0} - S_{1}) - \lambda_{2} (S_{1} - S_{2}) = E_{1} \lambda_{1}^{n-2} (\lambda_{1} - \lambda_{2})(\lambda_{1} - 1)$$

$$(S_{1} - S_{2}) - \lambda_{2} (S_{2} - S_{3}) = E_{1} \lambda_{1}^{n-3} (\lambda_{1} - \lambda_{2})(\lambda_{1} - 1)$$

$$(S_{2} - S_{3}) - \lambda_{2} (S_{3} - S_{4}) = E_{1} \lambda_{1}^{n-4} (\lambda_{1} - \lambda_{2})(\lambda_{1} - 1)$$

$$(119)$$

Solving for λ_1

$$\lambda_1 = \frac{(S_0 - S_1) - \lambda_2(S_1 - S_2)}{(S_1 - S_2) - \lambda_2(S_2 - S_3)} = \frac{(S_1 - S_2) - \lambda_2(S_2 - S_3)}{(S_2 - S_3) - \lambda_2(S_3 - S_4)}$$
(120)

From equations (117) and (120)

$$B_1 = \frac{(S_4 - S_3)(S_0 - 2S_2 + S_4) - (S_4 - S_2)[(S_1 - S_2) - (S_3 - S_4)]}{D}$$
(121)

$$B_2 = \frac{(S_4 - S_2)(S_4 - 2S_3 + S_2) - (S_4 - S_3)[(S_1 - S_2) - (S_3 - S_4)]}{D}$$
(122)

where
$$D = (S_4 - 2S_3 - S_2)(S_0 - 2S_2 + S_4) - (S_1 - S_2 - S_3 + S_4)^2$$

The weighted averages of B_1 and B_2 are used for the extrapolation as done with A in equation (113). If the sum of the absolute values of the weighted averages of B_1 and B_2 changes by less than 2%, then the extrapolation is performed. Then from equation (118), the extrapolated solution is

$$S* = \overline{B_2}S_0 + \overline{B_1}S_1 + (1 - \overline{B_1} - \overline{B_2})S_2$$
 (123)



10.0 CALCULATION OF VELOCITIES AND PRESSURE COEFFICIENTS

With the influence coefficients and the source densities determined, the calculation of velocities is a relatively simple matter. From equation (9), the total velocity is the sum of the freestream velocity and the disturbance velocity due to the body. The product of the source densities and the influence coefficients are summed for all of the elements, and then added to the freestream velocity to determine the total velocity at any point in the domain. Velocities on the surface of the body are calculated at the null points only, as the boundary conditions are enforced only at the null point of each element, and velocities at other points in the element would produce significant error due to the method of approximation. The components of the velocity at the centroid of the ith element are

$$V_{i_{x}} = V_{\infty_{x}} + \sum_{j=1}^{N} C_{ij_{x}} \sigma_{j}$$

$$V_{i_{y}} = V_{\infty_{y}} + \sum_{j=1}^{N} C_{ij_{y}} \sigma_{j}$$

$$V_{i_{z}} = V_{\infty_{z}} + \sum_{j=1}^{N} C_{ij_{z}} \sigma_{j}$$

$$(124)$$

From equation (15), the velocity induced by an element at its own null point has a magnitude of 2π directed along the outward normal vector of the element.



At a point off the surface of the body, the components of the velocity are determined just as if the point of interest was a null point of a single element. The total velocity at the field point is the sum of the freestream velocity and the contributions of each of the elements of the body surface. The contribution of each of the elements is determined by calculating the influence coefficient based on the element geometry, and multiplying the result by the source density for the element. The total velocity at the field point may be expressed as

$$\mathbf{V}_{p} = \mathbf{V}_{\infty} + \sum_{q=1}^{N} C_{pq} \mathcal{O}_{q}$$
 (125)

where p and q represent the field point and the source element respectively and the influence coefficient,

$$C_{pq} = \iint \frac{\partial}{\partial n} \left[\frac{1}{r(p,q)} \right] dr$$
 (126)

As discussed in section 6.0, the influence coefficient may be calculated by the exact method, or it may be approximated by the quadrupole or monopole method depending on the ratio of the distance, r_0 , between the field point and the centroid of the source element to the maximum dimension, t, of the source element.



The magnitude of the velocity at either the on-body or off-body points is given by

$$|\mathbf{V}| = \sqrt{V_X^2 + V_y^2 + V_z^2} \tag{127}$$

The pressure coefficient is calculated by using the result of equation (127) in equation (19), renumbered here for clarity.

$$C_{p} = \frac{p - p_{\infty}}{\frac{1}{2} p |\mathbf{v}_{\infty}|^{2}} = 1 - \frac{|\mathbf{v}|^{2}}{|\mathbf{v}_{\infty}|^{2}}$$
(128)



11.0 STREAMLINE CALCULATIONS

For the calculation of streamlines off the surface of the body, a timestep procedure is performed by calculating the velocity at the starting point of the streamline from equation (125), and advancing the streamline one time increment by a fourth order Runge-Kutta integration to a new point (Ralston 1965). The timestep procedure is repeated, thus creating a streamline composed of finite segments.

For the calculation of streamlines on the surface of the body, the streamline is started at a specified point and quadrilateral number. The local velocity is calculated from equation (124), and the values of a stream function are computed for each corner point. The stream function is chosen so that it has a value of zero at the last point on the streamline in the quadrilateral. The side of the quadrilateral through which the streamline exits is determined, and coordinates of the point on the side which has a stream function value of zero are computed. The direction of the streamline is verified by comparing it with the known direction of positive velocity. The next quadrilateral through which the streamline passes is determined by calculating the proximity of the new quadrilateral to the most recent point on the streamline. A circular area is computed which encloses the new quadrilateral with an additional 10% margin. If the last point of the streamline falls outside the circle, then - the quadrilateral is discarded and a new one selected until the streamline is adjacent to the new quadrilateral.



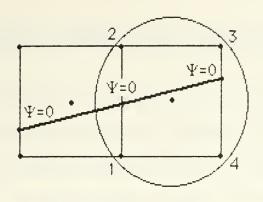


Figure 15. Calculation of on-body streamlines

This procedure is repeated along the surface of the body until all of the surface elements have been tested. The result is a streamline composed of segments from one side of an element to another.



12.0 DEVELOPMENT OF HIGHER ORDER PANEL METHODS

The XYZ Potential Flow program assumes a constant element source panel as described in Section 3.3. Extensive use of the constant element source panel method has shown that the primary diasadvantage of the method is that, in order to obtain a highly accurate solution, a large number of surface elements must be used to discretize the body surface. The method has been applied to problems of increasingly complex configurations (Hess 1977). By doing so, the size of the coefficient matrix is increased resulting in increased computer time and cost. Additional cost is accrued due to the manhours required to prepare the input. Therefore, while the constant element methods have proven to be very successful, the cost has motivated the development of higher order methods.

The higher order surface singularity methods discretize the body surface with curved elements having a variable source density, as compared to the flat elements of constant source strength used in the basic method. Hess (1973) showed that the effect of a curved surface and the effect of a variable source density are of the same order of magnitude. Therefore, the two effects must be used together to provide a "consistent" solution. The consistent higher order panel method provides the increased accuracy and speed desired for three dimensional Neumann problems (Hess 1979).

According to Hess (1979), the evolution of the higher order panel



method from the constant element method involved the derivation of new influence coefficients based on the integration of a variable source density over a curved element. Other portions of the method were unchanged. However, the development of the higher order velocity equations also required different programming logic.

In examining the potential for development of the higher order methods, Hess (1979) noted that "a consistent approach always uses a source polynomial one degree less than the panel polynomial." Through an independent effort, Brebbia (1984) presented a higher order approach using the direct method to solve for a surface potential polynomial stating that the potential function must be of a degree at least equal to the degree of the polynomial describing the element. Knowing that the velocity function is the derivative of the potential function, these two observations agree. As a result of his derivations, Hess showed that the solution of a flat element with a constant source requires one integral, a paraboloidal panel with a linearly varying source density requires six integrals, and a cubic element with a quadratic source density requires twenty-three integrals. Development of higher order methods has focused on the paraboloidal element with the linearly varying surface, as solutions of higher order than that offered little benefit for the amount of effort required to produce a working program (Hess 1979). Hess (1979) and Eriksson (1983) have independently developed programs for three dimensional higher order panel methods. The higher order Hess program evolved from the constant element program which he developed in the early 1960s, while Eriksson developed a new program based on the



work of Johnson and Rubbert (1975). Continued work in the near future is expected to deal primarily with refinement of the paraboloidal element with a linearly varying source (Eriksson 1983).

In order to alleviate the burden of preparing the input, a geometry package for input data generation has been developed which is incorporated into the Hess higher order panel program. This allows the user to enter relatively few points to describe the body. The geometry package enhances the surface representation by distributing additional points on the surface based on one of many algorithms or recurring geometries (Halsey 1978).

As the state of the art in fluid dynamics has progressed, the XYZ Potential Flow program has seen increasingly complex applications requiring a great deal of effort in preparing the input, and requiring long computer run times. Hess (1979) reported the use of the Hess constant element program for a configuration utilizing 7000 effective elements. Realizing that the computation time increases as the square of the number of elements, it is easy to see the motivation for developing the higher order panel methods. Though modern computers offer storage capacities which can handle most applications of the constant element method, the higher order panel methods can provide equal accuracy for much less user effort. While the constant element method is still a versatile tool, future generations of the surface singularity methods will be able to handle the more complex applications being demanded in fluid dynamics.



13.0 VELOCITY CALCULATIONS FOR A TRIAXIAL ELLIPSOID

As the only true body for which an analytical solution exists, a triaxial ellipsoid was selected for the sample calculations in order to compare calculated results with the analytical solution. Hess has made use of the triaxial ellipsoid throughout his works in developing both the constant element method and the higher order panel method. Therefore, the XYZPF program will be compared with existing results of the Hess method (Hess 1979).

The triaxial ellipsoid utilized for the calculations has semiaxes dimensions of 1, 2, and 0.5 in the x, y, and z directions respectively. The surface was discretized by selecting fixed intervals of 0.1 in the y direction, and fourteen equal divisions of the 90° sector in the x-z plane. The values of x and z were then solved in terms of y and an angle θ . This method yielded 280 elements in the first octant for a total of 2240 effective elements after employing symmetry. A FORTRAN program was used to generate the corner points and to prepare the input file for later use by the XYZPF program.

Figures (16) and (17) show excellent correlation with the analytical solution and little difference from the Hess solution using 4320 effective elements. The use of the centroid as the control point is an approximation used to simplify the multipole expansion of the potential about the origin of the local coordinate system. This approximation is valid for most elements. However, for elements which are long and thin,



the physical difference between the centroid location and the null point location is significant, and use of the centroid can produce significant error as may be observed in figure (16) when the value of y approaches 2.0.

Recent calculations on the same body (Hess 1979) showed that results of at least equal accuracy could be obtained using only 480 effective elements using the higher order panel method. These results are a significant demonstration of the value of the higher order panel method. Using the higher order panel method rather than the constant element method, the user has the option of obtaining equal accuracy with cruder discretization or higher accuracy for the same discretization effort. While the results of the triaxial ellipsoid show relatively little improvement in accuracy, the most significant advantages of the higher order panel method are evident for a body with concave regions (Hess 1977).



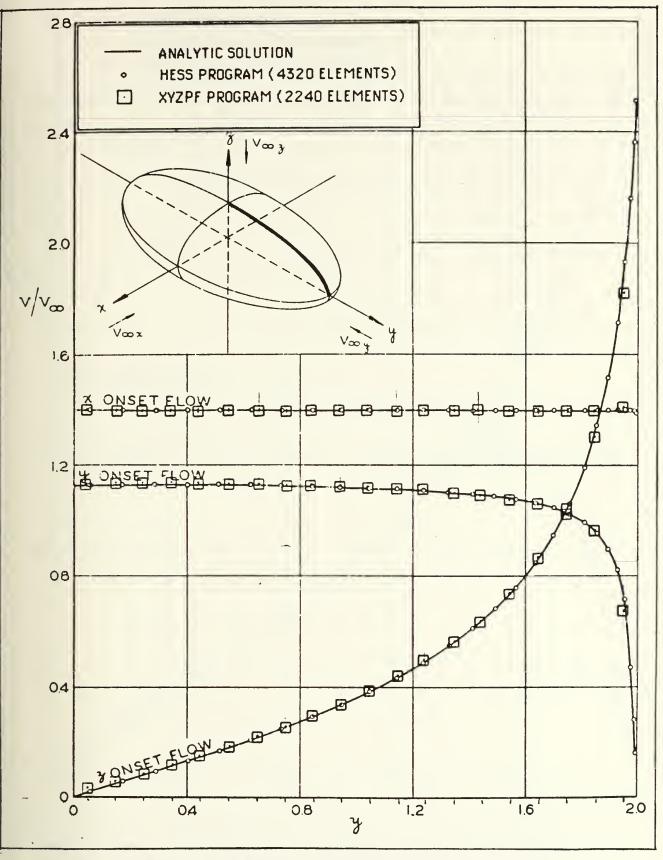


Figure 16. Comparison of analytic and calculated velocity distributions on an ellipsoid with axes ratios 1:2:0.5. Velocities in the xz-plane. (from Hess and Smith 1962)



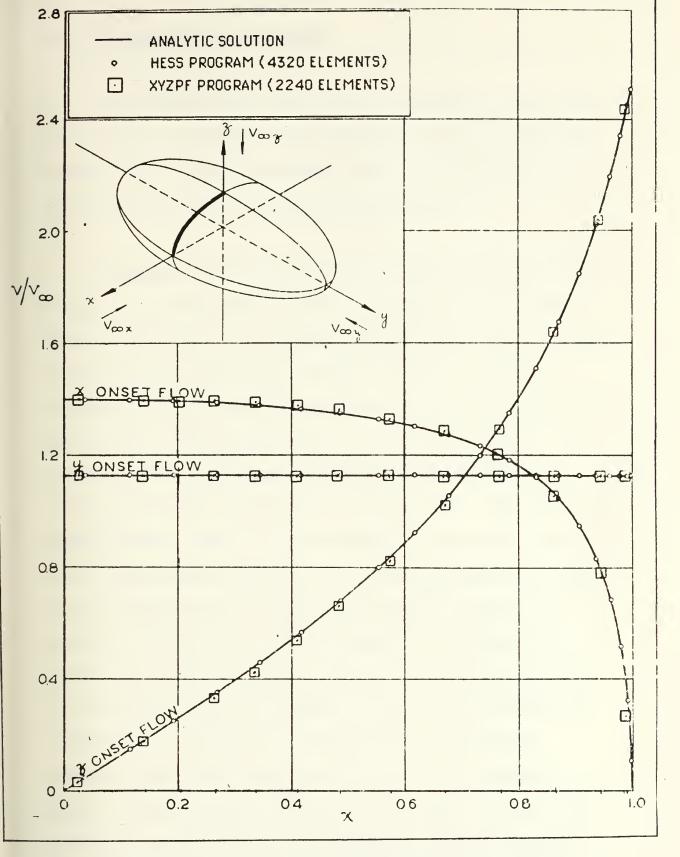


Figure 17. Comparison of analytic and calculated velocity distributions on an ellipsoid with axes ratios 1:2:0.5. Velocities in the yz-plane, (from Hess and Smith 1962)



14.0 CONCLUSION AND REMARKS

The objectives of this paper were (1) to describe the details of the approximation of an arbitrary three-dimensional body using quadrilateral elements, and (2) to provide a detailed derivation of the exact source panel integrations. Both of these objectives were met.

The method of surface discretization and source panel geometry is easily described using basic principles of geometry and vector algebra. By using quadrilateral surface elements, many surfaces can be discretized in a very straight forward logical fashion. The user can frequently visualize the contour lines of the surface which may be used to form the quadrilaterals, with some help from an intuitive approach to the fluid dynamics problem. The method of forming the planar quadrilateral element in the XYZPF Program differs slightly from the method presented by Hess and Smith (1962). The differences lie in the formation of the local coordinate system and the use of the centroid rather than the null point as the control point for applying the boundary conditions. The method of forming the local coordinate system has no effect on the potential flow calculations as long as one of the coordinate vectors is the outer normal to the planar element. The use of the centroid as the control point is an approximation used to simplify the multipole expansion of the potential about the origin of the local coordinate system. This approximation is valid for most elements. However, for elements which are long and thin, the physical difference between the centroid location and the null point location is significant, and use of the



centroid can produce significant error as may be observed in figure (16) when the value of y approaches 2.0.

A detailed derivation of the exact source panel integration has not previously appeared in literature, though the results are summarized by Hess and Smith (1962). The derivations presented in this paper verify the equations presented by Hess and Smith (1962), and the equations used in the XYZPF Program. The integral expressions for the velocity components were evaluated exactly with no assumptions or approximations used in the course of the integrations. Since the method of integration reduces the surface integral to a line integral around each of the sides of the element, the integration method can be generalized for a planar element with any number of sides, though the surface discretization used in the XYZPF Program uses only quadrilateral elements.

The calculation of potential flow about arbitrary three dimensional bodies is an engineering tool which is basic to design involving fluid dynamics. The XYZPF Program is a useful tool which has proven its value over the past 14 years. However, the increasing demands placed on this method are exposing the errors of the approximation as evident in the sample calculations presented in this paper. The requirement for increased accuracy has motivated the development of the higher order panel methods. Some of the limitations imposed on the XYZPF Program were due to computer memory and speed limitations. Advances in computer performance may allow future investigators to eliminate some



of the simplifying approximations used in the XYZPF Program, allowing increased accuracy without violating computer limitations. Some modifications might include the use of the null point as the control point rather than the panel centroid (as is used in the Hess program), or extending the range in which the exact velocity calculations are performed. The gains in accuracy by modifying the "constant element method" are limited by the basic approximations of the planar element and the constant source density for each element. Significant gains are most evident in the higher-order panel methods. This author concurs with Eriksson (1983) in expecting advances in the surface singularity methods to focus on the "development and refinement" of the higher order panel methods.



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APPENDIX I - XYZPF SECTION PF1

```
PROGRAM PFP1(INPUT=128.OUTPUT=128.TAPE5=INPUT,TAPE6=OUTPUT,TAPE03,
                  TAPE3=TAPE03, TAPE04, TAPE4=TAPE04, TAPE50=128)
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 4 SECTION 1
C
C
      READS INPUT AND COMPUTES QUADRILATERAL PARAMETERS
C
C
      FOR INFORMATION CONTACT
C
          BILL CHENG OR JANET DEAN
C
          NUMERICAL FLUID DYNAMICS BRANCH
                                              CODE 1843
C
          NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER
¢
          BETHESDA, MARYLAND
                                20084
      DIMENSION INDEX(9,3),6(9,6),F(9),CZ(9),IP(9),XP(9),YP(9),ZP(9)
                .MSK(100), WS(240),PROB(15),DM(650)
                X(800 ),Y(800 ),Z(800 ),ID(41,71),B(250),T(4600),KP(100)
      EQUIVALENCE (CZ(1),F(1))
      EQUIVALENCE(WS(1), KP(1)), (WS(101), MSK(1)), (WS(201), NP ), (WS(202),
     2 NSP), (WS(203), NEP), (WS(204), NSE), (WS(205), MIX), (WS(206), MIY).
     3 (WS(207),MTZ),(WS(209),TCVM),(WS(210),TSM),(WS(211),K),(WS(213),
     4 EPS),(WS(208),IPS ),(WS(212),IPF ),(WS(217),XI),(WS(218),YI),
     5(NS(219),ZI)
     EQUIVALENCE (Y12, Y23), (Y34, Y41)
      INTEGER P.P1,P2,P3,P4,PC,P5,P6,P7,P8
     WRITE (6,5)
   5 FORMAT(49H1XYZ POTENTIAL FLOW PROGRAM SECTION 1, VERSION 4 )
   10 FORMAT (11,15A4)
  20 FORMAT (1X, 1514)
  50 FORMAT (1X,217,6E12.5)
  30 FORMAT (1X,5F12.9)
       A. READ IN CONTROL PARAMETERS
     WS(220)=4.
     K1=0
      101=0
      102=0
      103=0
      104=0
      105=0
      106=0
      107=0
     MRXN=70
     MAXM=40
     MAXNOE=650
     MAXPC=800
     ICNTRL=1
     E0F50=0.
     READ (5 , 10)J, (PROB(1), I=1, 15)
     IF (EOF(5) .EQ. 0.) GO TO 9
     WRITE(6, 8)
  8 FORMAT(39HONO TITLE CARD FOUND - PROGRAM ABORTED )
     STOP
   9 CONTINUE
     ان=ل
     WRITE (6, 10) J. (PROB(1), I=1, 15)
     SB=0.
  21 FORMAT (17HONO. OF QUADS. = 14
                                         /17H NO. OF SECTIONS=.
    214/31H MAX. NO. OF ITERATIONS X FLOW , 13,9H Y FLOW ,
    313,9H Z FLOW ,13)
     READ (5 , 11)NOE, NSE, MIX, MIY, MIZ, ISM, EPS, LUCT, IPS, IPF, ISP
```



```
. LEDIT 1, LEDIT 3, LEDIT 4, LTAPE, XCENTER, VCENTER, ZCENTER
  11 FORMAT(614,F8.5,814,1X,3F5.3)
     IF (EOF(5) .EQ. O.) GO TO 19
     WRITE(6, 18)
  18 FORMAT(43HONO PARAMETER CARD FOUND - PROGRAM ABORTED
  19 CONTINUE
     IF (IEDIT1.EQ. 1) ICNTRL=0
     WRITE (6,21) NQE, NSE, MIX, MIY, MIZ
  31 FORMAT ("CONVERGENCE CRITERIA", F8.5)
  41 FORMAT (4H0 M,7X,2HX1,12X,2HX2,12X,2HX3,12X,2HX4,12X,2HXP,12X,
    1 2HXN, 12X, 1HB, 13X, 3HCZ4/4H N, 7X, 2HV1, 12X, 2HV2, 12X, 2HV3, 12X, 2HV4,
    2 12X, 2HVP, 12X, 2HVN, 12X, 2HFL, 12X, 3HCZ5/4H P, 7X, 2HZ1, 12X, 2HZ2, 12X,
    3 2HZ3, 12X, 2HZ4, 12X, 2HZP, 12X, 2HZN, 12X, 4HCZ1, 10X, 3HCZ6/>
  42 FORMAT (4H1 M,7X,2HX1,12X,2HX2,12X,2HX3,12X,2HX4,12X,2HXP,12X,
    1 2HXN, 12X, 1HR, 13X, 3HCZ4/4H N, 7X, 2HY1, 12X, 2HY2, 12X, 2HY3, 12X, 2HY4, 2 12X, 2HYP, 12X, 2HYN, 12X, 2HFL, 12X, 3HCZ5/4H P, 7X, 2HZ1, 12X, 2HZ2, 12X,
    3 2HZ3, 12X, 2HZ4, 12X, 2HZP, 12X, 2HZN, 12X, 4HCZ1 , 10X, 3HCZ6/>
  24 FORMAT (1H , L1, 19H PLANES OF SYMMETRY)
 240 WRITE (6,24) ISM
 270 WRITE (6,31) EPS
 280 IF (IPS.LE.O) GO TO 290
 285 WRITE (6,36) IPS, IPF
  36 FORMAT (45HONEN SOURCE DENSITY TO BE COMPUTED FOR QUADS.,14,3H - ,
    114)
 290 K=0
     WRITE(6,39)ISP
 39 FORMAT (9HO
                   -1SP = .13
     WRITE(6,37) (EDIT1, LEDIT3, LEDIT4, LTAPE
   FORMAT (9H0|ED|T1 =,|3/9H |ED|T3 =,|3/9H |ED|T4 =,|3/9H |TAPE =,
              13)
     WRITE(6,38) XCENTER, YCENTER, ZCENTER
  38 FORMAT(10HOXCENTER = ,F5.2/10H YCENTER =,F5.2/10H ZCENTER =,F5.2)
     MN=0
     P=1
     0 = 1.0
     DO 291 I=1,41
     DO 291 J=1,71
 291 ID(I,J)=0
     J=0
       ₽.
           READ FIRST PT.
     TERR=0
     IF (ITAPE.EQ.1) 60 TO 292
2000 READ (5,40) XI,YI,ZI,NI,MI,NS,NE,VN
     IF (EOF(5).NE.O. .OR. NS.LE.O.) GO TO 2050
     WRITE(6,45) ICHTRL,NS
  45 FORMAT(11,9H SECTION ,14)
     LINE=0
     GO TO 293
2050 IF(IERR.EQ.0) GO TO 2200
     WRITE(6,2100)
2100 FORMAT(39HONO POINT CARDS FOUND - PROGRAM ABORTED
     STOP
2200 IERR =1
     ITAPE=1
     WRITE(6,2300)
2300 FORMAT(47HOERROR IN INPUT - POINT CARDS NOT ON INPUT FILE
             53HPROGRAM WILL CHANGE ITAPE TO 1 AND TRY TO READ TAPE50 >
     IF ( EOF(5).EQ.0 ) WRITE(6,2400) XI,YI,ZI
2400 FORMAT(11H0EXTRA FLOW,3F12.5,5X,20HWILL NOT BE COMPUTED )
```

0



```
292 READ(50,40) XI,YI,ZI,NI,MI,NS,NE,UN
  40 FORMAT (3F12.9,414,F12.9)
     E0F50=E0F(50)
     IF (E0F50.NE.O. .OR. NS.LE.O) G0 T0 2450
     WRITE(6,45) ICHTRL,NS
     LINE=0
     GO TO 293
2450 IF (IERR.EQ.0) GO TO 2500
    WRITE(6,2100)
     STOP
2500 IERR=1
     ITAPE=0
    WRITE(6,2600)
2600 FORMAT("ERROR IN INPUT - POINT CARDS NOT ON TAPESO", 10X,
    1"PROGRAM WILL CHANGE ITAPE TO 0 AND TRY TO READ INPUT FILE")
    GO TO 2000
293 UNR=UN
    NSS=NS
    PC=1
     IF (NE .EQ.O) GO TO 2700
    IM=HIMM
    MM6X=M1
    HMIN=MI
    NM8X=MT
    GO TO 300
2700 MMTN=MT
    MMAX=MI
    HM1H=H1
    MMAX=N1
     GO TO 300
295 IF (ITAPE.EQ.1) GO TO 297
    READ (5,40) XI,YI,ZI,NI,MI,NS,ME,UN
     IF (E0F(5),EQ.O.) GO TO 299
    MS=0
    XI=0.
    Y1=0.
    ZI=0.
    60 TO 299
297 READ(50,40) XI,YI,ZI,NI,MI,NS,ME,UN
    E0F50=E0F(50)
     IF (E0F50 .NE.0) NS=0
299 PC=PC+1
     IF (NS.NE.NSS) GO TO 330
300 IF (NE.EQ.O) 60 TO 304
301 IN=NI
    NI=MI
    M1=1M
          STORE PT. IN PT. ARRAY
304 IF (MAXPC+1-PC) 295,305,310
305 WRITE(6,306) NS,MI,NI
306 FORMAT(60H ERROR IN INPUT - THERE ARE TOO MANY DATA POINTS IN SEC
    1TION , 14,30H - POINTS BEGINNING WITH M = , 14,5H N = , 14,
   2 17H WILL BE IGNORED >
    LINE=LINE+1
     104=104+1
    GO TO 295
310 X(PC)=X1
    Y(PC)=YI
    Z(PO)=ZI
    IF (MILLELMAXM LAND, NILLELMAXM) GO TO 315
    WRITE(6,311) MI,NI
```



```
LINE=LINE+1
  311 FORMAT(38H ERROR IN INPUT - INVALID M, N INDICES , 10X,
     1 14HPOINT WITH M = ,14,5H N = ,14,17H WILL BE IGNORED >
      105=105+1
     PC=PC=1
     60 TO 295
  315 ID(MI, NI)=PC
     CIM, XAMM) OXAM=XAMM
     CIM, HIMM) ON IM=HIMM
     MMAX=MAXO(MMAX, NI)
     CIM, MIMMOONEM=MIMM
     GO TO 295
  330 IF (IEDIT1.EQ.1) GO TO 294
     IF (LINE.LT.40) 60 TO 333
     WRITE(6,42)
     LIME=0
     GO TO 294
  333 WRITE(6,41)
  294 CONTINUE
C
       E. DO LOOPS TO SWEEP PT. ARRAY
     MIMM=PM
     MM2=MMAX-MMIN
     NN2=NMAX-NMTN
     WRITE(6,331) NSS,MMIN,MMAX,NMIN,NMAX
     LIME=LIME+1
  331 FORMAT(16HOERROR - SECTION .15.45H DOES NOT HAVE QUADS ARRANGED IN
     1 BLOCKS OF 4 ,9H MMIN= ,12,6H MMAX= ,12,6H NMIN= ,12 ,
    26H NMAX= ,12)
     106=106+1
 332 MM2=MM2/2
     NM2=NM2/2
     DO 404 NN=1,NN2
     M1=MMIN
     DO 402 MM=1, MM2
     NO= 1
0
      F. HAVE 9 CORNER PTS. BEEN GIVEN
     TT=ID(M1,N1)*ID(M1+1,N1)*ID(M1+2,N1)*ID(M1,N1+1)*ID(M1+1,N1+1)*
     1 ID(M1+1, M1+2)*ID(M1, M1+2)*ID(M1+1, M1+2)*ID(M1+2, M1+2)
     IF( IT.EQ.O ) GO TO 402
     IERR=0
     M2=M1+1
     N2=N1+1 = M1, M2
     DO 400 N=N1,N2
     GO TO (334,335,336,337) NO
 334 P1=1D(M ,N )
     P2=1D(M+1,N )
     P3=10(M+1,N+1)
     P4=10(M ,N+1)
     P5=1D(M±2,N )
     P6=10(M+2, N+1)
     P7=10(M+1,N+2)
     P8=1D(M ,N+2)
     P9=P1
     (X(P1).NE.X(P4).OR.Y(P1).NE.Y(P4).OR.Z(P1).NE.Z(P4))) GO TO 340
       P9=1D(M+2, N+2)
     60 TO 340
 335 P1=ID(M ,N+1)
     P2=1D(M ,N )
     P3=1D(M+1,N )
```



```
P4=10(M+1,N+1)
      P5=1D(M ,N-1)
      P6=1D(M+1,N-1)
      P7=1D(M+2,N )
      P8=1D(M+2,N+1)
     P9=P1
      (F((X(P1),NE,X(P2),OR,Y(P1),NE,Y(P2),OR,Z(P1),NE,Z(P2)) .AND.
        (X(P1).NE.X(P4).OR.Y(P1).NE.Y(P4).OR.Z(P1).NE.Z(P4))) GO TO 340
       P9=1D(M+2,N-1)
     GO TO 340
  336 P1=1D(M+1,N )
      P2=1D(M+1,N+1)
     P3=ID(M ,N+1)
P4=ID(M ,N )
     P5=10(M+1,N+2)
     P6=1D(M ,N+2)
     P7=1D(M-1,N+1)
     P8=1D(M-1,N )
     P9=P1
     IF((X(P1).NE.X(P2).OR.Y(P1).NE.Y(P2).OR.Z(P1).NE.Z(P2)) ...AND
        (X(P1).NE,X(P4).OR,Y(P1).NE,Y(P4).OR,Z(P1).NE,Z(P4))) G0 T0 340
       P9=10(M-1,N+2)
     GO TO 340
  337 P1=ID(M+1,N+1)
     P2=1D(M ,N+1)
     P3=1D(M ,N )
     P4=10(M+1,N
     P5=10(M-1,N+1)
     P6=10(M-1,N )
     P7=ID(M ,N-1)
     P8=1D(M+1,N-1)
     P9=P1
     (X(P1).NE,X(P4).OR,Y(P1).NE,Y(P4).OR,Z(P1).NE,Z(P4))) G0 T0 340
       P9=10(M-1, N-1)
  340 IP(1)=P1
      IP(2)=P2
      IP(3)=P3
      IP(4)=P4
      IP(5)=P5
      IP(6)=P6
      1P(7)=P7
      IP(8)=P8
      IP(9)=P9
Ū
       G2 COMPUTE NORMAL VECTOR (XM, YM, ZM)
     X1=X(P3)-X(P1)
     X2=X(P4)-X(P2)
     Y1=Y(P3)-Y(P1)
     Y2=Y(P4)-Y(P2)
     Z1=Z(P3)-Z(P1)
     Z2=Z(P4)-Z(P2)
     XN=Y2*Z1-Y1*Z2
     YH=X1*Z2-X2*Z1
     ZN=X2*Y1-X1*Y2
     R=SQ2(XN, YN, ZN)
      IF (R.GT. .00000000001) GO TO 345
     WRITE(6,343)
  343 FORMAT(33H ERROR IN INPUT - ZERO AREA QUAD )
     LIME=LIME+1
      101=101+1
      RQ=0.
```



```
XC=0.
      Y0=0.
      20=0.
      FL=0.
      0Z(1)=0.
      CZ(4)=0.
      0Z(5)=0.
      CZ(6)=0.
      IERR=1
      60 TO 351
  345 CONTINUE
      XN=XN/R
      YN=YN/B
      ZN=ZN/R
      80=.5*B
        COMPUTE CENTROID
C
      X1=X(P3)-X(P2)
      Y1=Y(P3)-Y(P2)
      Z1=Z(P3)-Z(P2)
      X5=Y1*Z2-Y2*Z1
      Y5=Z1*X2-Z2*X1
      Z5=X1*Y2-X2*Y1
      A1=S02(X5, Y5, Z5)
      82=8-81
      1T=1
      XC=(X(P2)+X(P4)+(R1*X(P3)+R2*X(P1))/R)/3.
      YC=(Y(P2)+Y(P4)+(B1*Y(P3)+82*Y(P1))/B)/3.
      ZC=(Z(P2)+Z(P4)+(A1*Z(P3)+B2*Z(P1))/B)/3.
        COMPUTE SECOND AND THIRD VECTORS
  945 X4=YN*Z1-Y1*ZN
      Y4=ZN*X 1-Z 1*XN
      Z4=XN*91-X1*9N
      R=1./SQ2(X4,Y4,Z4)
      X4=X4*8
      V4=V4*A
      Z4=Z4*A
      X3=ZN*Y4-Z4*YN
      Y3=XN*Z4-X4*ZN
      Z3=YN*X4-Y4*XN
C.
        COMPUTE POINTS IN QUAD SYSTEM
      00 947 1=1,9
      L=IP(1)
      XP(T)=X3*(X(L)-X0)+Y3*(Y(L)-Y0)+Z3*(Z(L)-Z0)
      YP(1)=X4*(X(L)-XC)+Y4*(Y(L)-YC)+Z4*(Z(L)-ZC)
  947 ZP(1)=XN*(X(L)-XC)+YN*(Y(L)-YC)+ZN*(Z(L)-ZC)
0
        COMPUTE MATRIX COEF. TO FIND SURFACE EQ.
      DO 949 1=2,9
      G(1,1)=1.
      G(1,2)=XP(1)
      G(1,3)=YP(1)
      G(1,4)=XP(1)**2
      G(1,5)=YP(1)**2
      8(1,6)=YP(1)*XP(1)
  949 F(1)=ZP(1)
      DO 953 1=1,6
      G(1,1)=G(9,1)
      6(5,1)=6(5,1)+6(6,1)
  953 6(6,1)=6(7,1)+6(8,1)
      F(1)=F(9)
      F(5)=F(5)+F(6)
      F(6)=F(7)+F(8)
```



```
C
        SOLUE MATRIX EQ. G*CZ=F FOR CZ
      CALL MATINS(6,9,6,F,6,1,DETERM, IDM, INDEX)
                         GO TO (955,960) IT
      IF (IDM.EQ. 1)
      TERR=1
      WRITE(6,954)
  954 FORMAT (33H ERROR IN INPUT - SINGULAR MATRIX )
      LINE=LINE+1
      1D2=1D2+1
      GO TO 960
  955 IT=2
C
        FIND NEW NORMAL VECTOR
      XN=XN-CZ(2)*X3-CZ(3)*X4
      YN=YN-CZ(2)*Y3-CZ(3)*Y4
      ZN=ZN-CZ(2)*Z3-CZ(3)*Z4
      A=1.7SQ2(XN,YN,ZN)
      XN=XN*A
      AN=AN*U
      ZN=ZN*A
      60 TO 945
C
        STORE DATA
  960 B(J±1)=XP(1)
      B(J+2)=YP(1)
      B(J+3)=XP(2)
      B(J+4)=VP(2)
      B(J+5)=XP(3)
      B(J+6)=XP(4)
      B(J+7)=YP(4)
      B(J+8)=X3
      B(J+9)=Y3
      B(J+10)=23
      B(J+11)=X4
      B(J+12)=Y4
      B(J+13)=Z4
      B(J+14)=CZ(1)
      B(J+15)=CZ(4)
      B(J+16)=CZ(5)
      B(J+17)=CZ(6)
      IF (K .LT. 7*MAXNQE) 60 TO 965
      107=107+1
      K1=K+K1
      K=0
  965 CONTINUE
      T(K+1)=X0
      T(K+2)=Y0
      T(K+3)=Z0
      T(K+4)=XN
      T(K+5)=YN
      T(K+6)=ZN
      T(K+7)=80
0
        COMPUTE QUADRUPOLE MOMENTS
      X11=XP(1)+XP(2)
      X12=XP(1)+XP(4)
      X13=XP(3)+XP(2)
      X14=XP(3)+XP(4)
      X15=XP(2)+XP(4)
      Y11=YP(1)+YP(2)
      Y12=YP(1)+YP(4)
      Y13=YP(3)+YP(2)
      Y14=YP(3)+YP(4)
      Y15=YP(2)+YP(4)
      R1=81/24.
```



```
R2=R2/24.
      R3=80/12.
      BXX=(X11**2+X12**2)*B1+(X13**2+X14**2)*B2+X15**2*B3
      AXV=(X|1*V|1+X12*V|2)*R1+(X|3*V|3+X|4*V|4)*R2+X|5*V|5*R3
      RYY=(Y11**2+Y12**2)*R1+(Y13**2+Y14**2)*R2+Y15**2*R3
C
        COMPUTE SOLID ANGLE
      XX=XC-XCENTER
      YY=YC-YCENTER
      ZZ=ZC-ZCENTER
      X1=XX*X3+YY*Y3+ZZ*Z3
      Y1=XX*X4+YY*Y4+ZZ*Z4
      Z1=XX*XN+YY*YN+ZZ*ZN
      RD=1./SQ2(X1,Y1,Z1)
      RCU=RD**3
      RSV=RCU**2*RD
      SA=SA+Z1*(A0*RCU+((AXX*(Y1**2+Z1**2+4.*X1**2)
            +8YY*(X1**2+Z1**2-4.*Y1**2))*1.5-15.*X1*Y1*8XY)*8SU)
      B(J+18)=AXX
      B(J+19)=AXY
     B(J+20)=844
       ERROR TESTS
      D1=SQ2((XP(3)-XP(1)),(YP(3)-YP(1)),0.)
     D2=SQ2((XP(4)-XP(2)),(YP(4)-YP(2)),0.)
      FL=.5*AMAX1(D1.D2)
      CZ23=ABS( CZ(2) ) + ABS( CZ(3) )
      IF( ABS(CZ(2))+ABS(CZ(3)) .GT. FL*.001 ) GO TO 970
      IF ( ABS( CZ(1)) .LT. FL*.3 ) 60 TO 977
 970 WRITE(6,975) CZ23
 975 FORMAT(29H QUESTIONABLE POINT -POOR FIT ,6E14.3)
      TERR=1
     LINE=LINE+1
 977 IF (YP(1)*XP(2)-YP(2)*XP(1) .GE. 0. .AND.
         YP(2)*XP(3)-YP(3)*XP(2) .GE. O. .AND.
         YP(3)*XP(4)-YP(4)*XP(3) .GE. 0. .AND.
         YP(4)*XP(1)-YP(1)*XP(4) .GE. 0.)
 980 WRITE(6,1000) ( XP(1), YP(1), 1=1,4)
 1000 FORMAT(41H ERROR IN INPUT - CROSSED OR CONCAVE QUAD
             4(2F10.5,3X)
     1
      IERR=1
     LINE=LINE+1
      ID3=ID3+1
 984 CRCF=SQ2((XP(2)-XP(1)),(YP(2)-YP(1)),0)+XP(3)-XP(2)+ SQ2((XP(1)-
          XP(4), (YP(1)-YP(4)), 0. )+SQ2((XP(4)-XP(3)), (YP(4)-YP(3)), 0. )
     1F ( 36.*AQ .GT. CRCF**2 ) GD TO 986
     LINE=LINE+1
     WRITE(6,961)
 961 FORMAT (24H WARNING LONG THIN QUAD.)
 986 IF ( Z1 .GE. 0. ) G0 TO 351
 350 WRITE (6,85)
  85 FORMAT (35H QUESTIONABLE POINT - INWARD NORMAL)
     IERR=1
     LINE=LINE+1
       J. EDITE QUAD INFORMATION
 351 IF (IEDIT1.EQ.2.AND. IERR.EQ.0) GO TO 354
      IF ( IEDIT1 .EQ. 1 ) GO TO 354
     GO TO (355,357,358,359) NO
 356 WRITE(6,51) M,X(P1),X(P2),X(P3),X(P4),XC,XN,AQ
                                                        ,CZ(4)
                                                        ,CZ(5)
    1
                  N,Y(P1),Y(P2),Y(P3),Y(P4),Y0,YN,FL
     2
                   P,Z(P1),Z(P2),Z(P3),Z(P4),Z0,ZN,CZ(1),CZ(6)
     GO TO 360
 357 WRITE(6,51) M,X(P2),X(P3),X(P4),X(P1),XC,XN,AQ
                                                        ,CZ(4)
```



```
,CZ(5)
   1
                  N, Y(P2), Y(P3), Y(P4), Y(P1), Y0, YN, FL
   2
                  P,Z(P2),Z(P3),Z(P4),Z(P1),ZC,ZN,CZ(1),CZ(6)
    GO TO 360
                                                         ,CZ(4)
358 WRITE(6,51)
                 M,X(P4),X(P1),X(P2),X(P3),XC,XN,AQ
                  N, Y(P4), Y(P1), Y(P2), Y(P3), Y0, YN, FL
                                                         ,CZ(5)
   2
                  P,Z(P4),Z(P1),Z(P2),Z(P3),ZC,ZN,CZ(1),CZ(6)
    GO TO 360
359 WRITE(6,51)
                 M,X(P3),X(P4),X(P1),X(P2),XC,XN,AQ
                                                         ,CZ(4)
                 N, Y(P3), Y(P4), Y(P1), Y(P2), Y0, YN, FL
                                                         ,CZ(5)
   1
   2
                 P,Z(P3),Z(P4),Z(P1),Z(P2),ZC,ZN,CZ(1),CZ(6)
360 CONTINUE
 51 FORMAT (1H ,13,8E14.5/1X,13,8E14.5/1X,13,8E14.5/)
    LINE=LINE+4
    IF (LINE.LT.50) GO TO 354
352 WRITE (6,42)
    LINE=0
354 CONTINUE
    J=J+20
    I = F
    DM(1)=UNR
    P=P+1
    N0=N0+1
    IERR=0
349 K=K+7
      K. WRITE OUT BLOCK OF B ARRAY IF FULL
    IF (J.LT.240) GO TO 400
355 WRITE (04) 0,(B(1),1=1,240)
    0=6
    0=0
      L.
         END OF DO LOOP OVER PT. ARRAY
400 CONTINUE
402 M1=M1+2
404 N1=N1+2
      M. SET FOR NEXT SECTION
    NSS=MS
    DO 405 M=MMIN, MMAX
    DO 405 M=MMIN, MMAX
405 ID(M, N)=0
    PC= 1
    IF (ME .EQ.0) GO TO 410
    MMAX=N1
    MMIN=HI
    NMIN=MI
    NMRX=MT
    GO TO 420
410 MMAX=M1
    MMIN=MI
    NM1N=N1
    NM8X=N1
420 NE=ME
    UMR=UN
    IF (NS.LE.0) GO TO 500
    WRITE(6,45) ICHTRL,NS
    LIME=0
    GO TO 300
500 WRITE (04) Q,(B(1), I=1,240)
550 NP=(K+K1)/7
    ISMP = ISM + 1
    GO TO (595,590,580,570),18MP
570 SR=SA+SA
580 SA=SA+SA
```



```
590 SR=SR+SR
      O1 WRITE PARAMETERS AND T ARRAY ON TAPE
  595 J = 1
      IF (ITAPE.EQ.1 .AND. E0F50 .NE.0 ) G0 T0 601
  597 \text{ WS(J)} = X1
     WS(J+20) = YI
     WS(J+40) = ZI
      J = J + 1
      IF(X1**2 + Y1**2 + Z1**2) 599,599,598
  598 WRITE(6,600) XI,YI,ZI
 600 FORMAT(11HOEXTRA FLOW, 10X, 3F12.5)
 601 READ(5,40) X1,Y1,Z1
      IF (EOF(5) .EQ. 0) GO TO 597
     X1=0.
     YI=0.
     ZI=0.
     GO TO 597
  599 IF (ISP.LT.0) GO TO 605
     WRITE (03) (PROB(1), 1=1, 15)
     WRITE (03) (WS(1),1=1,220),1EDIT3,1EDIT4
     WRITE (03) (T(1), I=1,K)
      WRITE (03) (DM(L), L=1,NP)
  605 CONTINUE
       N1 CHECK SOLID ANGLE
C
  610 WRITE (6,80) SA
  80 FORMAT(14HOSOLID ANGLE = .F8.3)
  620 REWIND 04
     REWIND 03
  622 | 103=101+102+103+104+105+106+107
      IF (IDS.EQ.O .AND. NP.EQ.NQE) GO TO 638
     WRITE(6,625)
      IF (ID1 .GT.0) WRITE(6,628) ID1
      IF (ID2 .GT.O) WRITE(6,629)
      IF (ID3 .GT.0) WRITE(6,630) ID3
      IF (104 .GT. 0) WRITE(6,631)
                                    104
      IF (ID5 .GT. 0) WRITE(6,632)
      IF (106 .GT. 0) WRITE(6,633) 106
      IF (107 .GT. 0) WRITE(6,634) NP, MAXNOE
      IF (NP.NE.NQE) WRITE(6,637) NP,NQE
      STOP
  625 FORMAT(38HOFATAL ERROR IN DATA - PROGRAM ABORTED)
  628 FORMATKIHO, 15,31H QUADRILATERALS WITH ZERO AREA
  629 FORMAT(1H0,15,44H QUADRILATERALS GENERATE A SINGULAR MATRIX
  630 FORMAT(1H0,15,26H CROSSED QUADRILATERALS
  631 FORMAT(1H0,15,32H SECTIONS HAVE TOO MANY POINTS
  632 FORMAT(1H0,15,34H POINTS HAVE INVALID M.N INDICES
  633 FORMAT(1H0,15,52H | SECTIONS DO NOT HAVE QUADS ARRANGED IN GROUPS O
     1F 4
  634 FORMATKIHO,15,48H QUADRILATERALS GIVEN, EXCEEDING THE LIMIT OF ,
     1 (4)
  637 FORMAT(1H0,15,28H QUADRILATERALS GIVEN, NOT ,14)
  638 IF (ISP.LE.O) GO TO 640
      WRITE(6,639) ISP
  639 FORMAT(7HO ISP= ,14,19H - PROGRAM ABORTED
      STOP
  640 CONTINUE
        02 READ PERS2 AND TRANSFER TO IT
      STOP 1
      END
C
      FUNCTION SQ2(X,Y,Z)
```



```
COMPUTE SQUAR ROOT OF R**2
      R= ABS(X)+ABS(Y) +ABS(Z) +.00000000000001
  700 RS=X**2+Y**2 +Z**2
      R=R+RS/R
      R=.25*R+RS/R
      R=R+RS/R
      S02= . 25*R+RS/R
      RETURN
      END
C
      SUBROUTINE MATINS(A,NR,N1,B,NC,M1,DETERM,ID,INDEX)
C
         MATRIX INVERSION WITH ACCOMPANYING SOLUTION OF SIMUL. EQ.
C
      PINOT METHOD
C
      FORTRAN IV SINGLE PRECISION WITH ADJUSTABLE DIMENSION
Ċ
      MOVEMBER 1971 S GOOD NAVAL SHIP R & D CENTER
C
      WHERE CALLING PROGRAM MUST INCLUDE
C
                   DIMENSION A(NR,NR), B(NR,NC), INDEX(NR,3)
C
                   WHERE NA,NO ARE DIMENSIONS OF A,B, INDEX
Ċ
                   N1 IS THE ORDER OF A
0
                   M1 IS THE NUMBER OF COLUMN VECTORS IN B (MAY BE 0)
                   DETERM WILL CONTAIN DETERMINANT ON EXIT
0
                   ID WILL BE SET BY ROUTINE TO 2 IF MATRIX A IS
                             1 IF INVERSION WAS SUCCESSFUL
                   SINGULAR.
0
                   MATRIX A (INPUT MATRIX) WILL BE REPLACED BY A INV
                   MATRIX B: THE COLUMN VECTORS WILL BE REPLACED
C
                              BY CORRESPONDING SOLUTION VECTORS
C
                   INDEX: WORKING STORAGE ARRAY
C
      IF IT IS DESIRED TO SCALE, THE DETERMINANT CARD 29 MAY BE
C
      DELETED AND DETERM PRESET BEFORE ENTERING THE ROUTINE
0
      DIMENSION A(NR,NR), B(NR,NC),
                                        INDEX(NR.3)
      EQUIVALENCE (IRON, JRON), (ICOLUM, JCOLUM), (AMAX, T, SWAP)
C
0
      INITIALIZATION
0
      H=H1
      11=111
      DETERM= 1.0
      DO 20 J=1,N
C
   20 INDEX(J.3)=0
      DO 550 I=1.N
C
0
      SEARCH FOR PIVOT ELEMENT
C.
      AMAX = 0.0
      DO 105 J=1,N
      IF(INDEX(J,3)-1) 60, 105, 60
   60 DO 100 K=1,N
      IF(INDEX(K,3)-1) 80, 100, 715
               AMAX -ABS (A(J,K))) 85, 100, 100
   80 IF (
   85 IROW = J
      100LUM = K
      AMAX = ABS(A(J,K))
  100 CONTINUE
  105 CONTINUE
      INDEX(ICOLUM,3) = INDEX(ICOLUM,3) + 1
      INDEX(1,1) = IROW
      INDEX(1,2) = ICOLUM
C
      INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL
```



```
C
      IF (IROW-ICOLUM) 140, 310, 140
  140 DETERM= -DETERM
      DO 200 L=1,N
      SWAP= A(IROW,L)
      A(TROW,L)=A(TCOLUM,L)
  200 ACTCOLUM, LD=SWAP
      IF(M) 310, 310, 210
  210 DO 250 L=1,M
      SWAP=B(IROW,L)
      B(TROW,L)=B(TCOLUM,L)
  250 B(ICOLUM, L)=SWAP
C
C
      DIVIDE PIVOT ROW BY PIVOT ELEMENT
C
  310 PIVOT = A(ICOLUM, ICOLUM)
      DETERM=DETERM*PIUOT
  330 \text{ A(ICOLUM, ICOLUM)} = 1.0
      DO 350 L=1,N
  350 ACTOBLUM, LD=ACTOBLUM, LD/PTVOT
      IF (M) 380, 380, 360
  360 DO 370 L=1.M
  370 B(ICOLUM, L)=B(ICOLUM, L)/PIVOT
C
C
      REDUCE NON-PIVOT ROWS
0
  380 DO 550 L1=1,N
      IF(L1-100LUM) 400, 550, 400
  400 T=A(L1, ICOLUM)
      A(L1, (COLUM)=0.0
      DO 450 L=1,N
  450 A(L1,L)=A(L1,L)-A(100LUM,L)*T
      IF (M) 550, 550, 460
  460 DO 500 L=1,M
  500 B(L1,L)=B(L1,L)-B(ICOLUM,L)*T
  550 CONTINUE
C
0
      INTERCHANGE COLUMNS
C
      DO 710 I=1,N
      L=14+1-1
      IF (INDEX(L,1)-INDEX(L,2)) 630, 710, 630
  630 JROW= INDEX(L, 1)
      JCOLUM=INDEX(L,2)
      DO 705 K=1,N
      SNAP = A(K, JROM)
      A(K, JROW)=A(K, JCOLUM)
      A(K, JCOLUM)=SMAP
  705 CONTINUE
  710 CONTINUE
      DO 730 K=1,N
      IF(INDEX(K,3)-1) 715, 720, 715
  720 CONTINUE
  730 CONTINUE
      10=1
  810 RETURN
  715 10=2
      GO TO 810
      END
```



APPENDIX II - XYZPF SECTION PF2

```
PROGRAM PF2(OUTPUT=128, TAPE6=OUTPUT, TAPE03, TAPE02, TAPE08,
                    TAPEO9, TAPEO1, TAPE11, TAPE04, TAPE4=TAPE04.
     1
     3
                    TAPE 1=TAPEO 1.
                    TAPES=TAPEOS, TAPE2=TAPEO2, TAPE8=TAPEO8, TAPE9=TAPEO9)
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 4 SECTION 2
C
C
      COMPUTES MATRIX COEFFICIENTS
                 B(241),T(4500),V1(1000),V2(1000),V3(1000),C1( 900),C2( 9
      COMMON
     200),03( 900),
                             WS(300),PROB(15),
     30X(8), 0Y(8), 0Z(8)
      EQUIVALENCE (Y3, Y2)
                                ,(WS(201),NP),(WS(210),SYM),(WS(211),KM)
           ,(WS(212),(PF)
                            ,(WS(208),IPS),(KM,MK)
      INTEGER SYM
      BLK=1.0
      1DM=0
      READ(03)
                   (PROB(1), I=1, 15)
      WRITE(6,5)
    5 FORMAT(49HOXYZ POTENTIAL FLOW PROGRAM SECTION 2, VERSION 4 ->
   90 FORMAT(1H0, 15A4)
      WRITE (6 ,90)
                               (PROB(1), 1=1, 15)
C
        A. READ PARAMETERS, I ARRAY, FIRST BLOCK OF B ARRAY
      READ(03)
                  (WS(1), I=1, 220)
      READ(03)
                   (T(1), 1=1, MK)
                 (B(1), I=1, 241)
      READ(04)
        B. START LOOP OVER OURDRALATERALS
C
      K=1
      J = 1
      P=1
      JC = 1
      JU=2
      MPH=5*((MP+4)/5)
      KMM=74NPN±1
  290 IF(B(1)-P)595,295,595
   98 FORMAT("POINTS OUT OF ORDER B(1)=".1F4.0." P=".1F4.0)
  295 J=2
  296 X1=B(J)
      Y1=B(J+1)
      X2=B(J+2)
      Y2=B(J+3)
      X3=B(J+4)
C
      V3=V2
      X4=B(J+5)
      Y4=B(J+6)
      XN=T(K+3)
      YN=T(K+4)
      ZN=T(K+5)
      XC=T(K)
      YC=T(K+1)
      ZC=T(K+2)
      A=T(K+6)
      XX=B(J+7)
      YX=B(J+8)
      ZX=B(J+9)
      XY=B(J+10)
      YY=B(J+11)
      ZY=B(J+12)
C
        C1 COMPUTE LENGTH OF SIDES OF OURD
      D12=SQ2F(X1,X2,Y1,Y2,0.,0.)
      D23=SQ2F(X2,X3,Y2,Y3,.0,.0)
```



```
D34=SQ2F(X3,X4,Y3,Y4,.0,.0)
      D41=SQ2F(X4,X1,Y4,Y1,.0,.0)
        C2 COMPUTE SLOPE OF SIDES
C
      IF(X2-X3)305,300,305
  300 0123=1.
      60 TO 310
  305 CM23=(Y2-Y3)/(X2-X3)
      C123=0.
  310 IF(X3-X4)315,311,315
  311 Cl34=1.
      GO TO 320
  315 CM34=(Y4-Y3)/(X4-X3)
      C134=0.
  320 IF(X4-X1)325,321,325
  321 CI41=1.
      GO TO 330
  325 CM41=(Y1-Y4)/(X1-X4)
      0141=0.
  330 IF(X1-X2)335,331,335
  331 0112=1.
      GO TO 340
  335 CM12=(Y2-Y1)/(X2-X1)
      CI 12=0.
        C3 COMPUTE QUADRAPOLE MOMENTS
C
  340 CTXX=B(J+17)
      C1XY=B(J+18)
      CTYY=B(J+19)
      CV12=0.8
      CX 12=0.0
      CY23=0.0
      CX23=0.0
      CY34=0.0
      CX34=0.0
      CY41=0.0
      CX41=0.0
        C4 COMPUTE SIN AND COS OF SLOPE ANGLE FOR EACH SIDE
Ç.
      IF (D12) 9341,9342,9341
 9341 CY12=(Y2-Y1)/D12
      CX 12=(X1-X2)/D12
 9342 1F(D23)9343,9344,9343
 9343 CY23=(Y3-Y2)/D23
      CX23=(X2-X3)/D23
 9344 IF(D34)9345,9346,9345
 9345 CY34=(Y4-Y3)/D34
      CX34=(X3-X4)/D34
 9346 IF(D41)9347,9348,9347
 9347 CY41=(Y1-Y4)/D41
      CX41=(X4-X1)/D41
C
        C5 COMPUTE MAX LENGTH OF QUAD
 9348 ST=ABS(X1-X3)
      ST2=SQ2F(X2,X4,Y2,Y4,.0,.0)
      ST=AMAX1(ST,ST2,D12,D23,D34,D41)
        Ð.
            START LOOP OVER NULL PTS.
  342 KQ=1
      L=1
  343 I=KQ
      IF(IPS) 9360,9360,9350
 9350 | F(L-1PS) | 9355,9352,9352
 9352 IF(L-IPF) 9360,9360,9355
 9355 C1(UC)=.0
      02(J0)=.0
      03(J0) = .0
```



```
G0 T0 541
 9360 IS=1
      XC0=T(1)
      YC0=T(1+1)
      Z00=T(1+2)
      XNQ=T(1+3)
      YN0=T(1+4)
  344 ZNQ=T(1+5)
C
           COMPUTE DISTANCE BETWEEN QUAD AND NULL PT.
0
            DETERMIN METHOD
  IF(RPQ-ST*4)350,350,460
  350 X=(XCQ-XC)*XX+(YCQ-YC)*YX+(ZCQ-ZC)*ZX
     Y=(X00-X0)*XY+(Y00-Y0)*YY+(Z00-Z0)*ZY
      Z=(XC0-XC)*XN+(YC0-YC)*YN+(ZC0-ZC)*ZN
      IF(RPQ-ST*2.0)355,355,400
C
           COMPUTE VELOCITY COEF. BY EXACT METHOD
  355 R1=SQ2F(X,X1,Y,Y1,Z,0.)
     R2=SQ2F(X,X2,Y,Y2,Z,0.)
      R3=SQ2F(X,X3,Y,Y3,Z,O.)
      B4=802F(X,X4,Y,Y4,Z,0.)
      IF ((R1+R2) .LE. D12)
                            GO TO 1000
      IF ((R2+R3) .LE. D23) G0 T0 1000
      IF ((R3+R4) .LE. D34) G0 T0 1000
      IF ((R4+R1) .LE. D41) GO TO 1000
      CLA1=ALOG((R1+R2-D12)/(R1+R2+D12))
      CLA2=ALOG((R2+R3-D23)/(R2+R3+D23))
      CLA3=RLOG((R3+R4-D34)/(R3+R4+D34))
      CLR4=RL0G((R4+R1-D41)/(R4+R1+D41))
      TVX=CY12*CLA1+CY23*CLA2+CY34*CLA3+CY41*CLA4
      TUY=0X12*CLA1+0X23*CLA2+0X34*CLA3+0X41*CLA4
      TVZ=0.
      IF(ABS(Z/ST)-.010) 375,361,361
  361 ZS0=Z**2
      E1=ZSQ+(X-X1)**2
      E2=Z80+(X-X2)**2
      E3=ZSQ+(X-X3)**2
      E4=ZSQ+(X-X4)**2
      H1=(Y-Y1)*(X-X1)
     H2=(Y-Y2)*(X-X2)
     H3=(Y-Y3)*(X-X3)
      H4=(Y-Y4)*(X-X4)
      IF(CI12)363,363,364
  363 WS1=(CM12*E1-H1)/(Z*R1)
     WS2=(CM12*E2-H2)/(Z*R2)
      AT 1=ATAN(US1)
      AT2=ATAN(US2)
      TVZ=RT1-RT2
  364 IF(C123)366,366,367
  366 AT3=ATAN((CM23*E2-H2)/(Z*R2))
      AT4=ATAN((CM23*E3-H3)/(Z*R3))
      TUZ=TUZ+RT3-RT4
  367 |F(C|34)368,368,369
  368 AT5=ATAN((CM34*E3-H3)/(Z*R3))
      AT6=ATAN((CM34*E4-H4)/(Z*R4))
      TVZ=TVZ+AT5-AT6
  369 | F(C141)370,370,375
  370 AT7=ATAN((CM41*E4-H4)/(Z*R4))
      AT8=ATAN((CM41*E1-H1)/(Z*R1))
      TUZ=TUZ+AT7-AT8
  375 GO TO 450
           COMPUTE VELOCITY COEF. BY QUADRAPOLE METHOD
```



```
400 RPQ3=RPQ**3
      RP07=(RP03**2)*RP0
      WS1= X/RP03
      XSQ=X**2
      YS0=Y**2
      ZSQ=Z**2
      PS=YSQ+ZSQ-4.*XSQ
      OS=XS0+ZSQ-4, *YSQ
      NS2=X*(9.*PS+30.*XS0)/RPQ7
      WS3=3.*Y*PS/RPQ7
      WS4=3.*X*0S/RP07
      TUX=A*W$1-CTXY*W$3-CTXX*W$2-CTYY*W$4
      WS1=Y/RP03
      NS2=Y*(9.*0S+30.*YS0)/RP07
      TUY=A*W$1-CTXX*W$3-CTXY*W$4-CTYY*W$2
      TUZ=Z*(A/RPQ3-3.*(C1XX*PS-5.*C1XY*X*Y+C1YY*QS)/RPQ7)
  450 UX(IS)=TUX*XX+TUY*XY+TUZ *XN
      UY(18)=TUX*YX+TUY*YY+TUZ*YN
      UZ(18)=TUX*ZX+TUY*ZY+TUZ*ZN
      GO TO 470
        H. COMPUTE VELOCITY COEF. BY MONOPOLE METHOD
  460 ARP03=A/(AP0**3)
      UX(18)= (X00-X0)*ARP03
      UY(18)= (YC0-YC)*8RP03
      UZ(18)= (ZCQ-ZC)*ARPQ3
0

    REFLECT NULL PT. IN PLANE OF SYMETRY

  470 GO TO(480,485,490,495,500,505,510,515),IS
0
          DO LOOPS SET UP TO FORCE USE OF INDEX REGISTERS
  480 J1=JU
      J2=J0
      UDX=UX(1)
      VDY=VY(1)
      UDZ=UZ(1)
      U1(J1)=UX(1)
      U2(J1)=UX(1)
      U3(J1)=UX(1)
      V1(J1+1)=UY(1)
      02(J1+1)=0Y(1)
      U3(J1+1)=UY(1)
      V1(J1+2)=VZ(1)
      U2(J1+2)=UZ(1)
      V3(J1+2)=VZ(1)
      IF(SYM) 530,530,481
  481 19=2
C
              XZ SYMETRY
      Y00=-Y00
      GO TO 345
  485 IF(SYM-1)517,517,486
C
              XY SYMETRY
  486 19=3
      Z00=-Z00
      GO TO 345
  490 18=4
      Y00=-Y00
      GO TO 345
  495 IF(SYM-2)516,516,496
              YZ SYMETRY
  496 19=5
      XCQ=-XC0
      GO TO 345
  500 18=6
      YC0=-YC0
```



```
60 TO 345
  505 18=7
      Z0Q=-Z0Q
      GO TO 345
  510 IS=8
      Y00=-Y00
      G0 T0 345
        J. ADD CONTRIBUTIONS OF ALL REFLECTIONS
  515 U1(J1)=U1(J1)+UX(8)+UX(7)+UX(6)+UX(5)
      V2(J1)=V2(J1)-VX(8)+VX(7)+VX(6)-VX(5)
      V3(J1)=V3(J1)-VX(8)-VX(7)+VX(6)+VX(5)
      U1(J1+1)=U1(J1+1)-UY(8)+UY(7)+UY(6)-UY(5)
      V2(J1+1)=V2(J1+1)+VY(8)+VY(7)+VY(6)+VY(5)
      U3(J1+1)=U3(J1+1)+UY(8)+UY(7)+UY(6)+UY(5)
      V1(J1+2)=V1(J1+2)-VZ(8)-VZ(7)+VZ(6)+VZ(5)
      V2(J1+2)=V2(J1+2)+VZ(8)-VZ(7)+VZ(6)-VZ(5)
      U3(J1+2)=U3(J1+2)+UZ(8)+UZ(7)+UZ(6)+UZ(5)
 516 V1(J1)=V1(J1)+VX(4)+VX(3)
      U2(J1)=U2(J1)+UX(4)-UX(3)
      U3(J1)=U3(J1)=UX(4)=UX(3)
      V1(J1+1)=V1(J1+1)+VY(4)-VY(3)
      U2(J1+1)=U2(J1+1)+UY(4)+UY(3)
      V3(J1+1)=V3(J1+1)-VY(4)+VY(3)
      V1(J1+2)=V1(J1+2)-VZ(4)-VZ(3)
      U2(J1+2)=U2(J1+2)-UZ(4)+UZ(3)
      V3(J1+2)=V3(J1+2)+VZ(4)+VZ(3)
  517 U1(J1)=U1(J1)+UX(2)
      U2(J1)=U2(J1)-UX(2)
      U3(J1)=U3(J1)+UX(2)
      U1(J1+1)=U1(J1+1)=UY(2)
      V2(J1+1)=V2(J1+1)+VY(2)
      U3(J1+1)=U3(J1+1)=UY(2)
      U1(J1+2)=U1(J1+2)+UZ(2)
      U2(J1+2)=U2(J1+2)-UZ(2)
      V3(J1+2)=V3(J1+2)+VZ(2)
  530
        C1(J2)=XN0*U1(J1)+YN0*U1(J1+1)+ZN0*U1(J1+2)
        C2(J2)=XN0*U2(J1)+YN0*U2(J1+1)+ZN0*U2(J1+2)
        C3(J2)=XN0*V3(J1)+YN0*V3(J1+1)+ZN0*V3(J1+2)
  540 JV=JV+3
  541 JC=JC+1
C
        D. WRITE COEFICIENTS
           WRITE COEF. ON TAPE OR DRUM IF STORAGE AREA IS FULL
  545 IF(UV-1001)570,555,555
  555 JU=2
      U1(1)=BLK
      U2(1)=BLK
      U3(1)=BLK
      IF(BLK-636.0) 560,563,566
  580 WRITE (01) BLK,V1,U2,U3
      GO TO 568
  563 REWIND 01
  566 WRITE(11) BLK,U1,U2,U3
  568 BLK=BLK+1.
  570 IF(UC-901)580,571,571
  571 IDW=IDW+1
      WRITE (02) IDN,C1
      WRITE (08) IDU,C2
      WRITE (09) IDW,03
  576 JC=1
  580 KQ=KQ+7
      L=L+1
C
            END OF LOOP OVER NULL PTS.
```



```
0343,343,581
      IF(KQ-KM
  581 C1(JC)=0
      02(JC)=0
      C3(UC)=0
      IF(KQ-KMM)541,585,585
  585 P=P+1
      K=K+7
      J=J+20
               )585,586,600
      IF (K-KM
C
        N. END OF LOOP OVER QUADS.
           READ NEXT BLOCK OF B ARRAY IF NEEDED
  586 IF(J-241)296,590,590
  590 READ(04)(B(1), I=1,241)
      J=2
      IF(B(1)-P)595,296,595
  595 WRITE (6,98) B(1),P
      STOP
  600 IF(BLK-636.0) 610,620,630
        O. WRITE REMAINING COEF. ON TAPE OR DRUM
  610 WRITE(01)BLK, V1, V2, V3
      REMIND 01
      G0 T0 640
  620 REWIND 01
  530 WRITE(11) BLK, V1, V2, V3
      REWIND 11
  640 MRITE (02) IDW, C1
      WRITE (08) IDN,02
      WRITE (09) IDH,C3
      REWIND 02
      REWIND 03
      RENIND 04
      REMIND 08
      REWIND 09
       P. TRANSFER TO PEPS3
      GO TO 5000
 1000 URITE(6,2000) L.P.
 2000 FORMAT(3H L= ,15,20X,3H P= ,F5.1)
 5000 CONTINUE
      STOP 2
      END
      FUNCTION SQ2F(X1, X2, Y1, Y2, Z1, Z2)
      X=X1-X2
      Y=Y1-Y2
      Z=Z1-Z2
      RS=Z**2+Y**2+X**2
      R=RBS(X)+RBS(Y)+RBS(Z)+1.0E-20
      R=R+RS/R
      R= . 25*R+RS/R
      R= R+RS/R
      SQ2F= .25*R+RS/R
      RETURN
      END
```



APPENDIX III - XYZPF SECTION PF3

```
PROGRAM PFP3(OUTPUT=128, TAPE02, TAPE08, TAPE09,
                    TAPE 12, TAPE03, TAPE6=OUTPUT, TAPE2=TAPE02,
     1
     2
                    TRPES=TAPEOS.TAPE9=TAPEO9.TAPE3=TAPEO3>
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 1 SECTION 3
C
      SOLVES MATRIX EQUATION FOR SOURCE DENSITY
                 SN(654), U(P(650), S(5,650), PROB(15), WS(220), DM(650),
      COMMON
                 B(220), COEF(900), XN(650), YN(650), ZN(650)
     1
      EQUIVALENCE (WS(213), EPS) , (KK, B(201))
      EQUIVALENCE (MIX, WS(205)), (MIY, WS(206)), (MIZ, WS(207))
      EQUIVALENCE (WS(201), NP), (WS(208), IPS), (WS(212), IPF), (WS(211), KM),
     1(KM, MK)
    5 FORMAT(49H1XYZ POTENTIAL FLOW PROGRAM SECTION 3, VERSION 4 )
      WRITE (6,5)
                (03)(PR0B(1), 1=1, 15)
                        ( 6, 1001)(PR0B(I), I=1, 15)
 1001 FORMAT(1H0, 15A4)
      READ (03) (WS(1), 1=1,220), FEDIT3, FEDIT4
                (03)(SKIP, SKIP, SKIP, XN(L), YN(L), ZN(L), SKIP, L±1, NP)
      D=-.5/3.14159265
      READ
               (03)(DM(1), 1=1, NP)
      K1=1
      K2=NP
  240 FORMAT (18HOCHANGES IN PROB - 1584)
      IF(IPS)1220, 1220, 1231
 1231 READ
               (12)( B(K), K=1, 15)
      WRITE
                        ( 6,240)(B(K),K=1,15)
               (12)( B(K), K=1, 220)
      READ
      READ
               (12)SK1P
      READ
               (12)SKIP
      K1=IPS
      K2=IPF
        A. SET CONDITIONS FOR FLOW OF -1 IN X DIRECTION
 1220 FX=-1
      FY=0
      FZ=0
      NF=-1
            COMPUTE INITIAL APPROXIMATION TO THE SOURCE
 1240 DO 1250 K=1,NP
      VIP(K)=XN(K)*FX+YN(K)*FY+ZN(K)*FZ+DM(K)
      S(5,K)=-UIP(K)*,11936
       C. SET PARTIAL SUM VECTOR TO ZERO
 1250 SN(K)=0.
      SN(NP+1)=0.
      SN(NP+2)=0.
      SN(NP+3)=0.
      SN(NP+4)=0.
      NRITE(6,997) FX, FY, FZ
      WRITE (6,998)
 998 FORMAT(27H01TERATION SUM OF CHANGES ,9X,1HA,10X,2HB1,10X,2HB2)
      1T=1
      10=5
      IF (IPS) 1260, 1260, 1255
 1255 READ(12) ($(5,K), K=1,KK)
      DO 1256 K=1,KK
      00 1256 1=1,4
 1256 S(1,K)=S(5,K)
        D. START ITERATION
 1260 BAND=0
```



```
IF (NF) 1261, 1262, 1263
 1261 READ (02) IDW, COEF
      GO TO 1264
 1262 READ (08) DW, COEF
      GO TO 1264
 1263 READ (09)1DW,COEF
 1264 J=0
        D. READ FIRST BLOCK OF COEF
C
        E. START LOOP OVER QUADS.
      DO 1290 K=1, NP
        F. PICK UP SOURCE DEMSITY
C
      SP=S(IC,K)
C
        G. START LOOP OVER NULL PTS.
      DO 1290 KP=1,NP,5
      IF(J-900)80,65,65
   65 IF (NF)67,68,69
   67 READ (02)/DW,COEF
      GO TO 70
   68 READ (08) IDW, COEF
      GO TO 70
   69 READ (09) IDW, 090F
   78 J=0
C
          COMPUTE PARTIAL SUM FOR NEXT 5 PTS.
   80 SN(KP)=SN(KP)+C0EF(J+1)*SP
      SN(KP+1)=SN(KP+1)+C0EF(U+2)*SP
      SM(KP+2)=SM(KP+2)+00EF(J+3)*SP
      SN(KP+3)=SN(KP+3)+C0EF(J+4)*SP
      SN(KP+4)=SN(KP+4)+C0EF(J+5)*SP
      J=J+5
        J. END OF LOOP OVER NULL PTS.
        K. END OF LOOP OVER QUADS.
 1290 CONTINUE
        L. COMPUTE NEW SOURCE
      IF (NF) 91,92,93
   91 REWIND 02
      GO TO 94
   92 REWIND 08
      60 TO 94
   93 REWIND 09
   94 PRSS=1.0
      SUM=0.
      DO 100 K=K1,K2
      SM(K)=( SM(K)+UIP(K) )*D
      TEST=ABS(SN(K)-S(10,K))
      SUM=SUM+TEST
      IF (TEST .GT. EPS) PASS=-1.0
  100 CONTINUE
      IF (PASS .EQ. 1.0) GO TO 180
      IF (IT.GE.MIX) 60 TO 180
      IF (IEDITS .EQ. 0) WRITE(6,99) IT, SUM
      |T=|T+1
      10=10-1
      IF (IC .EQ. 0) GO TO 120
      DO 110 K=K1.K2
      S(IC,K)=SN(K)
  110 SN(K)=0.
      GO TO 1260
  120 A=0.
      B1=0.
      B2=0.
      DR=0.
      D1=0.
```



```
D2=0.
     DO 140 K= K1,K2
     DS9=2*S(1,K)-SN(K)-S(2,K)
     (F(DS9 .GT. 0.) GO TO 122
     A=A+S(2,K)-S(1,K)
     DA=DA-DS9
     GO TO 125
 122 A = A + S(1,K) - S(2,K)
     DA=DA+DS9
 125 DS1=S(4,K)-S(3,K)
     DS2=S(3,K)-S(2,K)
     DS3=DS1-DS2
     DSS=S(2,K)-S(1,K)
     DS5=DS2-DSS
     DS6=DS1-DSS
     DS4=DS2-S(1,K)+SN(K)
     DS7=DS3*DS4-DS5*DS6
     DS8=DS6*DS5-DS4*DS3
     IF(DS7 .GT. 0.) GO TO 128
     B1=B1-DS1*DS4+DS2*DS6
     D1=D1-D87
     GO TO 130
 128 B1=B1+DS1*DS4-DS2*DS6
     D1=D1+DS7
 130 IF (DS8 .GT. 0.) GO TO 132
     B2=B2-D81*D85+D82*D83
     D2=D2-DS8
     GO TO 140
 132 B2=B2+D81*D85-D82*D83
     D2=D2+DS8
 140 CONTINUE
     A=A/DA
     B1=B1/D1
     B2=B2/D2
     IF(IT .EQ. 6) GO TO 155
     AR=A-AS
     AA=ABS(AA)
     IF (AA .GT. .02) GO TO 148
     DO 145 K=K1,K2
     $(5,K)=A*($N(K)-$(1,K))+$(1,K)
 145 SN(K)=0.
     WRITE(6,6000)
6000 FORMAT(29X, 17HA EXTRAPOLATION
     GO TO 160
 148 BB1=B1-BS1
     BB1=ABS(BB1)
     BB1=50, *BB1
     BB2=B2-BS2
     BB2=ABS(BB2)
     BB2=50.*BB2
     BBB=ABS(B1) + ABS(B2)
     IF ( (BB1 .GT. BBB) .OR. (BB2 .GT. BBB) ) GO TO 155
     DO 150 K=K1,K2
     $(5,K)=$(2,K)+B1*($(1,K)-$(2,K))+B2*($N(K)-$(2,K))
 150 SN(K)=0.
     WRITE(6,7000)
7000 FORMAT(29X, 17HB EXTRAPOLATION
     60 TO 160
 155 DO 158 K=K1,K2
     S(5,K)=SN(K)
 158 SN(K)=0.
 160 10=5
```



```
WRITE(6,161) A, B1,
161 FORMAT(29X,3E12.3)
      AS=A
      BS1=B1
      BS2=B2
      60 TO 1260
  180 WRITE(6,99) IT,SUM
      DO 182 K=K1,K2
  182 S(1,K)=SN(K)
      WRITE(03) (S(1,K), K=1,NP)
   99 FORMAT(4X, 13, E18.5)
  997 FORMAT (13H0 X VELOCITY=,F4.1,15H Y VELOCITY=,F4.1,
     115H Z VELOCITY=,F4.1)
      1F(FZ)1400,1390,1400
C
       P1 IF THIS WAS NOT LAST FLOW, SET FOR NEXT FLOW
 1390 FZ=FY
      FY=FX
      FX=0
      MIX=MIY
      MIV=MIZ
      MF=MF+1
      GO TO 1240
 1400 REWIND 03
      P2 READ IN PEPS4 AND TRANSFER TO IT
      STOP 3
      END
```



APPENDIX IU - XYZPF SECTION PF4

```
PROGRAM PFP4(OUTPUT, TAPE6=OUTPUT, TAPE03, TAPE01, TAPE11,
                    TAPE3=TAPE03, TAPE1=TAPE01)
C
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 1 SECTION 4
C
      COMPUTES VELOCITIES AND PRESSURE COEFFICIENTS FOR
C
      POINTS ON THE BODY
C
                 VX1(650), VY1(650), VZ1(650),
                                               - VX2(650),UY2(650),UZ2(650)
      COMMON
                                               $1(650), $2(650), $3(650)
                ,UX3(650),UY3(650),UZ3(650),
     1
     2
                   X(650), Y(650), Z(650),
                                                 - T4(650), T5(650), T6(650)
                  DM(650)
     3
      DIMENSION PROB(15), WS(220), CV1(1000), CV2(1000), CV3(1000)
      EQUIVALENCE (WS(201),NP),(WS(211),KM),(WS(217),VXI),(WS(218),UYI),
      1(WS(219), VZI), (WS(208), IPS), (WS(212), IPF)
      EQUIVALENCE (MIX, WS(205)), (MIY, WS(206)), (MIZ, WS(207))
    5 FORMAT(49HOXYZ POTENTIAL FLOW PROGRAM SECTION 4, VERSION 4 )
      WRITE (6,5)
      READ
               (03)(PROB(1), I=1, 15)
  100 FORMAT(1H , 1584)
      WRITE
                        ( 6,100)(PR08(1),1=1,15)
C.
            READ PARAMETERS AND SOURCE
      READ (03) (NS(I), I=1,220), IEDIT3, IEDIT4
                (03)(X(1),Y(1),Z(1),T4(1),T5(1),T6(1),SKIP, T=1,NP)
                (03)(DM(1), I=1, NP)
      D=-.5/3.14159265
                (03)($1(L), L=1, NP)
      READ
                (03)(82(1), I=1, NP)
      READ (03) (S3(1), I=1, NP)
      K1 = 1
      K2=NP
      IF(IPS)108, 108, 102
  102 K1=1FS
      K2=TPF
  108 BBR=1.
C
        B. READ FIRST BLOCK OF COEF.
      ITAPE=01
      READ (01) BB,CV1,CV2,CV3
      IF (BB-BBR) 300,120,300
  120 DO 125!=K1,K2
      VX1(1)=-1.0
                          -$1(1)*T4(1)
                                          70.
      UV1(1)=
                          -S1(1)*T5(1)
                                          70
      VZ 1(1)=
                                          /D
                          -S1(1)*T6(1)
      UX2(1)=
                                          70
                          -S2(1)*T4(1)
      092(1)=-1.0
                          -82(1)*T5(1)
                                          10
      VZ2(1)=
                          -S2(1)*T6(1)
                                          /D
      UX3(1)=
                          -S3(1)*T4(1)
                                          70
      UY3(1)=
                          -S3(1)*T5(1)
                                          /D
  125 VZ3(1)=-1.0
                          -$3(1)*T6(1)
                                          70
C
        C. SET UP LOOP OVER QUADS.
      J0=2
C
        D. PICK UP SOURCE
  130 S1J=S1(J)
      $2J=$2(J)
      $3J=$3(J)
0
        E. SET UP LOOP OVER NULL PTS.
      DO 180 JP=K1,K2
C
        F. COMPUTE PARTIAL SUM FOR 3 COMPONENTS OF 3 VELOCITIES
      VX 1(JP )=VX 1(JP )+S 1J*CU 1(JC )
      UY1(JP)=UY1(JP)+S1J*CU1(JC+1)
```



```
UZ1(JP)=UZ1(JP)+S1J*CU1(JC+2)
      UX2(JP)=UX2(JP)+S2J*CU2(JC)
      UY2(JP)=UY2(JP)+S2J*CU2(JC+1)
      VZ2(JP)=VZ2(JP)+S2J* CV2(JC+2)
      UX3(JP)=UX3(JP)+S3J*CU3(JC)
      UY3(JP)=UY3(JP)+S3J*CU3(JC+1)
      UZ3(JP)=UZ3(JP)+$3J*CU3(JC+2)
      J0=J0+3
        G. READ MORE COEF. IF NEEDED.
C
      IF (JC-1000)180,135,135
  135 JC=2
      IF(BBR-635.0) 140,150,155
  140 READ (01) BB,CV1,CV2,CV3
      GO TO 160
  150 REWIND 01
  155 READ (11) BB, CV1, CV2, CV3
  160 BBR=BBR+1.
      IF (BBR-BB) 300, 180,300
C
            END OF LOOP OVER NULL PTS.
  180 CONTINUE
      1+ل=ل
0
            END OF LOOP OVER QUADS.
      IF(J-NP)130,130,200
  200 IF(BBR-635.0) 231,231,232
  231 REWIND 01
      GO TO 233
  232 REWIND 11
        K. EDIT THE VELOCITIES ETC. AND WRITE THEM ON TAPE
  233 WRITE
                 (03)(UX1(1),UY1(1),UZ1(1)
                                                  (1=1, MP)
                                                   , l=1,NP)
                 (03)(UX2(1),UY2(1),UZ2(1)
      WRITE
                                                   , I=1, NP)
      WRITE
                 (03)(UX3(1),UY3(1),UZ3(1)
  235 FORMAT(1H1, 15A4, 8H PAGE = , 115)
      REWIND 03
      IP=K1+49
      IS=K1
      IPAGE= 1
      IF (IEDIT4 .EQ. 1) 60 TO 293
      IF (MIX .LE.O ) 60 TO 265
  242 FORMAT(8H0 X FLOW)
  240 FORMAT(4H PT.,10X,1HX,9X,1HY,9X,1HZ,13X,2HUX,8X,2HUY,8X,2HUZ,10X,
1 SHABS.U, 7X,2HCP,6X,6HSOURCE,4X,8HV NORMAL)
  245 FORMAT (1X, F3, 4X, 3F10.5, 4X, 3F10.5, 1F13.5, 2F11.5, E12.2)
  250 IF(IP-K2)255,255,260
C
        J. COMPUTE PRESSURE AND ABS. VALUE OF VELOCITY
  255 WRITE
                         (6,235)(PROB(1), I=1, 15), IPAGE
                         (6,242)
      WRITE
      WRITE
                         (6.240)
      DO 257 1=18,1P
      USQ=UX1(1)**2+UY1(1)**2+UZ1(1)**2
      VM=(ABS(UX1(1))+ABS(UV1(1))+ABS(UZ1(1)))*.79
      VM=VM+US070M
      UM= . 25*UM+USQ/UM
      UM
            =.5*(U11+US0/U11)
      CP
            =1.-080
            =UX1(1)*T4(1)
      UNB
                             +UV1(1)*T5(1) +UZ1(1)*T6(1)
  257 NRITE (6,245) 1,X(1),Y(1),Z(1),UX1(1),UY1(1),UZ1(1),UM
         , CP
                  ,S1(L),UNR
      18=18+50
      IP=1P+50
      IPAGE=IPAGE+1
      IF(K2-IS) 265,260,250
  260 IP=K2
```



```
60 TO 255
  265 IP=K1+49
      1S=K1
      IF (MIY .LE.O ) GO TO 280
  267 IF(IP-K2)275,275,270
  270 IP=K2
  275 WRITE
                        (6,235)(PROB(1),1=1,15),1PAGE
                        (6,277)
      WRITE
  277 FORMAT(SHO Y FLOW)
      WRITE
                        (6,240)
      DO 278 I=IS, IP
      US0=UX2(1)**2+UV2(1)**2
                                 -+UZ2(1)**2
      UM=(ABS(UX2(1))+ABS(UY2(1))+ABS(UZ2(1)))*.79
      UM=UM+US@/UM
      UM= . 25*UM+USQ/UM
          =.5*(VM+VSQ/VM)
      UM
      UNF:
            =UX2(1)*T4(1) +UY2(1)*T5(1) +UZ2(1)*T6(1)
      CP
           =1.-080
 278 WRITE (6,245) 1,X(1),Y(1),Z(1),UX2(1),UY2(1),UZ2(1),UM
                , $2(1), UNR
     1 , CP
      18=18+50
      IP=1P+50
      IPAGE=IPAGE+1
      IF(IS-K2)267,267,280
 280 IP=K1+49
      1S=K1
      IF (MIZ .LE.O ) GO TO 293
  282 IF(IP-K2)290,290,285
 285 1P=K2
                        (6,235)(PROB(1),1=1,15),1PAGE
 290 WRITE
     WRITE
                        (6,292)
 292 FORMAT(8H0 Z FLOW)
     WRITE
                        (6,240)
     DO 291 I=IS.IP
     US0=UX3(1)**2+UY3(1)**2+UZ3(1)**2
     UM=(ABS(UX3(1))+ABS(UY3(1))+ABS(UZ3(1)))*.79
      UM=UM+US07UM
      UM=.25*UM+USQ/UM
      UM.
           =:5*(UM+US0/UM)
      CP
           =1.-USQ
      UNR
           =UX3(1)*T4(1) +UY3(1)*T5(1) +UZ3(1)*T6(1)
 291 WRITE (6,245) 1,X(1),Y(1),Z(1),UX3(1),UY3(1),UZ3(1),UM
          CP.
                ,83(1),UNR
     18=18+50
      IP=IP+50
      IPAGE=IPAGE+1
      IF(IS-K2)282,282,293
      L. CHECK FOR A FOURTH FLOW
  293 J = 1
  294 \text{ UXI} = \text{WS(J)}
      VYI = MS(J+20)
      VZI = WS(J+40)
  295 | F (UX|**2+UY|**2+UZ|**2) 400,400,301
  301 IS=K1
      IP=K1+49
  320 IF (IP-K2)330,325,325
       N. EDIT THE VELOCITY AND PRESSURE FOR FOURTH FLOW
  325 IP=K2
  330 WRITE
                        (6,235)(PROB(1),1=1,15),1PAGE
      WRITE
                        (6,315)0X1,0Y1,0Z1
      WRITE
                        (6,340)
0
            COMPUTE VELOCITY AND PRESSURE FOR FOURTH FLOW
```



```
DO 333 I=IS, IP
         =- (UX1*UX1(1)+UY1*UX2(1)+UZ1*UX3(1))
     UX4
         =- (UX1*UY1(1)+UY1*UY2(1)+UZ1*UY3(1))
     UY4
     UZ4 = -(UX1*UZ1(1)+UY1*UZ2(1)+UZ1*UZ3(1))
     US0=UX4
             **2+UY4
                       **2+UZ4
                                  ***2
     UM=(ABS(UX4)
                   )+ABS(UY4
                               )+ABS(UZ4
                                          >)*.79
     UM=UM+USQ/UM
    UM=.25*UM+US0/UM
          =.5*(UM+USQ/UM)
    UM
           = 1.-(USQ)/(-UY1**2+UZ1**2+UX1**2)
    CP.
333 WRITE (6,345) 1,X(1),Y(1),Z(1),UX4 ,UY4 ,UZ4
                                                          , UM
         , CP
     18=18+50
     IP=IP+50
     IPAGE=IPAGE+1
     IF(K2-19)350,325,320
350 J = J+1
     60 TO 294
315 FORMAT(19H0 ONSET FLOW, UX1=,F6.3,2X,4HUY1=,F6.3,2X,4HUZ1=,F6.3)
340 FORMATK4H PT., 10X, 1HX,9X, 1HY,9X, 1HZ, 13X,2HUX,8X,2HUY,8X,2HUZ, 10X,
    1 5HABS.U. 7X,2HCP)
345 FORMAT (1X,13,4X,3F10.5,4X,3F10.5,1F13.5,1F11.5)
400 CONTINUE
     GO TO 5000
300 CONTINUE
    WRITE (6,310) ITAPE, BBR, BB
310 FORMAT (6HITAPE ,12,17H OUT OF POSSITION/114,6F6.1)
5000 CONTINUE
     STOP 4
    END
```



APPENDIX U - XYZPF SECTION PF5

```
PROGRAM PFP5(INPUT=128.OUTPUT=128.TAPE03.TAPE04
     1TAPE5=INPUT, TAPE6=OUTPUT, TAPE3=TAPE03, TAPE4=TAPE04)
\epsilon
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 4 SECTION 5
C
      COMPUTES VELOCITIES AND PRESSURE COEFFICIENTS FOR
C
      OFF BODY POINTS
C
                                 XP(500), YP(500), ZP(500), VX1(500), WS(220)
      COMMON
                 B(241),
     1, VY1(500), VZ1(500), VX2(500), VY2(500), VZ2(500), VX3(500), VY3(500)
     2,UZ3(500),UX(8),UY(8),UZ(8),S1(650),S2(650),S3(650),U1(3),U2(3),U3
     3(3) ,PROB(15) ,XN(650),YN(650),ZN(650),TA(650),TX(650)
     4,TY(650),TZ(650)
      EQUIVALENCE (KM, WS(211)), (KM, MK), (NP, WS(201)), (SYM, WS(210))
     1, (Y2, Y3), (MIX, WS(205)), (MIY, WS(206)), (MIZ, WS(207))
      INTEGER PAGE
      INTEGER SYM
    5 FORMAT(49HOXYZ POTENTIAL FLOW PROGRAM SECTION 5, VERSION 4
      WRITE (6,5)
        A. READ IMPUT
C
      READ(5,25) NOBP, LEDITS, LREAD
\mathbb{C}
        A. READ THE OFF BODY POINTS
      NOB=NOBP
      DO 10 1=1,NOB
      READ(5,26) = XP(1), YP(1), ZP(1)
      IF (EGF(5) .EQ. 0.) GO TO 10
      NOBP=1-1
      WRITE(6,9) NOBP, NOB
    9 FORMAT(1H0,15,31H OFF BODY POINTS SPECIFIED NOT ,13)
      GO TO 11
   10 CONTINUE
   11 CONTINUE
   25 FORMAT(314)
   26 FORMAT(3F12.5)
      P=1.
      READ (03) (PROB(1), I=1, 15)
      WRITE (6,90) (PROB(1),1=1,15)
   90 FORMAT(1H0, 18A4)
      WRITE(6,91) NOBP, LEDITS, IREAD
   91 FORMAT(8HONOBP = ,14 /SH | LEDITS= ,14/SH | IREAD = ,14)
      WRITE(6,92)
   92 FORMAT(17HO OFF BODY POINTS / 4H PT., 11X, 1HX, 12X, 1HY, 12X, 1HZ)
      WRITE(6,93) (1,XP(1), VP(1), ZP(1), I=1,NOSP)
   93 FORMAT(1X,13,2X,3F13.5)
C
        B. READ THE PARAMETERS, T ARRAY AND SOURCE FROM TAPE 31
      READ (03) (WS(1), I=1,220)
      READ (03) (TX(1),TY(1),TZ(1),XN(1),YN(1),ZN(1),TR(1),1=1,NP)
      READ (03) SKIP
C FORMERLY: WS(220) .EQ. 2.
C
      IF(NS(220) .EQ. 5.) READ(03) SKIP
      READ (03) ($1(1),1=1,NP)
      READ (03) ($2(1),1=1,NP)
      READ (03) ($3(1), I=1, NP)
C
            READ THE FIRST BLOCK OF THE B ARRAY
      READ (04) (B(1), I=1,241)
      K=1
      J = 1
      DO 100 L=1.NOBP
Ū
        D. SET THE PARTIAL VELOCITY TO THE FREE STREAM VELOCITY
```



```
VX1(1)=-1.0
      VY1(1)=0.
      VZ1(1)=0.
      VX2(1)=0.
      VY2(1)=-1.0
      0.0 = 0.0
      0.0=0.0
      VZ3(1)=-1.0
  100 UZ2(1)=0.
  290 IF(B(1)-P)291,295,291
  291 WRITE (6,98) B(1),P
   98 FORMAT(28HO POINTS OUT OF ORDER B(1)=,1F4.0,4H P=,1F4.0)
      STOP
C
        E.
           START LOOP OVER THE QUADS.
  295 J=2
        F1 PICK UP QUAD, INFORMATION
  296 X1=B(J)
      Y1=B(J+1)
      X2=B(J+2)
      Y2=B(J+3)
      X3=B(J+4)
      X4=B(J+5)
      Y4=B(J+6)
      XC=TX(K)
      VC=TV(K)
      ZC=TZ(K)
      A =TA(K)
      XX=B(J+7)
     YX=B(J+8)
      ZX=B(J+9)
      XY=B(J+10)
      YY=8(J+11)
      ZY=B(J+12)
0
        F2 COMPUTE LENGTH OF SIDES OF OUAD.
      D12=S02F(X1,X2,Y1,Y2,0.,0.)
      D23=SQ2F(X2,X3,Y2,Y3,.0,.0)
      D34=S02F(X3,X4,Y3,Y4,.0,.0)
      D41=S02F(X4,X1,Y4,Y1,.0,.0)
        F3 COMPUTE SLOPE OF SIDES
C
      1F(X2-X3)305,300,305
  300 CI23=1.
      GO TO 310
  305 CM23=(Y2-Y3)/(X2-X3)
      0123=0.
  310 IF(X3-X4)315,311,315
  311 0134=1.
      GO TO 320
  315 CM34=(Y4-Y3)/(X4-X3)
      0134=0.
  320 IF(X4-X1)325,321,325
  321 0141=1.
      GO TO 330
  325 CM41=(Y1-Y4)/(X1-X4)
      C141=0.
  330 IF(X1-X2)335,331,335
  331 Cl 12=1.
      GO TO 340
  335 CM12=(Y2-Y1)/(X2-X1)
      0112=0.
        F4 COMPUTE QUADRAPOLE MOMENTS
  340 CTXX=B(J+17)
      CTXY=B(J+18)
```



```
CTYY=B(J+19)
C
        F5 COMPUTE SIN AND COS OF SLOPE ANGLE FOR EACH SIDE
      CY12=(Y2-Y1)/D12
      CY23=(Y3-Y2)/D23
      CY34=(Y4-Y3)/D34
      CY41=(Y1-Y4)/D41
      CX 12=(X 1-X2)/D12
     CX23=(X2-X3)/D23
     CX34=(X3-X4)/D34
     CX41=(X4-X1)/D41
        F6 COMPUTE MAX DIAGINAL
      ST=SQ2F(X1,X3,Y1,Y3,0.,0.)
      ST2=SQ2F(X2,X4,Y2,Y4,.0,.0)
      IF(ST-ST2)341,342,342
  341 ST=ST2
        G. START LOOP OVER THE OFF BODY POINTS
  342 DO 530 JQ=1,NOBP
      18=1
      XCQ=XP(UQ)
      YCO=YP(UQ)
      200=ZP(J0)
      J1=1
  345 RPQ=SQ2F(XC,XCQ,YC,YCQ,ZC,ZCQ)
       H. DETERMIN METHOD
      IF(RPQ-ST*4)350,350,460
 350 X=(X00-X0)*XX+(Y00-Y0)*YX+(Z00-Z0)*ZX
      Y=(X00-X0)*XY+(Y00-Y0)*YY+(Z00-Z0)*ZY
      Z=(XCQ-XC)*XN(K)+(YCQ-YC)*YN(K)+(ZCQ-ZC)*ZN(K)
      1F(RPQ-ST*2.5)355,355,400

    COMPUTE INDUSED VELOCITY BY EXACT METHOD

  355 R1=S02F(X,X1,Y,Y1,Z,0.)
     R2=SQ2F(X,X2,Y,Y2,Z,0.)
R3=SQ2F(X,X3,Y,Y3,Z,0.)
      P4=SQ2F(X,X4,Y,Y4,Z,0.)
      IF((R1+R2),LE,D12) GO TO 1000
      IF((R3+R2),LE.D23) GO TO 1000
      IF((R3+R4).LE.D34) GO TO 1000
      IF((R1+R4).LE.D41) 60 TO 1000
      CLA 1=ALOG((R1+R2+D12)/(R1+R2+D12))
      CLA2=ALOG((R2+R3-D23)/(R2+R3+D23))
      CLR3=RL0G((R3+R4-D34)/(R3+R4+D34))
      CL64=8L06((84+81-041)/(84+81+041))
      TUX=CY12*CLA1+CY23*CLA2+CY34*CLA3+CY41*CLA4
      TUY=CX12*CLB1+CX23*CLB2+CX34*CLB3+CX41*CLB4
      TVZ=0.
      IF(ABS(Z)=.001*ST)375,361,361
 361 ZSQ=Z**2
      E1=ZSQ+(X-X1)**2
      E2=ZS0+(X-X2)**2
      E3=ZS0+(X-X3)**2
      E4=ZS0+(X-X4)**2
      H1=(Y-V1)*(X-X1)
      H2=(Y-Y2)*(X-X2)
      H3=(Y-Y3)*(X-X3)
     H4=(Y-Y4)*(X-X4)
      IF(CI12)363,353,364
  363 US1=(CM12*E1-H1)/(Z*R1)
      WS2=(CM12*E2-H2)/(Z*R2)
      AT 1=ATAN(US1)
      AT2=ATRN(US2)
      TVZ=RT 1-RT2
  364 IF(C123)366,366,367
```



```
366 AT3=ATAN((CM23*E2-H2)/(Z*R2))
      AT4=ATAN((CM23*E3-H3)/(Z*R3))
      TUZ=TUZ+AT3-AT4
  367 IF(C134)368,368,369
  368 AT5=ATAN((CM34*E3-H3)/(Z*R3))
      AT6=ATAN((CM34*E4-H4)/(Z*R4))
      TUZ=TUZ+AT5-AT6
  369 IF(CI41)370,370,375
  370 AT7=ATAN((CM41*E4-H4)/(Z*R4))
      AT8=ATAN((CM41*E1-H1)/(Z*R1))
      TUZ=TUZ+AT7-AT8
  375 GO TO 450
        J. COMPUTE INDUSED VELOCITY BY QUADRAPOLE METHOD
  400 RPQ3=RP0**3
      RP07=(RP03**2)*RP0
      WS1= X/RPQ3
      XS0=X**2
      YS0=Y**2
      ZSQ=Z**2
      PS=YS0+ZS0-4,*XS0
      OS=XS0+ZS0-4,*YS0
      NS2=X*(9.*PS+30.*XS0)/RPQ7
      NSS=S.*Y*PS/RPQ7
      WS4=3.*X*0S/RP07
      TUX=R*NS1-C1XY*NS3-C1XX*NS2-C1YY*NS4
      WS 1=Y/RP03
      WS2=Y*(9,*0S+30,*YS0)/RP07
      TUY=8*U3 1-01XX*U33-01XY*U34-01YY*US2
      TUZ=Z*(A/RPQ3-3.*(C1XX*PS-5.*C1XY*X*Y+C1YY*QS)/RPQ7)
 450 UX(1S)=TUX*XX+TUY*XY+TUZ*XN(K)
      UY(18)=TUX*YX+TUY*YY+TUZ*YN(K)
     UZC(S)=TUX*ZX+TUY*ZY+TUZ*ZN(K)
      GO TO 470
       K. COMPUTE INDUSED VELOCITY BY MONOPOLE METHOD
 450 ARP03=A/(RP0**3)
      UX(IS)= (XCQ-XC)*ARPQ3
      VY(18)= (YC0-YC)*ARP03
      VZ(1S) = (Z00 - Z0)*ARP03
Ū
       L. REFLECT OFF BODY POINT IN PLANE OF SYMETRY
  470 GO TO(480,485,490,495,500,505,510,515),IS
 489 U1(J1)=UX(1)
     U2(J1)=UX(1)
     V3(J1)=VX(1)
     U1(J1+1)=UV(1)
     V2(J1+1)=VY(1)
     V3(J1+1)=VY(1)
     V1(J1+2)=UZ(1)
     V2(J1+2)=VZ(1)
     U3(J1+2)=UZ(1)
      IF(SYM) 525,525,481
 481 IS=2
              XZ SYMETRY
     Y00=-Y00
     GO TO 345
 485 IF(SYM-1)517,517,486
             XY SYMETRY
 486 IS=3
     Z00=-Z00
     GO TO 345
 490 18=4
     Y00=-Y00
     60 TO 345
```



```
495 IF(SYM-2)516,516,496
C.
              YZ SYMETRY
  496 18=5
      XCQ=-XCQ
      GO TO 345
  500 IS=6
      YCQ=-YCQ
      GO TO 345
  505 IS=7
      Z00=-Z00
      GO TO 345
  510 18=8
      Y00=-Y00
      GO TO 345
        M. ADD CONTRIBUTIONS OF ALL REFLECTIONS
C
  515 V1(J1)=V1(J1)+VX(8)+VX(7)+VX(6)+VX(5)
      V2(J1)=V2(J1)=VX(8)+VX(7)+VX(6)=VX(5)
      V3(J1)=V3(J1)-VX(8)-VX(7)+VX(6)+VX(5)
      V1(J1+1)=V1(J1+1)-VY(8)+VY(7)+VY(6)-VY(5)
      U2(J1+1)=U2(J1+1)+UY(8)+UY(7)+UY(6)+UY(5)
      U3(J1+1)=U3(J1+1)+UY(8)-UY(7)+UY(6)-UY(5)
      U1(J1+2)=U1(J1+2)-UZ(8)-UZ(7)+UZ(6)+UZ(5)
      V2(J1+2)=V2(J1+2)+VZ(8)-VZ(7)+VZ(6)-VZ(5)
      V3(J1+2)=V3(J1+2)+VZ(8)+VZ(7)+VZ(6)+VZ(5)
  516 U1(J1)=U1(J1)+UX(4)+UX(3)
      U2(J1)=U2(J1)+UX(4)-UX(3)
      U3(J1)=U3(J1)=UX(4)=UX(3)
      U1(J1+1)=U1(J1+1)+UY(4)-UY(3)
      U2(J1+1)=U2(J1+1)+UY(4)+UY(3)
      U3(J1+1)=U3(J1+1)=UY(4)+UY(3)
      V1(J1+2)=V1(J1+2)-VZ(4)-VZ(3)
      V2(J1+2)=V2(J1+2)-VZ(4)+VZ(3)
      U3(J1+2)=U3(J1+2)+UZ(4)+UZ(3)
  517 V1(J1)=V1(J1)+VX(2)
      U2(J1)=U2(J1)-UX(2)
      U3(J1)=U3(J1)+UX(2)
      V1(J1+1)=V1(J1+1)=VY(2)
     U2(J1+1)=U2(J1+1)+UY(2)
      U3(J1+1)=U3(J1+1)-UY(2)
      V1(J1+2)=V1(J1+2)+VZ(2)
      U2(J1+2)=U2(J1+2)-UZ(2)
      V3(J1+2)=V3(J1+2)+VZ(2)
  525 L=P
      UX1(J0)=UX1(J0)+U1(1)*S1(L)
      VY1(JQ)=VY1(J0)+V1(2)*S1(L)
      VZ1(JQ)=VZ1(JQ)+V1(3)*S1(L)
      VX2(JQ)=VX2(JQ)+V2(1)*S2(L)
      VY2(J0)=VY2(J0)+V2(2)*S2(L)
      UZ2(J0)=UZ2(J0)+U2(3)*S2(L)
      VX3(JQ)=VX3(JQ)+V3(1)*S3(L)
      VY3(J0)=VY3(J0)+V3(2)*S3(L)
      VZ3(JQ)=VZ3(JQ)+V3(3)*S3(L)
  530 CONTINUE
C
        N. END OF LOOP OVER OFF BODY POINTS
  585 P=P+1
      K=K+1
      J=J+20
      IF(K-NP )586,586,599
  586 IF(J-241)296,590,590
        O. READ NEXT BLOCK OF B ARRAY IF NEEDED
  590 READ (04) (B(1),1=1,241)
      J=2
```



```
IF(B(1)-P)291,296,291
      Ρ.
         END OF LOOP OVER QUADS
599 CONTINUE
    PRGE = 1
    IF (IEDIT5 .EQ. 1) GO TO 825
601 FORMAT(4H PT., 11X, 1HX, 12X, 1HY, 12X, 1HZ, 14X, 2HVX, 11X, 2HVY, 11X, 2HVZ
   1,14X,2HCP)
602 FORMAT(7H X FLOW)
603 FORMAT(7H Y FLOW)
604 FORMAT(7H Z FLOW)
605 FORMAT(1H1, 15A4, 10X, 15HOFF BODY POINTS , 10X, 5HPAGE , 13)
    IF (MIX.EQ.0) GO TO 700
    WRITE(6,605) PROB, PAGE
    WRITE (6,602)
    WRITE (6,601)
    LIME=1
    LAST=53
606 IF(NOBP-LAST)607,610,610
607 LAST=NOBP
610 DO 615 I=LINE,LAST
611 FORMAT(1X, 113, 2X, 3F13.5, 2X, 3F13.5, 3X, F13.5)
      Q. COMPUTE PRESSURE AND EDIT 3 BASIC FLOWS
    CP1=1,-(UX1(1)**2+UV1(1)**2+UZ1(1)**2)
615 WRITE (6,611) L,XP(L),YP(L),ZP(L),VX1(L),VY1(L),VZ1(L),CP1
    LINE=LAST+1
    LAST=LINE+54
    PAGE=PAGE+1
    IF(LINE-NOBP)620,620,700
620 WRITE(6,605) PROB,PAGE
    WRITE (6,601)
    GO TO 606
700 IF (MIY.EQ.0) GO TO 800
    WRITE(6,605) PROB,PAGE
    WRITE (6,603)
    WRITE (6,601)
    LINE=1
    LAST=55
706 IF(NOBP-LAST)707,710,710
707 LAST=NOBP
710 DO 715 I=LINE, LAST
    CP2=1.=(UX2(1)**2+UY2(1)**2+UZ2(1)**2)
715 WRITE (6,611) 1,XP(1),YP(1),ZP(1),UX2(1),UY2(1),UZ2(1),CP2
    LINE=LAST+1
    LAST=LINE+54
    PAGE=PAGE+1
    IF(LINE-NOSP)720,720,800
720 WRITE(6,605) PROB, PAGE
    WRITE (6,601)
    GO TO 706
800 IF (MIZ.E0.0) GO TO 825
    WRITE(6,605) PROB,PAGE
    WRITE (6,604)
    WRITE (6,601)
    LINE=1
    LAST=55
806 IF(NOBP-LAST)807,810,810
807 LAST=NOBP
810 DO 815 I=LINE, LAST
    CP3=1.-(UX3(1)**2+UY3(1)**2+UZ3(1)**2)
815 WRITE (6,611) [,XP(1),YP(1),ZP(1),UX3(1),UV3(1),UZ3(1),CP3
    LINE=LAST+1
    LAST=LINE+54
```



```
PAGE=PAGE+1
     IF(LINE-NOBP)820,820,825
820 WRITE(6,605) PROB,PAGE
    WRITE (6,601)
     GO TO 806
825 J = 1
826 IF (IREAD.EQ.0) GO TO 827
    READ(5,26) UX4,UY4,UZ4
     IF (EOF(5).NE. 0.) GO TO 900
    GO TO 828
827 UX4=WS(J)
    UV4 = HS(J+20)
     UZ4 = US(J+40)
828 CP=UX4**2+UY4**2+UZ4**2
     IF(CP)900,900,830
      R. COMPUTE FOURTH FLOW AND EDIT IT
830 LINE=1
    LAST=51
    WRITE(6,605) PROB, PAGE
                              UX = F7.3/15X,4HUY = 
831 FORMAT(19HOONSET FLOW
    1F7.3/15X,4HUZ = ,F7.3)
    WRITE (6,831) UX4,UY4,UZ4
    WRITE (6,601)
835 IF(NOBP-LAST)837,840,840
837 LAST=NOBP
840 DO 845 I=LINE, LAST
     UXP=-UX4*UX1(1)-UY4*UX2(1)-UZ4*UX3(1)
    UYP=-UX4*UY1(1)-UY4*UY2(1)-UZ4*UY3(1)
    UZP=-UX4*UZ1(1)-UY4*UZ2(1)-UZ4*UZ3(1)
     CP4= 1.-(UXP**2+UYP**2+UZP**2)/CP
845 WRITE (6,611) 1, XP(1), YP(1), ZP(1), VXP, VYP, VZP, CP4
    LINE=LAST+1
    LAST=LINE+54
    PAGE=PAGE+1
     IF(LINE-NOBP)850,850,860
850 WRITE(6,605) PROB,PAGE
    WRITE (6,601)
    GO TO 835
860 d = d+1
    GO TO 826
1000 WRITE(6, 1001) JQ,L,XP(JQ),YP(JQ),ZP(JQ)
1001 FORMAT(16HOOFF BODY POINT , 13,23H ON BOUNDARY OF QUAD
                                                                  ,13/
           3H X=,F12.5,5X,2HY=,F12.5,5X,2HZ=,F12.5)
    GO TO 530
900 CONTINUE
      S. REWIND TAPES AND STOP
    REWIND 03
    RENIND 04
    STOP 5
    FUNCTION SQ2F(X1, X2, Y1, Y2, Z1, Z2)
    X=X1-X2
    Y=Y1-Y2
    Z=Z1-Z2
    BS=Z**2+Y**2+X**2
    R=ABS(X)+ABS(Y)+ABS(Z)+1.0E-20
    R=R+RS/R
    R= . 25*R+RS/R
    R= R+RS/R
    SQ2F= .25*R+RS/R
    RETURN
    END
```



APPENDIX VI - XYZPF SECTION PF6

```
PROGRAM PFP6(INPUT=128, TAPE16, OUTPUT=128, TAPE03, TAPE04,
                    TAPES=INPUT, TAPE6=OUTPUT, TAPE3=TAPE03, TAPE4=TAPE04)
C
      XYZ POTENTIAL FLOW PROGRAM VERSION 4 SECTION 6
C
C
      COMPUTES VELOCITIES AND PRESSURE COEFFICIENTS FOR
C
      OFF BODY STREAMLINES
               XP(100), YP(100), ZP(100), VX1(100), NS(220)
     1, VY1(100), VZ1(100), VX2(100), VY2(100), VZ2(100), VX3(100), VY3(100)
     2,UZ3(100),UX(8),UY(8),UZ(8),S1(650),S2(650),S3(650),U1(3),U2(3),U3
     3(3) , PROB(15) , XN(650), YN(650), ZN(650), TX(650), TY(650), TZ(650)
     1,B(13000),
                        XT(100), YT(100), ZT(100), AP(5), GM(4), SKY(100),
     1 SKZ(100),SKX(100),DX(100),DY(100),DZ(100),CP(100)
      EQUITARLENCE (KM, WS(211)), (KM, MK), (NP, WS(201)), (SYM, WS(210))
     1, (Y2, Y3)
      INTEGER SYM ,P
C
        A. READ INPUT
      WRITE (6,5)
    6 FORMAT(314,4F12.5)
    8 FORMAT(3F12.5)
    5 FORMAT(49H0XYZ POTENTIAL FLOW PROGRAM SECTION 6, VERSION 4 )
    7 FORMAT (1X,9F12.5)
   20 FORMAT(1H1,14,31H STREAMLINES TO BE COMPUTED AT
                                                         .14,10H STEPS OF
     1 ,F8.4,28H T FOR AN ONSET VELOCITY OF ,3F8.4)
   21 FORMAT(1X, 15HSTARTING POINTS/,3X,2HPT,5X,1HX,11X,1HY,11X,1HZ)
   22 FORMAT(1X,14,3F12.5)
      READ (03) (PROB(1),!=1,15)
      WRITE (6.90) (PROS(1), 1=1, 15)
   90 FORMAT(1H0, 15A4)
            READ THE PARAMETERS, I ARRAY AND SOURCE FROM TAPE 31
      READ (03) (NS(1), I=1, 220)
      READ(03) (TX(L),TY(L),TZ(L),XN(L),YN(L),ZN(L),TA(L),L=1,NP)
      READ (03) SKIP
      IF ( WS(220) .EQ. 2. ) READ(03) SKIP
      READ (03) (S1(1), I=1,NP)
      READ (03) (S2(I), I=1,NP)
      READ (03) ($3(1),1=1,NP)
C
        C. READ THE B ARRAY
      WZ = NP
      WZ = (WZ + 11.0)/12.0
      NB = WZ
      18 = 2
      1F=241
      D0 12 IP = 1.NB
      READ (04) P, (B(1), 1=18, 1F)
      18=18+240
   12 IF=1F+240
      AP(1) = .5
      AP(2) = .5
      AP(3) = 1.
      RP(4)=0.
      AP(5)=0.
      GM(1) = 1.76.
      GM(2) = 1.73.
      GM(3) = 1./3.
   83 READ (5,6) NOBP, NST, LEND, DT, UXI, UYI, UZI
      USQ=UX1**2+UV1**2+UZ1**2
      NOB=NOBP
      DO 10 I=1, NOB
      READ(5, 8) XP(1), YP(1), ZP(1)
```



```
IF (E0F(5) .EQ. 0.) GO TO 10
      MOBP=1-1
      WRITE(6,9) NOBP, NOB
    9 FORMAT(1H0,15, 28H STREAMLINES SPECIFIED NOT ,13)
      GO TO 11
   10 CONTINUE
   11 CONTINUE
      WRITE(16) NOBP, NST, LEND, UXI, UYI, UZI
      WRITE(6,20) NOBP, NST, DT, UXI, UYI, UZI
      WRITE(6,21)
      WRITE(6,22) (1,XP(1),YP(1),ZP(1), I=1,N08P)
      NOBP - NUMBER OF STREAMLINES TO BE TRACED.
C
      NST - NUMBER OF STATIONS AT WHICH STREAMLINES SHOULD BE COMPUTED.
C
      00 15 I=1,NOBP
      XT(1) = XP(1)
      YT(1) = YP(1)
      ZT(1) = ZP(1)
      SKX(1)=0.
      SKY(1) = 0.
   15 \text{ SKZ}(1) = 0.
      TC=0
      TRK=5
   98 K=1
      P = 1
      J= 1
      DO 100 I=1, NOBP
        D. SET THE PARTIAL VELOCITY TO THE FREE STREAM VELOCITY
€:
      VX1(1)=-1.0
      VY1(1)=0.
      V21(1)=0.
      UX2(1)=0.
      VY2(1)=-1.0
      UX3(1)=0.0
      UY3(1)=0.0
      VZ3(1)=-1.0
  100 VZ2(1)=0.
        E. START LOOP OVER THE QUADS.
  295 J=2
        F1 PICK UP QUAD, INFORMATION
  296 X1=B(J)
      Y1=B(J+1)
      X2=B(J+2)
      Y2=B(J+3)
      X3=8(J+4)
      X4=B(J+5)
      Y4=8(J+6)
      XC=TX(K)
      YC=TY(K)
      ZC=TZ(K)
      A = TA(K)
      XX=B(J+7)
      YX=8(J+8)
      ZX=B(J+9)
      XY=B(J+10)
      YY=B(J+11)
      ZY=B(J+12)
C
        F2 COMPUTE LENGTH OF SIDES OF OURD.
      D12=S02F(X1, X2, Y1, Y2, 0., 0.)
      D23=SQ2F(X2,X3,Y2,Y3,.0,.0)
      D34=SQ2F(X3,X4,Y3,Y4,.0,.0)
      D41=SQ2F(X4,X1,Y4,Y1,.0,.0)
C
        F3 COMPUTE SLOPE OF SIDES
```



```
IF(X2-X3)305,300,305
  300 0123=1
      GO TO 310
  305 CM23=(Y2-Y3)/(X2-X3)
      0123=0.
  310 IF(X3-X4)315,311,315
  311 0134=1.
      GO TO 320
  315 CM34=(Y4-Y3)/(X4-X3)
      0134=0.
  320 IF(X4-X1)325,321,325
  321 0141=1.
      GO TO 330
  325 CM4 1=(Y1-Y4)/(X1-X4)
      C141=0.
  330 IF(X1-X2)335,331,335
  331 Cl12=1.
      60 TO 340
  335 CM12=(Y2-Y1)/(X2-X1)
      0112=0
        F4 COMPUTE QUADRAPOLE MOMENTS
  340 C1XX=B(J+17)
      C1XY=B(J+18)
      CTYY=8(J+19)
        F5 COMPUTE SIN AND COS OF SLOPE ANGLE FOR EACH SIDE
C
      CY12=(Y2-Y1)/D12
      CY23=(Y3-Y2)/D23
      CY34=(Y4-Y3)/D34
      CY41=(Y1-Y4)/D41
      CX 12=(X1-X2)/D12
      CX23=(X2-X3)/B23
      CX34=(X3-X4)/D34
      CX4 1= (X4-X1)/B41
        F6 COMPUTE MAX DIAGINAL
      ST=S02F(X1,X3,Y1,Y3,0.,0.)
      ST2=SQ2F(X2,X4,Y2,Y4,.0,.0)
      IF(ST-ST2)341,342,342
  341 ST=ST2
        G. START LOOP OVER THE OFF BODY POINTS
  342 DO 530 JQ=1,NOBP
      1S=1
      X00=XP(J0)
      Y00=Y2(J0)
      Z00=ZP(J0)
      J1 = 1
  345 RPQ=SQ2F(X0,X0Q,Y0,Y0Q,Z0,Z0Q)
        H. DETERMIN METHOD
      IF(RPQ-ST*4)350,350,460
  350 X=(XCQ-XC)*XX+(YCQ-YC)*YX+(ZCQ-ZC)*ZX
      Y=(XCO-XC)*XY+(YCO-YC)*YY+(ZCO-ZC)*ZY
      Z=(X0Q-X0)*XN(K)+(Y0Q-Y0)*YN(K)+(Z0Q-Z0)*ZN(K)
      !F(RPQ-ST*2.5)355,355,400
            COMPUTE INDUSED VELOCITY BY EXACT METHOD
  355 R1=SQ2F(X,X1,Y,Y1,Z,O.)
      R2=S02F(X,X2,Y,Y2,Z,0.)
      R3=SQ2F(X,X3,Y,Y3,Z,0.)
      R4=SQ2F(X,X4,Y,Y4,Z,0.)
      CLB1=BLOG((B1+B2-D12)/(B1+B2+D12))
      OLA2=ALOG((R2+R3-D23)/(R2+R3+D23))
      CLA3=ALOG((R3+R4-D34)/(R3+R4+D34))
      CLR4=RL0G((R4+R1-D41)/(R4+R1+D41))
      TVX=CY 12*CLA 1+CY23*CLA2+CY34*CLA3+CY4 1*CLA4
```



```
TUY=0X12*0LA1+0X23*0LA2+0X34*0LA3+0X41*0LA4
      TUZ=0.
      IF(ABS(Z)-.001*ST)375,361,361
 361 ZSQ=Z**2
      E1=280+(X-X1)**2
      E2=ZSQ+(X-X2)**2
     E3=ZSQ+(X-X3)**2
     E4=ZS0+(X-X4)**2
     H1=(Y-Y1)*(X-X1)
     H2=(Y-Y2)*(X-X2)
     H3=(Y-Y3)*(X-X3)
     H4=(Y-Y4)*(X-X4)
      IF(0112)363,363,364
 363 NS1=(CM12*E1-H1)/(Z*R1)
     WS2=(CM12*E2-H2)/(Z*R2)
     AT 1=ATAM(NS1)
     AT2=ATAN(NS2)
      TUZ=AT 1-AT2
  354 IF(C123)356,356,367
 366 RT3=ATAN((CM23*E2-H2)/(Z*R2))
      RT4=ATAN((CM23*E3-H3)/(Z*R3))
      TUZ=TUZ+AT3-AT4
 367 IF(C134)368,368,369
 358 AT5=ATAN((CM34*E3-H3)/(Z*R3))
      RT6=RTRN((CM34*E4-H4)/(Z*R4))
     TUZ=TUZ+AT5-AT6
 369 !F(0141)370,370,375
 370 AT7=ATAN((CM41*E4-H4)/(Z*R4))
      AT8=AT6N((CM41*E1-H1)/(Z*B1))
      TUZ=TUZ+AT7-AT8
 375 GO TO 450
          COMPUTE INDUSED VELOCITY BY QUADRAPOLE METHOD
  400 RP03=RP0***3
      RPQ7=(RPQ3**2)*RPQ
     WS1= X/RP03
     XS0=X**2
     YS0=Y**2
     ZS0=Z**2
     PS=YS0+ZS0-4.*XS0
      QS=XSQ+ZSQ-4,*YSQ
     US2=X*(9,*PS+30,*XS0)/RP07
     WS3=3.*Y*PS/RPQ7
     WS4=3.*X*GS/RPG7
     TUX=R*MS1-C1XY*MS3-C1XX*MS2-C1YY*MS4
     WS 1=Y/RP03
     WS2=Y*(9.*QS+30.*YSQ)/RPQ7
      TUY=8*NS1-01XX*NS3-01XY*NS4-01YY*NS2
      TVZ=Z*(A/RPQ3-3.*(C1XX*PS-5.*C1XY*X*Y+C1YY*QS)/RPO7)
  450 UX(1S)=TUX*XX+TUV*XV+TUZ*XN(K)
      UY(18)=TUX*YX+TUY*YY+TUZ*YN(K)
      UZ(18)=TUX*ZX+TUY*ZY+TUZ*ZN(K)
      GO TO 470
C
        K. COMPUTE INDUSED VELOCITY BY MONOPOLE METHOD
 460 ARP03=A/(RP0**3)
      UX(18)= (XC0-XC)*ARP03
      VY(18)= (YCQ-YC)*ARPQ3
      VZ(18)= (ZCQ-ZC)*ARPQ3
       L. REFLECT OFF BODY POINT IN PLANE OF SYMETRY
 470 GO TO(480,485,490,495,500,505,510,515),IS
 480 V1(J1)=VX(1)
      U2(J1)=UX(1)
      V3(J1)=VX(1)
```



```
V1(J1+1)=VY(1)
      V2(J1+1)=VY(1)
      V3(J1+1)=VY(1)
      V1(J1+2)=VZ(1)
      V2(J1+2)=VZ(1)
      U3(J1+2)=UZ(1)
      1F(SYM) 525,525,481
  481 18=2
              XZ SYMETRY
C
      YCQ=-YCQ
      60 TO 345
  485 IF(SYM-1)517,517,486
C
              XY SYMETRY
  486 IS=3
      Z00=-Z00
      GO TO 345
  490 IS=4
      Y00=-Y00
      GO TO 345
  495 IF(SYM-2)516,516,496
              YZ SYMETRY
  496 IS=5
      XC0=-XC0
      60 TO 345
  500 19=6
      Y00=-Y00
      GO TO 345
  505 18=7
      Z00=-Z00
      60 TO 345
  510 18=8
      Y00=-Y00
      GO TO 345
        M. ADD CONTRIBUTIONS OF ALL REFLECTIONS
  515 V1(J1)=V1(J1)+VX(8)+VX(7)+VX(6)+VX(5)
      V2(J1)=U2(J1)-UX(8)+UX(7)+UX(6)-UX(5)
      V3(J1)=V3(J1)-VX(8)-VX(7)+VX(6)+VX(5)
      V1(J1+1)=V1(J1+1)-VY(8)+VY(7)+VY(6)-VY(5)
      U2(J1+1)=U2(J1+1)+UY(8)+UY(7)+UY(6)+UY(5)
      V3(J1+1)=V3(J1+1)+VY(8)-VY(7)+VY(5)-VY(5)
      V1(J1+2)=V1(J1+2)-V2(8)-V2(7)+V2(6)+V2(5)
      V2(J1+2)=V2(J1+2)+VZ(8)-VZ(7)+VZ(6)-VZ(5)
      U3(J1+2)=U3(J1+2)+UZ(8)+UZ(7)+UZ(6)+UZ(5)
  516 V1(J1)=V1(J1)+VX(4)+VX(3)
      U2(J1)=U2(J1)+UX(4)-UX(3)
      U3(J1)=U3(J1)-UX(4)-UX(3)
      U1(J1+1)=U1(J1+1)+UY(4)-UY(3)
      V2(J1+1)=V2(J1+1)+VY(4)+VY(3)
      U3(J1+1)=U3(J1+1)-UY(4)+UY(3)
      V1(J1+2)=V1(J1+2)-VZ(4)-VZ(3)
      V2(J1+2)=V2(J1+2)-VZ(4)+VZ(3)
      U3(J1+2)=U3(J1+2)+UZ(4)+UZ(3)
  517 01(31)=01(31)+0X(2)
      U2(J1)=U2(J1)-UX(2)
      U3(J1)=U3(J1)+UX(2)
      V1(J1+1)=V1(J1+1)=VY(2)
      U2(J1+1)=U2(J1+1)+UY(2)
      V3(J1+1)=V3(J1+1)-VY(2)
      V1(J1+2)=V1(J1+2)+VZ(2)
      U2(J1+2)=U2(J1+2)-UZ(2)
      U3(J1+2)=U3(J1+2)+UZ(2)
  525 UX1(JQ)=UX1(JQ)+U1(1)*S1(P)
```



```
UY1(J@)=UY1(J@)+U1(2)*S1(P)
   UZ1(J0)=UZ1(J0)+U1(3)*S1(P)
    UX2(JQ)=UX2(JQ)+U2(1)*S2(P)
   UY2(J0)=UY2(J0)+U2(2)*S2(P)
   VZ2(J0)=VZ2(J0)+V2(3)*S2(P)
   UX3(JQ)=UX3(JQ)+U3(1)*S3(P)
   VY3(J0)=VY3(J0)+V3(2)*S3(P)
530 VZ3(J0)=VZ3(J0)+V3(3)*93(P)
     N. END OF LOOP OVER OFF BODY POINTS
585 P=P+1
   K=K+1
   J=J+20
    IF(K-NF )296,296,599
     P. END OF LOOP OVER QUADS
599 H=AP(1BK)*DT
   00.730 l = 1,008P
63 FORMAT(2X,13,3F12.5,9X,4F12.5)
   DX(+)=-(UX1*UX1(+)+UY1*UX2(+)+UZ1*UX3(+))
   DY(1)=-(UX1*UY1(1)+UY1*UY2(1)+UZ1*UY3(1))
730 DZ(1)=-(UX1*UZ1(1)+UY1*UZ2(1)+UZ1*UZ3(1))
    IF(IRK.EQ.5) GO TO 900
    IF(IRK.E0.4) GO TO 800
   DO 750 I=1, NOBP
   XP(+)=XT(+)+DX(+)*H
   VP(1)=YT(1)+DY(1)*H
   ZP(1)=ZT(1)+DZ(1)*H
   SKX(T)=SKX(T)+GM(TRK)*DX(T)
   SKY(1)=SKY(1)+GM(1RK)*DY(1)
750 SKZ(1)=SKZ(1)+GM(1RK)*DZ(1)
    18K = 18K + 1
   GO TO 98
800 H=DT
   DO 830 1=1, NOSP
   DX(1)=-(UX1*UX1(1)+UY1*UX2(1)+UZ1*UX3(1))
   DY(1)=-(UX1*UY1(1)+UY1*UY2(1)+UZ1*UY3(1))
   DZ(1)=-(UX1*UZ1(1)+UY1*UZ2(1)+UZ1*UZ3(1))
   XP(1)=XT(1)+H*DX(1)/6.+SKX(1)*H
   XT(1)=XP(1)
   YP(1)=YT(1)+H*DY(1)/6.+SKY(1)*H
   YT(1)=YP(1)
   ZP(1)=ZT(1)+H*DZ(1)/6.+SKZ(1)*H
   ZT(1)=ZP(1)
   SKX(1)=0.
   SKY(1) = 0.
830 \text{ SKZ}(1) = 0.
    18K = 5
   GO TO 98
900 IRK = 1
    DO 905 I=1.NOBP
    DSQ=DX(1)**2+BY(1)**2+DZ(1)**2
    CP(T)=1.-DS0/US0
905 CONTINUE
    WRITE(6,61) | 1TC
61 FORMAT(6HO STEP, 14/)
   WRITE(6,62)
 62 FORMAT(3X,4HLINE,5X,1HX,11X,1HY,11X,1HZ,20X,2HVX,10X,2HVY,
           10X,2HUZ,10X,2HCP)
   WRITE(6,63) (1,XP(1),YP(1),ZP(1),DX(1),DY(1),DZ(1),CP(1),I=1,NOBP)
    WRITE(16) ( XP(1), YP(1), ZP(1), I=1, NOBP )
    IF(ITC.EQ.NST) GO TO 910
    1T0=1T0+1
    GO TO 599
```



```
910 IF(IEND.EQ.0 ) GO TO 83
   REWIND 03
   REWIND 04
   ENDFILE 16
   REWIND 16
    STOP 6
    END
   FUNCTION SQ2F(X1, X2, Y1, Y2, Z1, Z2)
   X=X1-X2
   Y=Y1-Y2
   Z=Z1-Z2
   RS=Z**2+Y**2+X**2
   R=888(X)+888(Y)+888(Z)+ 1.0E-20
   R=.3422*(R+(RS+RS)/R)
   R= R+RS/R
   SQ2F= .25*R+RS/R
   RETURN
   END
```



APPENDIX VII - XYZPF SECTION PF7

```
PROGRAM PFP7(TAPE7, INPUT=128, OUTPUT=128, TAPE5=INPUT, TAPE17,
     1TAPE6=OUTPUT, TAPEO3, TAPEO4, TAPE3=TAPEO3, TAPE4=TAPEO4)
Ū
C
      XYZ POTENTIAL FLOW PROGRAM | VERSION 4 AND VERSION 5 | SECTION 7
      COMPUTES VELOCITIES AND PRESSURE COEFFICIENTS FOR
C
      ON BODY STREAMLINES
                X(658), Y(658), Z(658), XN(650), YN(650)
      COMMON
     1.ZN(650), UX1(650), UY1(650), UZ1(650), UX2(650), UY2(650)
     2, UZ2(650), UX3(650), UY3(650), UZ3(650), XC1(658), YC1(658)
     3,XC2(658),YC2(658),XC3(658),XC4(658),YC4(658)
     4X3(658), Y3(658), Z3(658), X4(658), Y4(658), Z4(658)
     DIMENSION XL(150), YL(150), ZL(150), UX(150), UY(150), UZ(150),
     10P(150), GK1(150), GK2(150), H2(150), STML(150), UASS(150), NOURD(150)
     5,DMX(650),PROB(15),YC3(658),SF(5),XCR(5),YCR(5)
     7MSP(50), WS(220) , XST(50), YST(50), ZST(50)
      EQUITURLENCE (WS(201), NP), (YC3, YC2)
      READ(03)(PROB(1), I=1, 15)
     RERD(03)(WS(1), I=1,220)
      READ(03)(X(1),Y(1),Z(1),XN(1),YN(1),ZN(1),
     1SK (P. (=1, NP.)
     READ(03)SKIP
      IVER =WS(220)
     WRITE(6,5) IVER
   5 FORMAT(46HOXYZ POTENTIAL FLOW PROGRAM SECTION 7, VERSION ,12)
     IF (IVER.E0.5) READ(03) SKIP
     READ(03)SKIP
     READ(03)SKIP
     READ(03)SKIP
     READ(83)(UX1(1), UV1(1), UZ1(1), I=1, NP)
     READ(03)(UX2(1),UV2(1),UZ2(1),I=1,NP)
     READ(03)(UX3(1),UY3(1),UZ3(1),I=1,NP)
     REWIND 03
     NB=(NP+11)/12
     DO 80 1=1,NB
     1FN=1*12
     1S=!FN-11
     READ(04) Q,(XC1(J),YC1(J),XC2(J),
     1902(J),XC3(J),XC4(J),9C4(J),X3(J),93(J),
    2Z3(J), X4(J), Y4(J), Z4(J), (SKIP, K=1,7), U=IS, IFN )
     IF(NQ.NE.18) 60 TO 450
  80 CONTINUE
     REWIND 04
     DO 90 L=1,NP
     D1=(XC1(1)**2+YC1(1)**2)*1.01
     D2=(XC2(+)**2+YC2(+)**2)*1.01
     D3=(XC3(+)**2+YC3(+)**2)*1.01
     D4=(XC4(1)**2+YC4(1)**2)*1.01
  90 DMX(I)=AMAX1(D1,D2,D3,D4)
  11 FORMAT(3F12.4,314,F12.4)
  12 FORMAT(3F12.4, 14)
     MID=75
 100 READ(5,11) UXI, UYI, UZI, NLIN, MAXU, IWRITE, AMACH
     IF (E0F(5).NE.O.) NLIN=0.
     MXJ=MAXJ
     IF ( MAXJ .LE. O .OR. MAXJ .GT. NP/2) MAXJ = NP/2
     UXAM-OIM=UMIM
     MAXJ=MID+MAXJ
     IF (MAXJ.GT.MID*2) MAXJ=MID*2
```



```
IF ( MINJ .LT.1) MINJ = 1
     WRITE(7 ) NLIN
     WRITE(17) NLIN. VXI. VYI. VZI
      IF(NLIN.LE.0) GO TO 550
     WRITE(6,30) = (PROB(1), I=1,15)
      WRITE(6,34) UXI,UYI,UZI,NLIN,MXJ,IWRITE,AMACH
   34 FORMAT(34HOON BODY STREAMLINES - INPUT DATA /6H VXI =,F10.5/
     16H UYI =,F10.5/6H UZI =,F10.5/6H NLIN=, 110/
     2 6H JMAX=, [10, /, SH [WRITE=, [10, /, 9H MACH NO=, F10.5)
     WRITE(6,38)
   38 FORMAT(27HOSTREAMLINE STARTING POINTS/5H LINE,11X,1HX,12X,1HY,
     1 12X, 1HZ, 10X, 3HNSP)
     LIM=MLIM
      DO 45 I=1,LIN
     READ(5,12) XST(1), YST(1), ZST(1), NSP(1)
      IF (EGF(5),EQ.O.) GO TO 45
     NL 1 N=1-1
     WRITE(6,42) MLIN,LIN
  42 FORMAT(1H0, 15, 28H STREAMLINES SPECIFIED NOT
      IF(NLIN.LE.O) GO TO 550
     GO TO 48
  46 FORMAT(1X, 13, 2X, 3F13.5, 19)
  48 CONTINUE
     USQ=UX1**2+UV1**2+UZ1**2
     IF (AMACH .EQ. 0.) 60 TO 1130
C *** COMPUTE CRITICAL MACH NO.
     USD = 0.
     DO 1100 I=1, NP
     US = (UX)*UX1(1)+UY)*UX2(1)+UZ)*UX3(1))**2 +
           (UX1*UP1(1)+UP1*UP2(1)+UZ1*UP3(1))**2 +
           (UXT*UZ1(1)+UYT*UZ2(1)+UZ1*UZ3(1))**2
     IF (US .GT. USD) USD = US
 1100 CONTINUE
     U = SQRT(USD/VSQ)
     CMNA = 1.70
     DO 1110 I=1,3
     CMNB = (((CMNB**2+5))/6.)**1.75)/U
     CMNC = (((CMNB**2+5.)/6.)**1.75)/U
 1110 CMMA = (CMMA*CMMC-CMMB**2)/(CMMA+CMMC-2.*CMMB)
     WRITE(6,1120) CMNA
 1120 FORMAT(21H CRITICAL MACH NO. =,F5.3)
 1130 CONTINUE
     START LOOP OVER STREAMLINES
     DO 400 LL=1, MLIN
     DIRT=1.
  101 31=1
     RF=1.
     UX(MID)=0.
     UY(MID)=0.
     UZ(MID)=0.
     CP(MID)=0.
     H2(MID)=1.
     GK1(M1D)=0
     GK2(MID)=0.
     STML(MID)=0.
  102 NO=NSP(LL)
     LNO=NO
     XL(MID)=XST(LL)
     YE(MID)=VST(EE)
     ZL(MID)=ZST(LL)
     J=MID
```



```
JL=J
      SEPARATE CALCULATION OF SECOND
0
      POINT FROM MAIN LOOP
     XLT=(XL(J)-X(NQ))*X3(NQ)+(YL(J)-Y(NQ))*Y3(NQ)
                               +(ZL(J)-Z(N0))*Z3(N0)
      YLT=(XL(J)-X(N0))*X4(N0)+(YL(J)-Y(N0))*Y4(N0)
                               +(ZL(J)-Z(NQ))*Z4(NO)
     XL(J)=XLT*X3(NQ)+YLT*X4(NQ)+X(NQ)
      YE(J)=XET*Y3(N0)+YET*Y4(N0)+Y(N0)
      ZL(J)=XLT*Z3(NQ)+YLT*Z4(NQ)+Z(NQ)
  105 \text{ IQT=MOD(NQ,4)} + 1
      GO TO (630,600,610,620) TOT
 600 NR=NO+1
     NU=N0+2
      GO TO 107
 510 NR=N0+2
      NU=NO-1
      GO TO 107
 620 NR=N0-2
      NU=N0+1
      GO TO 107
 630 NR=NQ-1
      NU=N0-2
  107 UXQ=-(UX1*UX1(NQ)+UY1*UX2(NQ)+UZ1*UX3(NQ))
      UYG=-(UXT*UY1(NG)+UYT*UY2(NG)+UZT*UY3(NG))
      UZ0=-(UX1*UZ1(N0)+UY1*UZ2(N0)+UZ1*UZ3(N0))
      UXR=-(UX1*UX1(NR)+UY1*UX2(NR)+UZ1*UX3(NR))
      UYR=-(UX1*UY1(NR)+UY1*UY2(NR)+UZ1*UY3(NR))
      UZR=-(UX1*UZ1(NR)+UY1*UZ2(NR)+UZ1*UZ3(NR))
      UXU=-(UX F*UX 1(NU )+UY F*UX2(NU )+UZ F*UX3(NU ))
      UYU=-(UX1*UY1(NU)+UY1*UY2(NU)+UZ1*UY3(NU))
      UZU=-(UX:1*UZ:1(NU:)+UY:1*UZ2(NU:)+UZ:1*UZ3(NU:)>
C
      TRANSFORM VELOCITIES TO QUAD SYSTEM
      UQ=UXQ*X3(NQ)+UYQ*Y3(NQ)+UZQ*Z3(NQ)
      VQ=UX0*X4(N0)+UY0*Y4(N0)+UZ0*Z4(N0)
      CSR=1./(XN(NQ)*XN(NR)+YN(NQ)*YN(NR)+ZN(NQ)*ZN(NR))
      UT=UXR*X3(NR)+UYR*Y3(NR)+UZR*Z3(NR)
      UT=(UXB*X4(NB)+UYB*Y4(NB)+UZB*Z4(NB))*CSB
      XXE=
            (X3(NR)*X3(N0)+Y3(NR)*Y3(N0)+Z3(NR)*Z3(N0))
      XYR=
             (X4(NR)*X3(N0)+Y4(NR)*Y3(N0)+Z4(NR)*Z3(N0))
      UR=UT*XXR+UT*XYR
             (X3(NR)*X4(N0)+Y3(NR)*Y4(N0)+Z3(NR)*Z4(N0))
      YXR=
      YYR=
             (X4(NB)*X4(N0)+Y4(NB)*Y4(N0)+Z4(NB)*Z4(N0))
      UR=UT*YXR+UT*YYR
      UU=UXU*X3(NQ)+UYU*Y3(NQ)+UZU*Z3(NQ)
             (XN(NO)*XN(NU)+YN(NO)*YN(NU)+ZN(NO)*ZN(NU))
      VU=(UXU*X4(NQ)+UYU*Y4(NQ)+UZU*Z4(NQ))/CSU
C
      FIND RELATIVE COORDINATES OF NEIGHBORING QUADS
      XD=X(NR)-X(NO)
      YD=Y(NB)-Y(ND)
      ZD=Z(NR)-Z(NO)
      XT = XD*X3(NR)+YD*Y3(NR)+ZD*Z3(NR)
      YTT=XD*X4(MR)+YD*Y4(MR)+ZD*Z4(MR)
      ZT =XD*XN(N8)+YD*YN(N8)+ZD*ZN(N8)
      YT=(-4*S0RT(YTT**2+ZT**2)+YTT*CSR+YTT)*CSR*, 16666667
      XR=XT*XXR+YT*XYR
      YB=XT*YXB+YT*YYB
      XD=X(NU)-X(NO)
      YD=Y(NU)-Y(NO)
      ZD=Z(NU)-Z(NO)
      XU=XD*X3(N0)+YD*Y3(N0)+ZD*Z3(N0)
      YT=X0*X4(N0)+Y0*Y4(N0)+Z0*Z4(N0)
```



```
ZT=XD*XN(NO)+YD*YN(NO)+ZD*ZN(NO)
      YU=(4, *SQRT(YT**2+ZT**2)+YT/CSU+YT)*, 16666667
      FIND COEFFICIENTS OF VELOCITY FUNCTIONS
C
      DEN=1.7(XR*YU-XU*YR)
      U1=((UR-U0)*YU-(UU-U0)*YR) *DEN
      U2=-((UR-UQ)*XU-(UU-UQ)*XR )*DEN
      V1=((VR-VQ)*YU-(VU-VQ)*YR) *DEN
      V2=-((VR-VQ)*XU-(VU-VQ)*XR )*DEN
      FIND VELOCITY AT STREAMLINE POINT
C
      USL=U0+U1*XLT+U2*YLT
      USL=UQ+U1*XLT+U2*YLT
      UXP=USL*X3(N0)+USL*X4(N0)
      UYP=USL*Y3(NO)+USL*Y4(NO)
      UZP=USL*Z3(NQ)+USL*Z4(NQ)
C
      FIND GEODESIC CURVATURES GK1.GK2
      US00=USL**2+USL**2
      DEN=USOD*SORT(USOD)
      GK 1P=(USL*(USL*U2-USL*U2)-USL*(USL*U1-USL*U1))/DEN
      GK2P=(USL*(USL*U1+USL*U2)-USL*(USL*U1+USL*U2))/DEN
C
      FIND LOCAL STREAM FUNCTION
      CXY=(U1*U0**2-U2*U0**2)/US0B
      CYY=U2-U0*VQ*(U1+V2)/VSQD
      CXX=U2-CYY-V1
      CO=XLT*VO-YLT*UO-CXY*XLT*YLT-CYY*YLT**2-CXX*XLT**2
      FIND STREAM FUNCTION AT CORNER POINTS
C
      XOR(1)=XO1(NO)
      XCR(2)=XC2(NQ)
      XCR(3)=XC3(NO)
      XCB(4)=XC4(NO)
      XCR(5)=XCR(1)
      YCB(1)=YC1(NO)
      YCR(2)=YC2(NO)
      YCR(3)=YC3(NQ)
      YCR(4)=Y64(NQ)
      YCR(5)=YCR(1)
      00 110 N=1,4
  110 SF(H)=00-V0*XCR(H)+U0*YCR(H)+CXY*XCR(H)*YCR(H)+CYY*YCR(H)**2
     1
            +0XX*XCR(N)**2
      SF(5)=SF(1)
      TEST=0
      DO 120 N=1,4
      IF ( SF(N)*SF(N+1) .GE. 0. ) GO TO 120
      XM=(XCR(N)+XCR(N+1))*.5
      YM=(YCR(N)+YCR(N+1))*.5
C
      FIND INTERSECTION WITH SIDE OF OUAD.
      SFM=00-U0*XM+U0*YM+CXY*XM*YM+CYY*YM**2+CXX*XM**2
      AC=2.*(SF(N)-2.*SFM+SF(N+1))
      BC=3, *SF(N)-4, *SFM+SF(N+1)
      IF (AC .EQ. 0)
                      G0 T0 113
      SR=SQRT(BC**2-4,*AC*SF(N))
      TP=(BC+SR)/(2,*AC)
      IF (TP .LE. 1. .AND. TP .GE. 0. ) GO TO 115
      TP=(BC-SR)/(2.*AC)
      GO TO 115
  113 IF (BC .EO. 0 ) GO TO 120
      TP=SF(N)/BC
  115 XNP=(1.-TP)*XCR(N)+TP*XCR(N+1)
      YMP=(1,-TP)*YCB(N)+TP*YCB(N+1)
      TESTP=((XMP-XLT)*UQ+(YMP-YLT)*UQ)*DIRT
      IF (TESTP .LE. TEST) GO TO 120
      TEST=TESTP
      XNT=XNP
```



```
YNT=YNP
     120 CONTINUE
              IF( TEST .EQ. 0) 60 TO 280
             AVERAGE LAST VELOCITY AND CURVATURE
C
             PR*(4XU+(U)XU)=(U)XU
             UY(J)=(UY(J)+UYP)*AF
             UZ(J)=(UZ(J)+UZP)*AF
             GK1(J)=(GK1(J)+GK1P)*8F
             GK2(J)=(GK2(J)+GK2P)*AF
             H2(J)=H2(JL)*(2.-GK1(JL)*(STML(J)-STML(JL)))/(2.+GK1(J)*(
                             STML(U)-STML(UL)))
             CP(J)=1.-(UX(J)**2+UY(J)**2+UZ(J)**2)/USQ
             UABS(J)=SQRT(1.-CP(J))
             COMPUTE VELOCITY AT NEXT POINT
C
             NOUAD(U)=NO
             ال=يال
             1L+L=L
             USL=U0+XNT*U1+YNT*U2
             USL=U0+XNT*U1+YNT*U2
             UX(J)=USL*X3(NQ)+USL*X4(NQ)
             UY(J)=USL*Y3(N0)+VSL*Y4(N0)
             UZ(J)=USL*Z3(N0)+USL*Z4(N0)
C
             COMPUTE GEODESIC CURVATURES
             US00=USL**2+USL**2
             DEM=USQD*SQRT(USQD)
             GK 1(J)=(USL*(USL*U2-USL*U2)-USL*(USL*U1-USL*U1))/DEN
             GK2(J)=(USL*(USL*U1+USL*U2)-USL*(USL*V1+USL*V2))/DEN
             CORD=SORT((XNT-XLT)**2+(YNT-YLT)**2 )*DIRT
             STML(J)=STML(JL)+CORD
C.
             COMPUTE H2
             H2(J)=H2(JL)*(2.-CORD*GK1(JL))/(2.+CORD*GK1(J))
             CP(J)=1.-VSQB/VSQ
             UABS(J)=SQRT(1.-CP(J))
             AF= .5
             LNO=NO
             XL(J)=XNT*X3(NQ)+YNT*X4(NQ)+X(NQ)
             ( 0H) P+*TMP+( 0H) P*TMX=( U) P+TMX=( U) P+TMX=( U) P+TMP+( U
             ZE(J)=XNT*Z3(N9)+YNT*Z4(N0)+Z(N0)
             IF ( J .LE. MINJ .OR. J .GE. MAXJ )
                                                                                                    - 60 TO 280
C
             FIND NEXT OURD.
             1 = 1
    250 NQ=1
             IF(1.EQ.LNQ) GO TO 280
             TEST=(XL(J)-X(1))**2+(YL(J)-Y(1))**2+
           1(ZL(J)-Z(1))**2-DMX(1)
              IF(TEST.GT.O.) GO TO 280
             DS1=(XC1(1)-XC2(1))**2+(YC1(1)-YC2(1))**2
             DS2=(XC2(1)-XC3(1))**2+(YC2(1)-YC3(1))**2
             DS3=(XC3(1)-XC4(1))**2+(YC3(1)-YC4(1))**2
             DS4=(XC4(1)-XC1(1))**2+(YC4(1)-YC1(1))**2
             XLT=(XL(J)-X(T))*X3(T)+(YL(J)-Y(T))*Y3(T)+
            1(2L(J)-Z(1))*Z3(1)
             YET=(XE(J)-X(T))*X4(T)+(YE(J)-Y(T))*Y4(T)+
           1(ZE(J)-Z(I))*Z4(I)
             ZLT=(XL(J)-X(T))*XN(T)+(YL(J)-Y(T))*YN(T)+
           1(ZL(J)-Z(1))*ZN(1)
             ZSQ=ZLT**2
             TEST=ZSQ-.1*DMX(1)
              IF(TEST.GT.O.) GO TO 280
             RC1=SORT(ZS0+(XLT-XC1(L))**2+(YLT-YC1(L))
              RC2=SQRT(ZSQ+(XLT-XC2(1))**2+(YLT-YC2(1))**2)
```



```
RC3=SQRT(ZSQ+(XLT-XC3(1))**2+(YLT-YC3(1))**2)
    RC4=SQRT(ZSQ+(XLT-XC4(1))**2+(YLT-YC4(1))**2)
    TEST= ((RC1+RC2)**2)-DS1 *1.21
    IF(TEST.LT.0.) GO TO 105
    TEST= ((RC2+RC3)**2)-DS2 *1.21
    IF(TEST.LT.0.) 60 TO 105
    TEST= ((RC3+RC4)**2)-BS3 *1.21
    IF(TEST.LT.O.) GO TO 105
    TEST= ((RC4+RC1)**2)-DS4 *1.21
    IF(TEST.LT.0.) 60 TO 105
280 1=1+1
    IF(1.LE.NP) GO TO 250
282 IF (DIRT .LT. 0.) 60 TO 285
    DIRT=-1.
    1 -= 1
    U=XAMU
    GO TO 102
285 JMIN=J
    SS=STML(JMIN)
    DO 290 J=JMIN,JMAX
290 STML(J)=STML(J)-SS
    JMN=JM1N+1
    JMX=JMAX-2
    RF=1.
    L=JMN
    WRITE(6,30)(PROB(1),1=1,15)
30 FORMAT(1H1, 15A4)
    WRITE(6,20)UXI,UYI,UZI
20 FORMAT( 18H0 ONSET FLOW, VXI=,F6.3,2X,4HVYI=,F6.3,2X,4HVZI=,F6.3)
    WRITE(6,50) LE,NSP(LL),XST(LL),YST(LL),ZST(LL)
50 FORMATK11HO LINE NO. ,12,31H PASSING THROUGH QUADRILATERAL ,13,
           28H WITH STARTING POINT,
                                       X=,F12.5,2X,2HY=,F12.5,2X,
   1
           2HZ=.F12.5 //)
   IF (JMIN.LE.MINJ .OR. JMAX.GE.MAXJ) WRITE(6,65)
65 FORMAT(35H PROBABLE ERROR - LINE IS VERY LONG)
    DO 330 J=JMN,JMX
    IF ( (STML(J+2)-STML(L-1)).LT, 8.*(STML(J+1)-STML (L)))    G0 T0 320
    WRITE(6,310) XE(E),YE(E),ZE(E),XE(U+1),YE(U+1),ZE(U+1)
310 FORMAT(14H POINT DELETED , 10X,3F12.5,10X,3F12.5)
    STML(L)=(AF*STML(L)+STML(J+1))/(AF+1.)
    XL(L)=(AF*XL(L)+XL(J+1))/(AF+1.)
    YL(L)=(AF*YL(L)+YL(J+1))/(AF+1.)
    ZL(L)=(AF*ZL(L)+ZL(J+1))/(AF+1.)
    UX(L)=(AF*UX(L)+UX(J+1))/(AF+1.)
    UY(L)=(8F*UY(L)+UY(U+1))/(8F+1.)
    UZ(E)=(AF*UZ(E)+UZ(J+1))/(AF+1.)
    GK1(L)=(AF*GK1(L)+GK1(J+1))/(AF+1.)
    GK2(L)=(AF*GK2(L)+GK2(J+1))/(AF+1.)
    H2(L)=(AF*H2(L)+H2(J+1))/(AF+1.)
    CP(L)=1.-(UX(L)**2+UY(L)**2+UZ(L)**2)/US0
    UABS(L)=SORT(1,-CP(L))
    AF=AF+1.
    GO TO 330
320 RF=1.
    L=L+1
    K=J+1
    STML(L)=STML(K)
    XL(L)=XL(K)
    YL(E)=YL(K)
    ZL(E)=ZL(K)
    UX(L)=UX(K)
    UY(L)=UY(K)
```



```
UZ(L)=UZ(K)
      GK1(L)=GK1(K)
      GK2(L)=GK2(K)
      H2(L)=H2(K)
      CP(L)=CP(K)
      UABS(L)=UABS(K)
      NOUAD(L)=NOUAD(K)
  330 CONTINUE
      L=L+1
      STML(L)=STML(JMAX)
      XL(L)=XL(JMAX)
      AF(F)=AF(GWBX)
      ZL(L)=ZL(JM8X)
      UX(L)=UX(JMAX)
      UY(L)=UY(JMAX)
      UZ(L)=UZ(JMRX)
      GK 1(L)=GK 1(JMAX)
      GK2(L)=GK2(JMAX)
      H2(L)=H2(JMAX)
      CP(L)=CP(JMAX)
      UABS(L)=UABS(JMAX)
      JMAX=L
      NOURD (JMAX )=NOURD (JMAX-1)
      NOURD(JMIN)=NOURD(JMIN+1)
      WRITE(6,51)
   51 FORMAT(4H0 | 1,6X,1HX,9X,1HY
     19X,1HZ,09X,2HVX,8X,2HVY,8X,2HVZ,09X,
     22HCP, 8X,2HK1, 8X,2HK2, 8X,2HH2,8X,2HSL,8X,1HU,9X,1HP)
      IF (AMACH .EQ. 0.) GOTO 1160
C *** COMPUTE COMPRESSIBILITY CORRECTION
      DO 1150 J=JMIN,JMAX
      USD = (UX(J)**2+UY(J)**2+UZ(J)**2)/US0
      USDA = USD
      SM = AMACH**2
      00 1140 1=1,3
      R = (1.+.2*SM*(1.-USDA))
      IF (R, LT, .000001) R = .000001
      USD8 = USD/R**2.5
      B = (1.+.2*SM*(1.-USDB))
      IF (R .LT. .000001) R = .000001
      USDC = USD/R**2.5
 1140 USDA = (USDC*USDA-USDB**2)/(USDC+USDA-2.*USDB)
      B = (1. + .2*SM*(1. -USDA))
      IF(R,LT,.000001)R = .000001
      R = R**1.25
      UX(J) = UX(J)/R
      AV(J) = UV(J)/B
      UZ(J) = UZ(J)/R
      UABS(J) = SQRT(USDA)
 1150 \text{ CP(J)} = (R**2.8-1.)/(.7*SM)
 1160 CONTINUE
      K=0
      DO 53 I=JMIN, JMAX
      K=K+1
   53 WRITE(6,60) K,XL(1),YL(1),ZL(1),UX(1),UY(1),UZ(1),CP(1),
                     GK1(1), GK2(1), H2(1), STML(1), URBS(1), MGURD(1)
   60 FORMAT(1X, 13, 3F 10.5, 1X, 3F 10.5, 1X, 6F 10.5, 16)
    8 FORMAT(3F12.5)
      WRITE(17) K, (XL(I), YL(I), ZL(I), NOUAD(I), I=JMIN, JMAX
        IMPITE LE. 0
                          --
                                 WRITE SL, U, H2, K2
        INFITE .GE. 2
                                 NRITE X,Y,Z,CP
        INPITE .EQ. 1
                                 WRITE SL, U, H2, K2 AND X, Y, Z, CP
```

C

0



```
IF (IWRITE.GT. 1) GO TO 340
    WRITE(7) K, (STML(1), UABS(1), H2(1), GK2(1), I=JMIN, JMAX)
340 IF (IWRITE.LT.1) GO TO 400
    URITE(7)
              K, (XL(I),YL(I),ZL(I),CP(I), I=JMIN,JMAX)
    GO TO 400
300 WRITE(6,50) NSP(LL)
    WRITE(6,65)
    GO TO 282
400 CONTINUE
    GO TO 100
    READ NEXT SET OF STREAMLINES
450 WRITE(6,451)18,NQ
451 FORMAT(14H TAPE 04 ERROR, 214)
550 ENDFILE 7
   REWIND 7
   ENDFILE 17
   REWIND 17
   REWIND 04
    STOP 7
    END
```



APPENDIX VIII - TRIAXIAL ELLIPSOID INPUT FILE

| SAMPLE PROBLEM | | | _ | _ | _ | _ | | | | | |
|----------------------------|-----------------------------|---------------------|--------|----------|---|--------|---|----------------------|-------|---------|--|
| 280 5 150 15 1,00000 | 0 150 3 .00000 | 0 1 00000. | 0 | 0 | 0 | 0 | 0 | 0 0 .00000 | . 000 | .600 .0 | |
| . 97861 | .00000 | . 10286 | 1 | 2 | 1 | 0 | | .00000 | | | |
| . 90789 . 82350 | . 00000 . 00000 | . 20960 . 28359 | 1 | 3 4 | 1 | 0 | | .00000 .00000 | | | |
| . 71583 | . 00000 | . 349 14 | 1 | 5 | 1 | 0 | | .00000 | | | |
| . 62478 . 52537 | . 00000 . 00000 | .39040 .42544 | 1 | 6 7 | 1 | 0 | | . 00000 . 00000 | | | |
| .44721 | .00000 | .44721 | 1 | 8 | 1 | 0 | | .00000 | | | |
| . 375 30 . 29822 | . 00000 . 00000 | . 45345 . 47725 | 1 | 9 10 | 1 | 0 | | . 00000 . 00000 | | | |
| . 23692 | .00000 | .48576 | 1 | 11 | 1 | 0 | | .00000 | | | |
| . 15957 . 11467 | . 00000 00000 . | . 49275 . 49670 | 1 | 12 13 | 1 | 0 | | . 00000 . 00000 | | | |
| .05248 | . 00000 | .49931 | 1 | 14 | 1 | 0 | | .00000 | | | |
| .00000 .99875 | . 00000 . 10000 | . 50000 . 00000 | 1 2 | 15 1 | 1 | 0 | | . 00000 . 00000 | | | |
| .97739 | . 10000 | . 10273 | 2 | 2 | 1 | 0 | | .00000 | | | |
| .90676 .82257 | . 10000 . 1 0 000 | . 20934 . 28323 | 2 | 3 | 1 | 0 | | . 00000 . 00000 | | | |
| .71494 | . 10000 | . 20020 . 34870 | 2 | 5 | 1 | 0 | | .00000 | | | |
| . 52399 . 52471 | . 10000 . 10000 | .38991 .42490 | 2 | 6 ? | 1 | 0 | | . 00000 . 00000 | | | |
| . 44565 | . 10000 | .44665 | 2 | Ś | 1 | 0 | | .00000 | | | |
| . 37483 . 29785 | . 10000 . 10000 | . 46287 . 47665 | 2 | 9 10 | 1 | 0 | | .00000 | | | |
| . 23663 | . 10000 | . 485 16 | 2 | 11 | 1 | Ū | | . 00000 | | | |
| . 16946 . 11453 | . 10000 . 10000 | . 492 13 . 49608 | 2 | 12 13 | 1 | 0 | | .00000 .00000 | | | |
| . 05241 | . 10000 | . 49859 | 2 | 14 | 1 | Ü | | . 00000 | | | |
| .00000 .99499 | . 10000 . 20000 | . 49937 . 00000 | 2 3 | 15 1 | 1 | 0 | | .00000 .00000 | | | |
| .97371 | . 20000 | . 10234 | 3 | 2 | 1 | Ō | | .00000 | | | |
| . 90334 . 81947 | . 20000 . 20000 | . 20855 . 28217 | 3 3 | 3 4 | 1 | 0 | | .00000 .00000 | | | |
| .71225 | . 20000 | . 34739 | 3 | 5 | 1 | 0 | | .00000 | | | |
| . 52 154 . 52274 | . 20000 . 20090 | . 38845 . 42330 | 3 | 5 7 | 1 | 0 | | . 00000 . 00000 | | | |
| .44497 | . 20000 | .44497 | 3 | 8 | 1 | Ō | | .00000 | | | |
| . 37342 . 29672 | . 20000 . 20000 | .45113 .47486 | 3 | g 10 | 1 | 0 | | . 00000 . 00000 | | | |
| . 23574 | . 20000 | .48333 | 3 | 11 | 1 | 0 | | .00000 | | | |
| . 16882 . 11410 | . 20000 . 20000 | . 49028 . 49421 | 3 | 12 13 | 1 | 0 0 | | . 00000 . 00000 | | | |
| . 05222 | . 20000 | .49581 | 3 | 14 | 1 | 0 | | .09090 | | | |
| .00000 .98869 | . 20000 . 30000 | . 49749 . 00000 | 3 4 | 15 1 | 1 | 0 | | .00000 .00000 | | | |
| . 96754 | . 30000 | . 10 159 | 4 | 2 | 1 | 0 | | . 00899 | | | |
| . 89762 . 81428 | .30008 .0000 | . 20723 . 28038 | 4 | 3 4 | 1 | 0 Ú | | .00000 .00000 | | | |
| . 70774 | .30000 | .34519 | 4 | 5 | 1 | 0 | | .00000 | | | |
| .61771 .51943 | . 30000 . 30000 | . 38599 . 42852 | 4 4 | 6 7 | 1 | 0 | | . 00000 . 00000 | | | |
| .44215 | .30000 | . 442 15 | 4 | 8 | 1 | Û | | .00000 | | | |
| . 37 105 . 29484 | . 30000 . 30000 | . 45821 . 47185 | 4 | 9 10 | 1 | 0 | | . 00000 . 00000 . | | | |
| . 23424 . 16775 | . 30000 . 30000 | .48027 | 4 | 11 | 1 | 0 | | .00000 | | | |
| . 10773 | . 30000 | . 487 18 | 4 | 12 | 1 | 0 | | .00000 | | | |



| .11338 .05189 .00000 .97980 .95884 .89955 .80696 .70137 .61215 .51476 .43818 .36771 .29219 .23214 .16624 .11235 .05142 .00000 .97980 .95884 .89955 .80596 .70137 .61215 .51476 .43818 .36771 .29219 .23214 .16624 .11236 .9696 .70137 .61215 .51476 .43818 .36771 .29219 .23214 .16624 .11236 .00000 .96825 .94754 .87906 .79745 .69310 .60434 .50569 .43301 .36338 .28875 .2940 .16428 .11103 .05081 .00000 .95394 .9354 .86507 .78566 .59500 .50117 .42562 .35801 .28448 .22601 .16185 .10939 |
|--|
| .30000 .30000 .30000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .40000 .50000 |
| .49108 .49366 .49434 .00000 .10078 .20537 .27786 .34208 .38251 .41684 .43818 .45409 .46761 .47595 .48280 .48667 .48922 .48990 .00000 .10078 .20537 .27786 .34208 .38251 .41684 .43818 .45409 .40000 .10078 .20537 .27786 .34208 .38251 .41684 .43818 .45409 .46761 .47595 .48920 .00000 .09959 .20295 .27458 .33805 .37801 .41193 .43301 .44874 .46209 .47034 .47710 .48093 .48346 .48412 .00000 .09812 .19995 .27458 .38365 .37242 .49539 .47034 .47710 .48093 .48346 .48412 .00000 .09812 .19995 .27458 .37242 .49539 .47035 .47382 |
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| 4512345573901234551232222222222222222222222222222222 |
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| .05006 .00000 .93675 .91671 .85047 .77150 .67056 .58526 .49214 .41893 .35156 .27936 .22194 .15894 .10742 .04916 .00000 .91652 .89691 .83210 .75484 .65607 .57262 .48151 .40988 .34397 .27332 .21714 .15550 .10510 .00000 .91552 .21714 .15550 .10510 .00000 .91552 .21714 .15550 .10510 .00000 .91552 .21714 .15550 .10510 .00000 .91552 .21714 .15550 .10510 .04810 .04810 .04810 .04810 .04810 .04810 .04810 .04810 .04810 .04810 .05988 .34397 .27332 .21714 .15550 .10510 .04810 .04687 .04687 .04687 .04687 .04687 .04687 .04687 |
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| .60000 .7 |
| .47531 .47697 .00000 .09635 .19635 .32705 .36571 .39853 .41893 .43414 .44706 .45504 .46158 .46529 .46773 .46837 .00000 .09427 .19210 .25991 .31999 .35781 .48922 .40988 .42476 .43741 .45161 .45523 .45763 .45763 .45926 .00000 .09427 .19210 .25991 .31999 .35781 .45926 .00000 .09427 .19210 .25991 .31999 .35781 .45763 .4 |
| 889999999999999999900000000000000000000 |
| 14 15 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 1 2 3 4 5 6 7 8 9 10 11 12 13 14 |
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| .00000 .86603 .84750 .78626 .71326 .61993 .54107 .45498 .38730 .32502 .25826 .20518 .14694 .09931 .04545 .00000 .83516 .81730 .75824 .68784 .59784 .59784 .59784 .59784 .59787 .43877 .37350 .31343 .24906 .19787 .14170 .09577 .04383 .00000 .78289 .72631 .65888 .57267 .49982 .42030 .35777 .30024 .23857 .18954 .13573 .09174 .04198 .00000 .78289 .72531 .65888 .57267 .4982 .42030 .35777 .30024 .23857 .4982 .42030 .72531 .65888 .57267 .49982 .42030 .35777 .30024 .23857 .49982 .42030 .35777 .30024 .33577 .49982 .42030 .78289 .72531 .65888 .57267 .49982 .42030 .35777 .30024 .33577 .49982 .42030 .35777 .49982 .42030 .35777 .49982 .42030 .30000 .300 |
|--|
| .90000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.10000 |
| .44651 .00000 .08908 .18152 .24559 .30236 .33810 .36844 .38730 .40136 .41331 .42068 .42673 .43016 .43242 .43301 .00000 .17505 .23684 .29159 .32605 .35531 .37350 .38706 .39858 .40559 .41153 .41701 .41758 .20000 .08228 .16768 .22687 .27931 .31232 .34035 .35777 .37076 .38180 .39455 .40000 .08228 .16768 .22687 .27931 .31232 .34035 .39736 .3 |
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| 15 1 2 3 4 5 6 7 8 9 10 11 2 3 4 5 6 7 8 9 10 |
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| .75993 .74368 .68994 .62588 .54399 .47479 .39925 .33985 .28520 .22663 .18005 .12894 .08714 .69887 .64836 .58817 .51121 .44618 .37519 .31937 .26802 .21297 .16920 .12117 .08189 .03748 .00005 .66144 .64729 .60051 .54476 .47348 .41325 .25800 .24824 .19725 .15671 .11222 .07585 .03471 .00000 .58717 .54473 .449416 .42950 .37487 .31522 .26833 .27580 .29580 .24824 .19725 .15671 .11222 .07585 .03471 .00000 .58717 .54473 .49416 .42950 .37487 .31522 .26833 .25838 .2518 .17893 .17893 .26800 .58717 .54473 .49416 .42950 .37487 .31522 .26833 .25838 .25838 .25838 .25838 .26838 .2 |
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| .00000 .07816 .15928 .21551 .26532 .29668 .32330 .33985 .35219 .36268 .37946 .37946 .37944 .37997 .00000 .07345 .14969 .20252 .24933 .27880 .30382 .31937 .34082 .34690 .35189 .3558 .35707 .00000 .06803 .13864 .18758 .23938 .23 |
| 17 17 17 17 17 17 17 17 17 17 17 17 17 1 |
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|--------------------|--------------------|----------|----------------|--------|--------|--------------------|
| .59717 .54473 | 1.60000 1.60000 | | 21 2 21 3 | 5 5 | 0 | .00000 |
| . 494 16 | 1.60000 | | 21 4 | 5 | 0 | .00000 00000 |
| .42950 | 1.60000 | | 21 5 | 5 | 0 | .00000 |
| .37487 | 1.60000 | | 21 6 | 5 | O O | . 00000 |
| .31522 | 1.60000 | | 21 7 | 5 | ō | .00000 |
| .26833 | 1.60000 | | 21 8 | 5 | 0 | .00000 |
| . 225 18 | 1.60000 | | 21 9 | 5 | 0 | .00000 |
| . 17893 | 1.60000 | | 21 10 | 5 | 0 | . 00000 |
| . 14215 | 1.60000 | | 21 11 | 5 | 0 | .00000 |
| . 10 180 | 1.60000 | | 21 12 | 5 | 0 | .00000 |
| .06880 .03149 | 1.50000 1.50000 | | 21 13 21 14 | 5 5 | 0 | . 00000 . 00000 |
| .00000 | 1.60000 | | 21 15 | 5 | 0 | . 00000 |
| .52678 | 1.70000 | | 22 1 | 5 | Ö | .00000 |
| .51552 | 1.70000 | | 22 2 | 5 | 0 | . 00000 |
| .47826 | 1.70000 | | 22 3 | 5 | 0 | .00000 |
| . 43386 | 1.70000 | | 22 4 | 5 | 0 | . 00000 |
| .37709 | 1.70000 | | 22 5 | 5 | 0 | .00000 |
| .32912 .27676 | 1.70000 1.70000 | | 22 6 22 7 | 5 5 | 0 | . 08860 . 08860 |
| .23558 | 1.70000 | | 22 8 | 5 | 0 | . 00000 |
| . 19778 | 1.70000 | | 22 9 | 5 | 0 | . 00000 |
| . 15710 | 1.70000 | | 22 10 | 5 | Ō | . 00000 |
| . 12481 | 1.70000 | . 25589 | 22 11 | 5 | 0 | . 00000 |
| . 09938 | 1.70000 | | 22 12 | 5 | 0 | . 00000 |
| .05041 | 1.70000 | | 22 13 | 5 | 0 | . 00000 |
| .02765 | 1.70000 | | 22 14 | 5 | 0 | .00000 |
| . 00000 . 43589 | 1,70000 1,80000 | | 22 15 23 1 | 5 5 | 0 | . 00000 . 00000 |
| .42657 | 1.80000 | | 23 1 23 2 | 5 | Ü | . 00000 |
| .39574 | 1.80000 | | 23 3 | 5 | 0 | . 00868 |
| .35900 | 1.80000 | | 23 4 | 5 | ō | .00000 |
| .31202 | 1.80000 | . 152 18 | 23 5 | 5 | Ū | . 000000 |
| . 27233 | 1.80000 | | 23 6 | 5 | 0 | . 60080 |
| .22900 | 1.80000 | | 23 7 | 5 | 0 | . 00000 |
| . 19494 | 1.80000 | | 23 8 | 5 | 0 | .00000 |
| . 16359 . 12999 | 1.80000 1.80000 | | 23 9 23 10 | 5 5 | 0 | . 00000 00000 . |
| . 10327 | 1.80000 | | 23 10 23 11 | 5 | 0 | . 00000 |
| .07396 | 1.80000 | | 23 12 | 5 | Ü | . 00000 |
| .04998 | 1.80000 | | 23 13 | 5 | Ō | .00000 |
| .02288 | 1.80000 | . 2 1764 | 23 14 | 5 | Ū | . 00000 |
| .00000 | 1.80000 | | 23 15 | 5 | 0 | . 00000 |
| .31225 | 1.90000 | | 24 1 | 5 | 0 | .00000 |
| .30557 .28349 | 1.90000 1.90000 | | 24 2 24 3 | 5 5 | 0 | . 00000 . 00000 |
| . 25717 | 1.90000 | | 24 3 24 4 | 5 | 0 | . 00000 |
| .22352 | 1.90000 | | 24 5 | 5 | Ü | .00000 |
| . 19509 | 1.90000 | | 24 6 | 5 | 0 | . 00000 |
| . 16405 | 1.90000 | . 13284 | 24 7 | 5 | (j | . 00000 |
| . 13964 | 1.90000 | | 24 8 | 5 | Ü | .00000 |
| .11719 | 1.90000 | | 24 9 | 5 | 0 | .00000 |
| .09312 .07398 | 1.90000 | | 24 10 | 5 | 0 | . 00000 . 00080 |
| .05298 | 1.90000 1.90000 | | 24 11 24 12 | 5 | Ü Ü | . 00000 |
| .03581 | 1.90000 | | 24 13 | 5 | Ö | . 00000 |
| .01639 | 1.90000 | | 24 14 | 5 | 0 | .00000 |
| . 00000 | 1.90000 | . 156 12 | 24 15 | 5 | 0 | . 00000 |
| .00000 | 2.00000 | | 25 1 | 5 | 0 | . 00000 |
| .00000 | 2.00000 | . 00000 | 25 2 | 5 | 0 | . 00000 |



| .00000 .00000 .00000 .00000 .00000 .00000 .00000 .00000 .00000 | 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 2.00000 | .00000 .00000 .00000 .00000 .00000 .00000 .00000 .00000 .00000 | 25 25 25 25 25 25 25 25 25 25 25 25 25 2 | 3 4 5 6 7 8 9 10 11 12 13 14 15 | 000000000000000 | 00000000000000 | . 00000 . 00000 . 00000 . 00000 . 00000 . 00000 . 00000 . 00000 . 00000 |
|--|---|--|---|---------------------------------|-----------------|----------------|---|
| (EOR) 3 0 0 2.00000 .00000 | .00000 .00000 3.00000 | . 00000 1 . 50000 . 00000 | | | | | |
| (EOR) 2 20 1 1.00000 1.50000 (EOR) | -1.00000 1.00000 .00000 | . 10000 . 00000 . 00000 | | .000 | | | .00000 |
| -1,0000 1,0000 (E0F:) | . 0000 . 0500 | . 0000 . 0000 | 1 | 0 | 1 | | |

(EOF)



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SAMPLE PROBLEM TRIAXIAL ELLIPSUID
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NU. OF QUADS. = 280
NO. OF SECTIONS = 5
MAX. NO. UF SECTIONS S FLUM 150 Y FLOW 150
3 PLANES OF SYMMETRY
DNVERGENCE CRITERIA .00001
ISP = 0
IEDITI = 0
IEDITA = 0
ITAPE = .00
YCENTER = .00
YCENTER = .00



| 573 | 970 | 12411±+00 17850±+01 .29580E-02 | 17886E+01 12417E+00 20145E-01 | 17719E+01 11160E+00 1748E-01 | 11154E+00 17755E+01 49839E-02 | 95484E-01 74362E+00 .12543E-02 | 74521E+00 95755E-01 28143E-01 | 74292E+00 84505E-01 94470E-02 | 84442E-01 74470E+U0 73090E-U4 | 76789E-01 42378E+00 .84063E-03 | 42496E+U0 70925E-U1 15018E-U1 | 42372E+U0 71978E-U1 39695E-U2 | 71955E-01 42500E+00 .22457E-03 | 66911E-01 32052E+00 .17961E-02 |
|-----|-------|--|--|--|--|--|---|--|--|--|--|--|---|---|
| FL | C 2 1 | .10500k-01 .72568k-01 .52298k-02 | .10480E-01 .72630E-01 .52152E-02 | .12797E-01 .81395E-01 .75324E-02 | .12771E-01 .81672E-01 .75096E-02 | .11209E-01 .75334E-01 .25735E-02 | .11185E-01 .75703E-01 .256/2E-02 | .12606E-01 .80694E-01 .31622E-02 | .12578E-01 .81066E-01 .31536E-02 | .99910E-02 .70832E-01 .12491E-02 | .99691E-02 .71213E-01 .12471E-02 | .10534E-01 .72808E-01 .13556E-02 | .10509E-01 .73086E-01 .13521E-02 | .81086E-02 .64511L-01 .70022E-03 |
| NX | ZZ | .97898E+00 .12345E-01 .20357E+00 | .97838E+00 .37158E-01 .20343E+00 | .833596+00 .110496-01 .552276+00 | .83317E+U0 .33368E-U1 .55200E+U0 | .65904E+00 .95106E-02 .75152E+00 | .65939e+00 .28614e-01 .75125e+00 | .51966±+00 .84797e=02 .85433E+00 | .51952E+00 .25340E-01 .85408E+00 | .41272E+00 .77244E-02 .91002E+00 | .41262E+00 .23064E-01 .91061E+00 | .33241E+00 .72964E-02 .94311E+00 | .33229e+00 .21690e-01 .94293E+00 | . 20830L+00 .5,409E-02 .90329E+00 |
| γP | d7 | .96669E+U0 .49989E-U1 .51397E-U1 | .93621E+00 .14997E+J0 .51268E-01 | .94266E+00 .49490E-01 .15613E+00 | .94030E+00 .14597E+00 .15574E+00 | .86521E+00 .49990E-01 .24644E+00 | .86304E+00 .14997E+00 .24532E+00 | .76924E+00 .49989E-01 .31617E+00 | .76731E+00 .14997E+00 .31537E+00 | .66989E+00 .49991E-01 .30954c+00 | .60821E+00 .14997E+00 .36861E+00 | .57471L+00 .49959L-01 .40706E+00 | .5/32/E+00 .14997E+00 .40654E+00 | .495988+00 .499901-101 .43005-00 |
| ٨,٨ | 5.4 | .99875E+U0 .10000E+U0 .00000E+G0 | .99459E+00 .20000E+00 .00000E+00 | .97739E+00 .10000E+00 .102/3E+00 | .973711+00 .20000=+00 .10234c+00 | .906766+00 .100000+00 .20934E+00 | . 503346+00 .20000£+00 .20875£+00 | .82257L+00 .10000E+00 .28323E+00 | .81947£ +00 .20000L +00 .28217E+00 | .71454E+00 .10000E+00 .34670E+00 | .71225E+00 .20000=+00 .34739E+00 | .62399E+00 .10000E+00 .30391E+00 | . 521642+00 . 200002+00 . 30445E+00 | .100c5c+60 .42476c+50 |
| ۲۶ | 7.3 | .9/739£+u0 .1u000E+u0 .1u2/3E+u0 | .97371E+00 .20000E+00 .10234E+00 | .9 u6 76E + CO .100 UOE + UO .20934 E + OU | .90334E+00 .20000E+00 .20855E+00 | .82257E+00 .10000E+00 .20323E+00 | .81947E+00 .20000E+00 .20217E+00 | .71494E+00 .10000L+00 .34870L+00 | .71225E+00 .20000E+00 .34739L+00 | .62399E+00 .10006E+00 .30991E+00 | .621646+00 .20060=+00 .308456+00 | .52471E+00 .10000£+00 .42490E+00 | .52274L+00 .20006L+00 .42336L+00 | .108001+08 .108001+08 .448051+00 |
| 7.4 | 77 | .97801E+00 .0000UL+00 .10286E+00 | .97739E+00 .10000E+00 .10273E+00 | .90789E+00 .00000E+00 .20950E+00 | .40676E+00 .10000E+00 .20934E+00 | .82360E+00 .00000L+00 .20359E+00 | .82257E+U0 .10000E+U0 .28323E+U0 | .715&3E+00 .00000E+00 .34%14E+00 | .714946+00 .100606+00 .348/06+00 | .62478E+U0 .000UUE+U0 .39040E+U0 | .62349e+00 .10000e+00 .38991E+00 | .52537E+60 .000c0E+00 .42544E+00 | .52471E+00 .10000E+00 .42490E+00 | .447_10+60 .0u0c0E+u0 .447_21L+00 |
| ۲٦ | 2.1 | .10000E+01 .00000E+00 .00000E+00 | .99875E+60 .10000E+00 .00000E+00 | .97861E+00 .00000E+00 .10286E+00 | .97739£+U0 .10000£+00 .10273£+C0 | .90789E+00 .00060E+00 .20960E+00 | .90676E+00 .10000E+00 .20934E+00 | .82360E+00 .00000L+00 .26359E+00 | .82257±+00 .10000£+00 .28323£+00 | .71583E+00 .00000E+00 .34914E+00 | .71494E+00 .10000E+00 .34870E+00 | .62478E+00 .00000E+00 .39040E+03 | .62399E+00 .10000E+00 .38791E+00 | .52537E+U0 .000001+U9 .42544E+U1 |
| N | ۵ | | 2 2 | 312 | 7 7 7 | 3 2 2 | 6 2 3 | 446 | 4 7 8 | 5 1 6 | 5 10 | 6 1 11 | 6 2 12 | 7 1 13 |



| 32183E+00 | 32082E+00 | 67020E-01 | 65399E-01 | 27971E+00 | 27942E+00 | 64660E-U1 | 63885E-01 | 25913E+00 | 25890E+00 | 63170E-01 | 63181E-01 | 25358E+U0 |
|-------------|--------------|--------------|-------------|------------|---------------|---------------|------------|---------------|---------------|---------------|---------------|---------------|
| 68965E-01 | 67036E-01 | 32189E+00 | 27940E+00 | 65426E-01 | 64671E-01 | 27975E+U0 | 25888E+00 | 63901E-01 | 63172E-01 | 25915E+00 | 25222E+00 | 63182E-U1 |
| 85764E-02 | 24607E-02 | .94007E-03 | .359 U7E-03 | 52681E-02 | 31447E-02 | 61924E-U3 | 13246E-02 | 38368E-02 | 15840E-02 | 79794E-03 | .70397E-03 | 11849E-U2 |
| .80900E-02 | .73677E-02 | .73505E-02 | .78256E-02 | .78076E-02 | .61850E-02 | .61699E-02 | .67573E-02 | .67418E-02 | .55108E-02 | .54976E-02 | .62211b-02 | .62006E-02 |
| .64733E-01 | .62218E-01 | .62395E-01 | .63586E-01 | .63728E-01 | .50856E-01 | .58954E-01 | .60397E-01 | .60466E-01 | .57122E-01 | .57160E-01 | .5v907b-01 | .5c913E-01 |
| .69804E-03 | .60291E-03 | .60228E-03 | .59108E-03 | .58967E-03 | .42796E-03 | .42729E-03 | .45426E-03 | .45363E-03 | .35406E-03 | .35332E-03 | .40223b-03 | .40212E-03 |
| .26835E+00 | .22029E+00 | .22026E+00 | .17622E+00 | .17617E+00 | .13759E+00 | .13760E+00 | .10330E+00 | .10324e+00 | .71678E-01 | .71667E-01 | .41954E-01 | .41972E-01 |
| .20727E-01 | .6703EE-02 | .20108E-01 | .65574E-02 | .19635E-01 | .64023E-02 | .19331E-01 | .63313E-62 | .19106E-01 | .63130E-02 | .16943E-01 | .62428E-02 | .18875E-01 |
| .90310E+00 | .97541E+00 | .97523E+00 | .984.3E+00 | .98416E+00 | .99047E+00 | .99030E+00 | .99463E+00 | .99447e+00 | .99741E+00 | .99725E+00 | .99910E+00 | .99694E+00 |
| .48477E+U0 | .41100E+00 | .40997e+00 | .33655E+00 | .33571E+00 | .26741E+00 | .26674E+00 | .20317E+00 | ,20266E+00 | .14208E+00 | .14173E+00 | .43523t-01 | .83315E-01 |
| .14997E+U0 | .49990L-01 | .14997e+00 | .49989E-01 | .14997E+00 | .49989E-01 | .14997E+00 | .49990E-01 | ,14997E+00 | .49989E-01 | .14997E+00 | .49941t-01 | .14997E+00 |
| .43496E+U0 | .45505E+00 | .45391e+00 | .47006E+00 | .46688E+00 | .48121E+00 | .48000E+00 | .45895E+00 | ,48773E+00 | .49442E+00 | .49318E+00 | .49769t+00 | .49645E+U0 |
| .522 /4L+00 | .44665E+00 | .44497E+00 | .37403E+00 | .37342E+00 | .29705L+00 | .29672E+00 | .23603E+00 | .23574E+U0 | .16946t+00 | .16862E+00 | .11453E+00 | .11410£+00 |
| .200 U0E+00 | .100C0E+00 | .20000E+00 | .10000E+00 | .20006E+00 | .10000E+00 | .200v0E+00 | .10000L+00 | .26000E+U0 | .10000t+00 | .20060E+00 | .100c0E+00 | .20000£+00 |
| .42330E+00 | .44665E+00 | .44457E+00 | .40287E+00 | .40113E+00 | .47605L+00 | .47466E+00 | .48516E+00 | .44333E+00 | .49213t+00 | .49628E+00 | .49cc8L+00 | .494£1£+03 |
| .44447E+00 | .37463E+00 | .3 /342E+00 | .29785E+UC | .29672E+00 | .23663E+00 | .23574E+UU | .10946E+00 | .10862E+00 | .11453c+00 | .11410L+00 | .52410e-01 | .52220L-v1 |
| .20000E+00 | .10000E+00 | .20000E+00 | .1UOUOE+UO | .20000E+00 | .10000E+00 | .2uOUUE+UU | .10000E+00 | .200J0E+00 | .10000c+00 | .2 ∪600E+00 | .10000e+00 | .25000c+u0 |
| .44477E+00 | .40267E+00 | .40113E+00 | .47665E+UO | .47485E+00 | .40516E+00 | .4u333E+UO | .49213E+00 | .49028E+00 | .49608c+00 | .4342LE+00 | .49809e+00 | .49601c+u0 |
| .44665L+00 | .37530E+00 | .37483E+U0 | .298.2E+00 | .29785E+00 | .23692E+00 | .23663E+UO | .16967E+U0 | .16945E+00 | .11407c+00 | .11453E+60 | .52460L-01 | .52410t-01 |
| .10000E+00 | .00000E+00 | .1U0C0E+U0 | .00000E+00 | .10000E+00 | .00000E+00 | .1UOUOE+UO | .00000E+U0 | .10000E+00 | .00000c+00 | .100.00E+00 | .00000E+00 | .10000E+00 |
| .44665L+00 | .46345E+00 | .46287E+U0 | .477.5E+00 | .476u5E+00 | .48576E+00 | .48516E+UO | .492/5E+U0 | .49213E+00 | .47670c+00 | .49608E+00 | .49931E+00 | .49409t+00 |
| .52471E+00 | .44721E+00 | .44665E+00 | .37530E+00 | .37483E+00 | .29822E+00 | .29785E+00 | .23692E+00 | .23663E+00 | .16967£+00 | .16946E+00 | .11467E+00 | .11453E+00 |
| .10900E+09 | .000C0E+00 | .1000E+00 | .00000E+00 | .10000E+00 | .00000E+00 | .10000E+00 | .00000E+00 | .10000E+60 | .00000£+00 | .10000E+00 | .00000L+00 | .1000nE+00 |
| .42450E+00 | .44721E+00 | .44665E+00 | .46345E+00 | .46287E+00 | .47725E+00 | .47665L+00 | .48576E+00 | .48516E+00 | .49275£+00 | .49213E+00 | .49670E+00 | .49608E+00 |
| 7 2 7 14 | 8 1 15 | 8 2 16 | 9 17 | 9 18 | 10 1 19 | 10 2 20 | 11 1 2 2 1 | 11 2 22 | 12 1 23 | 12 2 24 | 13 1 25 | 13 2 26 |



| 25223E+00 | 62812E-01 | 12683E+00 | 18064E+01 | 17812E+01 | 11365E+U0 | 97736E-01 | 75390E+U0 | 74763E+U0 | 87042E-U1 | 79895E-01 | 43003E+00 | 42716E+00 |
|--------------------------|---|--|--|--|--|--|---|--|--|--|--|--|
| 62811E-01 | 25358E+00 | 17958E+01 | 12715E+00 | 11485E+00 | 17928E+U1 | 74942E+00 | 99216E-U1 | 87945E-U1 | 754U9E+U0 | 42769E+00 | 80645E-01 | 75178E-01 |
| .15965E-02 | .19808E-03 | .12965E-01 | 48494E-01 | 87983E-01 | 11139E-01 | .10285E-01 | 65154E-U1 | 46661E-U1 | 64145E-U3 | .70682E-02 | 34708E-01 | 21719E-01 |
| .52450e-02 | .52329E-02 | .10440E-01 | .10379E-01 | .12720E-01 | .12641E-01 | .11137E-01 | .11064E-01 | .12521E-01 | .12437E-01 | .99235E-02 | .98545E-02 | .10460E-01 |
| .56467E-01 | .56454E-01 | .72619E-01 | .72539E-01 | .81841E-01 | .81902E-01 | .75979E-01 | .75171E-01 | .81325E-01 | .81479E-01 | .71403E-01 | .71642E-01 | .73203E-01 |
| .33126E-03 | .33063E-03 | .51918E-02 | .51480E-02 | .74677E-02 | .73965E-02 | .25610E-02 | .25426E-02 | .31434E-02 | .31174E-02 | .12507E-02 | .12416E-02 | .13545E-02 |
| .13060E-01 | .12995E-01 | .97716E+00 | .97529E+00 | .83234E+00 | .83107E+00 | .65892E+U0 | .65816E+00 | .51923c+00 | .51874E+00 | .41245E+00 | .41214E+00 | .33212E+00 |
| .62272E-02 | .18816E-01 | .62193E-01 | .47549E-01 | .558L5E-01 | .78560E-01 | .47902E-01 | .67468E-01 | .42573c-01 | .60024E-01 | .3b7.8E-01 | .54728E-01 | .36365E-01 |
| .99990L+00 | .99974E+00 | .20321E+00 | .20254E+00 | .55145E+00 | .55058E+00 | .75069E+00 | .74905E+00 | .85357c+00 | .85262E+00 | .91016E+00 | .90947E+00 | .94254E+00 |
| .26222E-01 | .20158E-01 | .98124E+U0 | .97372E+U0 | .93556E+00 | .92839E+00 | .45808E+00 | .85211E+00 | .70344E+00 | .75759E+U0 | .56484E+00 | .65975E+00 | .57038£+00 |
| .49959E-01 | .14997E+00 | .24995E+U0 | .34993E+U0 | .24995E+00 | .34992L+00 | .24995E+00 | .34992E+00 | .24995E+00 | .34992E+U0 | .24945E+00 | .34992E+00 | .24995E+00 |
| .49934E+00 | .49809E+00 | .51008E-U1 | .50618E-01 | .15495E+00 | .15377E+00 | .24458E+00 | .24271E+00 | .31378E+00 | .31138E+U0 | .36676E+00 | .36394E+00 | .40459E+00 |
| .52410E-01 | .52220L-01 | .948696+00 | . 97980e+u0 | .967548+00 | . 95864E+00 | .89762E+00 | .88955E+UU | .814288+00 | .806,46£+00 | .107/4±+00 | . 101378 +00 | .61771:+00 |
| .10000E+00 | .2000CL+00 | .30000c+00 | .40000e+u0 | .30000E+00 | .40000E+00 | .30000E+00 | .4UUUUE+UO | .30006e+00 | .400,00E+00 | .30000E+00 | . 409 c08 + 00 | .30000:+00 |
| .49869E+00 | .4460L+00 | .00000c+00 | .00000e+u0 | .101698+00 | .10078E+00 | .20723E+00 | .2U537L+UU | .26038k+00 | .277,06E+00 | .34519±+00 | . 342 c38 + 00 | .30577:+10 |
| .00000L+00 .10000E+00 | .000000E+00 .20000E+00 .49749E+00 | .96754E+00 .30000E+00 .10159E+60 | .958848+00 .400008+00 .100788+00 | .89702E+00 .30000£+00 .20723E+00 | .88955E+00 .40000E+00 .20537E+00 | .81428E+U0 .3~U0UE+U0 .2~O38E+CO | .8u6,46E+00 .4u0u0E+00 .27786E+00 | .70774£+00 .33000£+00 .34519E+00 | .701372+00 .400002+00 .34208E+00 | .617712+00 .3v0v0E+v0 .3o599L+v0 | .61215E+00 .40000E+00 .30251E+00 | .51943L+06 .30060L+06 .42662L+06 |
| .00000E+00 | .00000E+00 | .97371E+00 | .96754£+00 | .90334E+00 | .89762E+00 | .81947L+v0 | .81428E+U0 | .71225£+00 | .707742+60 | .62104E+00 | .61771£+00 | .522741+00 |
| .00000E+00 | .10000E+00 | .20000E+00 | .30600£+00 | .20000E+00 | .30000E+00 | .20000E+u0 | .3U0U0c+U0 | .20060£+00 | .30060L+00 | .20000E+00 | .3v0c0£+00 | .20002+00 |
| .50000E+00 | .49937E+00 | .10234E+00 | .10169£+00 | .20855E+00 | .20723E+00 | .28217E+00 | .28038E+U0 | .34739£+00 | .34519E+00 | .38845E+00 | .3d599£+00 | .423301+00 |
| .52480E-01 | .52410t-01 | .99499E+00 | .98869E+00 | .97371£+00 | .96754E+00 | .90334E+00 | .89762L+00 | .81947E+U0 | .81428E+U0 | .71225E+U0 | .76774E+00 | .62164E+00 |
| .00000E+00 | .10000t+00 | .20000E+00 | .30000E+00 | .20000£+00 | .30000E+00 | .20000E+00 | .30000E+00 | .2U0U0L+U0 | .3UUUUE+C0 | .2U0U0E+00 | .30000E+00 | .20000L+00 |
| .49931E+00 | .49869t+00 | .00000E+00 | .00000E+00 | .10234£+00 | .10169E+00 | .20855E+00 | .20723E+00 | .28217L+O0 | .26038E+O0 | .34739E+00 | .34519E+00 | .38845E+00 |
| 14 1 27 | 14 2 28 | 1 3 3 2 9 | 1 4 30 | 2 3 | 32 | 6 C C | 3 4 4 | 33 33 | 3 4 4 | 3 7 5 | 3.4.5 | 39 39 |



| 74777E-01 | 70941E-01 | 32575E+00 | 32311E+U0 | 68865E-01 | 67399E-U1 | 28330E+00 | 28118£+00 | 66271E-01 | 65772E-01 | 26399E+00 | 26176E+00 | 65058E-01 |
|------------|-------------|---|------------|--------------|---------------------|----------------|-------------|------------|---------------|------------|---------------|---------------|
| 43056E+00 | 32329E+U0 | 71303E-01 | 69037E-01 | 32599E+00 | 28124E+U0 | 67558E-01 | 66344E-01 | 24340E+00 | 26178E+00 | 65822E-01 | 65073E-01 | 20404E+00 |
| .33122E-02 | .40087E-02 | 20919E-01 | 12483E-01 | .98076E-U3 | .28884E-U2 | 12965E-01 | 75106E-02 | .54621E-03 | .28002E-02 | 72947E-02 | 26159E-02 | .12042E-02 |
| .10307E-01 | .80526E-02 | .79956E-02 | | .72649E-02 | .777126-02 | .77154E-02 | .61406E-02 | .60968E-02 | .67098E-02 | .6c619e-02 | .54713E-02 | .54319E-02 |
| .73400E-01 | .64904E-01 | .65019E-01 | | .62618E-01 | .638166-01 | .63850E-01 | .59019E-01 | .59051E-01 | .60493E-01 | .6u478e-01 | .57171E-01 | .57158E-01 |
| .13452E-02 | .70054E-03 | .69684E-03 | | .60090E-03 | .592566-03 | .58930E-03 | .43046E-03 | .42851E-03 | .45931E-03 | .45697e-03 | .35894E-03 | .3577E-03 |
| .33195E+00 | .26823E+U0 | .26808E+00 | .220196+00 | .22003E+00 | .17610E+00 | .17601E+00 | .13753E+00 | .13745E+00 | .10328E+U0 | .10327E+00 | .71555E-U1 | .71523E-01 |
| .513e8E-01 | .34755E-U1 | .48948E-01 | .337406-01 | .47520E-01 | .32960E-01 | .46439E-01 | .32396E-01 | .45651E-01 | .31977E-U1 | .45129E-01 | .31713L-U1 | .44723E-01 |
| .94190E+00 | .90273E+U0 | .96215E+00 | .974876+00 | .97434E+00 | .98382E+00 | .98329E+00 | .98997E+00 | .98946E+00 | .99414E+U0 | .99303E+00 | .99693E+U0 | .99644E+00 |
| .56602E+00 | .46232E+60 | .47863E+U0 | .40790E+00 | .40478E+U0 | .33401E+00 | .33145E+00 | .26539e+00 | .26335c+U0 | .20164e+00 | .20009c+00 | .14101E+00 | .139932+ JO |
| .34992E+00 | .24995E+00 | .34992E+30 | .24995L+00 | .34993E+U0 | .24995E+00 | .34992E+00 | .24995e+00 | .34992c+U0 | .24995t+00 | .34993c+00 | .24995E+00 | .349922+ CO |
| .40149E+00 | .43276E+00 | .42945E+00 | .45162E+00 | .44816E+U0 | .40651E+00 | .46294E+00 | .47758e+00 | .47392c+OU | .48527e+00 | .48155E+00 | .49069E+03 | .48694E+ CO |
| .61215E+00 | .51943£ +U0 | .51476L+00 | .44215E+00 | .43818E+UO | .37105E+v0 | .36771E+UU | .29464E+60 | .29219E+00 | .23424L+00 | .23214E+00 | .16775L+00 | .166242+00 |
| .40000E+00 | .3∪U00£+U0 | .400C0E+00 | .300C0E+00 | .43000E+UO | .30000E+00 | .40000E+UU | .30000E+00 | .40000E+00 | .30000L+00 | .40000E+00 | .30000E+00 | .400062+00 |
| .36251E+00 | .4∠062£+U0 | .41604E+00 | .44215E+00 | .43818E+OO | .45821E+00 | .454U9E+UO | .47lo5E+00 | .46701L+00 | .48027E+00 | .47595E+00 | .48718L+00 | .462002+00 |
| .51476E+J0 | .44215E+00 | .43818E+00 | 7105e | .307/1c+U0 | .29484 <u>c</u> +u0 | .2 /21/9E +u0 | .23424E+00 | .23214E+00 | .10775c+u0 | .10624E+00 | .11338E+00 | .1.236E+00 |
| .4J0UUL+UO | .30000E+00 | .40060E+00 | 0000e | .4U0JUc+U0 | .30000E+00 | .4 v0 00E +u0 | .30000E+00 | .4v0u0E+J0 | .3u0u0c+u0 | .40000E+00 | .30000E+00 | .40050_+00 |
| .416U4E+UO | .44215E+00 | .43818E+06 | 5821E | .454CYE+U0 | .47165 <u>c</u> +u0 | .4 o7 bl E +u0 | .46027E+00 | .47595E+U0 | .4c718c+u0 | .48280L+00 | .41108E+00 | .43667E+06 |
| .51943£+00 | .44497L+00 | .44215E+00 | .37342E+00 | .37165E+UO | .29672L+U0 | .29464E+UO | .23574E+60 | .23424E+00 | .10882c+U0 | .167/52+00 | .11410E+00 | .11338E+00 |
| .300.0£+00 | .20000E+00 | .30000E+00 | .20000E+00 | .30000E+UO | .2UUCOE+U0 | .300UOE+UO | .20060E+60 | .30000E+00 | .20000c+U0 | .3JOUNE+UO | .20900E+00 | .30000E+00 |
| .42002£+00 | .44497L+00 | .44215E+00 | .45113E+00 | .45821E+OO | .47486E+U0 | .47165E+UO | .48333E+00 | .48027E+00 | .49028E+U0 | .48718E+UO | .49421E+00 | .43108E+00 |
| .61771E+00 | .52274E+00 | .51943E+00 | .44497E+00 | .44215E+00 | .37342E+00 | .37105E+00 | .29672 E+00 | .29484E+00 | .23574E+00 | .23424E+09 | .16952E+U0 | .16775E+00 |
| .3COCOE+00 | .200COE+00 | .3COCOE+00 | .2000L+00 | .30000E+00 | .200C0E+00 | .30000E+00 | .20000 E+00 | .30000E+00 | .20000E+00 | .30000E+C0 | .20900E+U0 | .300C0E+00 |
| .38599£+00 | .42330E+00 | .42062E+00 | .44497E+00 | .44215E+00 | .46113E+00 | .45821E+00 | .474 86E+00 | .47185E+00 | .48333E+00 | .48027E+00 | .49028E+U0 | .48718E+00 |
| 940 | 433 | 7 | 8 E E | ω 4 4 | 0 W W | 6 4 4 9 | 10 | 10 | 11 3 49 | 111 4 5 0 | 12 3 51 | 12 4 52 |



| 1 .11338£+00 .82098E-01 .41930E-01 .61770E-0264578E-01 | .300001+30 .24995E+00 .31601E-01 .58886E-01 - | 0 .491082+06 .493/42+00 .9988622+00 .403312-03 .66019E-03 | .11236e+00 .82203e-01 .41823e-01 .61329E-02 | .400006E+JU .34493E+U0 .44512E-U1 .58827E-01 | 0 .486u7_+uu .49016e+00 .99813e+00 .40084e-0317060E-u2 | .51890E-J1 .20028E-J1 .13056E-J1 .52085E-02 | 0 .300.00L+00 .24995=+00 .31518E-01 .55420E-0164452E-01 | 0 .4y3c6L+u() .4y558L+J() .4yy42E+00 .33300E-U314554E-02 | U .51420t-Ul .25528t-Ul .13150t-Ol .51710t-O264447E-Ul | |
|--|---|---|---|--|--|---|---|--|--|---------------|
| | | | | • | | | | • | | |
| | | | | | | | | • | | |
| .113382+00 | . 300 cor + 3C | 441082+00 | .11236E+00 | . 400 UCE + JU | .486674+00 | .51890E-J1 | .300 COL +00 | .44306E+0() | .514206-01 | .40000£+00 |
| .51070c-01 | .30000E+00 | .413066+00 | .514604-01 | .40000£+06 | .40922L+00 | .000000E+00 | . 30000E+00 | .4,4346+00 | .0000000 | . 400 00E +00 |
| .522205-01 | . 200 UOE + CO | .496511+00 | .518,0E-01 | . 300 UNE +00 | . 49306E+00 | . 000000 + U0 | .2000E+00 | 00+3642640 | 00+300000 | .30000E+00 |
| .11410E+60 | .20000E+00 | .49421E+00 | .11338£+00 | .30000E+00 | .491086+00 | .52220E-01 | .20000c+00 | .49681c+00 | .518401-01 | 30000F + 00 |
| 13 |) M | 53 | 13 | 4 | 5.4 | 14 | 6 | 55 | 14 | 4 |



| 42 + 5 | .94754E+UU .96825E+UO .96 .50000E+UC .50000E+UO .44 .99590E-U1 .00000E+UO .50 | .93354E+00 .95374E+00 .95084E+00 .96941E+00 .60000E+00 .54988E+00 .14006E+00 .14046E+00 .96157E+00 | .8/966E+U0 .94754E+C0 .91876E+U0 .82930E+U0 .509U0E+U0 .500U0E+C0 .44990E+U0 .10190E+U0 .20295E+U0 .54943E+U0 | .80607E+00 .93354E+00 .90657E+00 .82700E+00 .60000E+00 .54988E+00 .12567E+00 .12567E+00 .12567E+00 .12567E+00 | .74745E+U0 .879U6E+U0 .84326E+U0 .65712E+U0 .530U0E+U0 .500UE+U0 .449Y0E+U0 .87571E-U1 .27458E+U0 .20295L+U0 .24019E+U0 .74868E+U0 | .7d5u6e+00 .8ubu7e+00 .83208e+00 .65576E+00 .6u00ue+u0 .6u0u0e+00 .549u8e+00 .1u826e+00 .27032e+u0 .19995e+00 .23700e+00 .74716E+00 | .69310E+00 .79745E+00 .74973E+00 .51807E+00 .50000E+00 .77847E-01 .33805E+00 .27458E+00 .30815E+00 .85179E+00 | .60286E+00 .6000E+00 .33305E+00 | .60494e+00 .69310E+00 .65290E+00 .41176E+00 .50000E+00 .44996e+00 .70847E-01 .37801E+00 .33805E+00 .36017E+00 | .59600±+00 .68286±+00 .64424±+00 .41124±+00 .60000±+00 .54988±+00 .8780€=01 .37242±+00 .33342±+00 .35534±+00 | .50869E+00 .66494E+09 .56014E+00 .33168E+00 .50000E+00 .44990E+00 .66554E-01 .41131+00 .37601E+06 .39733E+00 .94104E+00 | .501172400 .59600E+00 .55271E+00 .33125E+00 .600002400 .54968E+00 .82409E-01 .40504E+00 .37246E+00 .37246E+00 | .43301E+00 .50869E+00 .47367E+00 .26764E+00 .50000E+00 .50000R+00 .44490E+00 .63612E-01 |
|---|---|--|---|---|--|---|---|--|---|--|---|---|---|
| 71 Y2 Y2 72 72 72 72 72 72 72 72 72 72 72 72 72 | 0£+00 .95 0£+00 .40 0£+00 .10 | .96825£+00 .94754£+60 .50000£+00 .50000£+00 .99590£-01 | .95864E+U0 .88955E+U0 .40000E+U0 .40000E+U0 .10078E+U0 .20537E+U0 | .94754E+00 .87946E+00 .54060E+00 .50046E+00 .99590E-01 .20295E+00 | .88955E+00 .80696E+00 .40000E+00 .40000E+00 .20537E+00 .27786E+00 | .87906E+60 .79745E+00 .50000E+00 .500.0E+00 .20295E+60 .27458E+00 | .80696e+00 .70137E+00 .40000E+00 .27786E+00 .342v8e+00 | .79745E+UO .69310E+UO .50000E+UO .27458E+UO .33385E+UO | .70137E+00 .61215E+00 .40000E+60 .40000E+00 .34208E+00 .38251E+00 | .64310E+00 .60494E+00 .50000E+00 .50000E+00 .33865E+00 .37801E+00 | .61215E+00 .51476E+00 .400u0E+00 .400u0E+00 .31251E+00 .41684E+00 | .60494E+00 .50869E+00 .50000E+00 .37801E+00 .41193E+00 | .51476E+00 .43818E+00 .40000E+00 |



| 33211E+00 78371F=01 | 33856E-UI | 30E | | 73069E-01 33278E+00 | .36245E-U2 | 71294E-01 | 28574E+U0 .46377E-U2 | 288016400 | 71735E-U1 | 21403E-01 | 28550E+00 | 0256E | 37E | 70017E-01 | 28915E+00 | .75220E-03 | 69391E-01 | 26535E+00 | .261335-02 | 26783E+U0 | 69533E-01 11550E-01 | 26527E+00 | .68896 | 74949E-02 | 68825E-01 | 26/90E+00 | 82566E-U4 | 69052E-01 | 23 / 38E + UU . 40314E-U2 | 26.1 | 69061E-01 | 42201E-U2 |
|--------------------------|-------------|--------------------------|---------------|--------------------------|------------|------------|--|-------------|---------------|------------|-------------|--------------|---------------|------------|------------------|------------|------------|---------------|------------------|--------------|---------------------------|------------|--------------|------------|------------|----------------|---------------------|-------------|------------------------------|-----------|---------------------|------------|
| .78217e-02 .65098e-01 | .69443E-U3 | .71951E-02 .62603E-01 | •6 U6U7E-U3 | .71069E-02 .62605E-01 | .601016-03 | .704066-02 | .63833E-01 .59331E-03 | 75466 F-02 | .63773E-01 | .567896-03 | .603806-02 | 5E-0 | 3 | .59636E-02 | 54030E-0 | .43101E-03 | .65976E-02 | .60428E-01 | .46106E-03 | .65159E-02 | .60339E-01 | .53794E-02 | .571226-01 | .36353E-03 | .531294-02 | .5/061E-01 | .30011E-U3 | .60735E-02 | .41059E-01 | 0-31000 | .50606E-01 | .40761t-03 |
| .26752E+U0 .78712E-U1 | .90033E+UU | .21967E+U0 .61741E-01 | • 91331E+00 | .21971E+00 .70307E-01 | .97257E+UO | .17583E+00 | .60313E-01 .96257E+00 | 1754.45 +00 | .74504E-01 | .98163E+00 | .13738E+00 | .593156-01 | .98874E+U0 | .13725E+00 | .73327E-01 | .96762E+00 | .10314E+00 | .58629E-01 | . 99294E+00 | .102 y8E +00 | .72506E-01 .99204E+00 | .71509E-01 | .58105E-01 | .99574E+00 | .71524E-01 | ./1929t-01 | 004340464 | .41821E-01 | .94745E+00 | 1974777 | .71607E-01 | .99605E+00 |
| . 407386+00 | .41930E+00 | .40057E+00 .44770E+00 | 00.310644. | .39526E+U0 .54988E+U0 | .43703E+U0 | .32801c+00 | .44440E+00 .45814E+00 | 37466 = 400 | .54988E+00 | .45206E+00 | .20002E+00 | .44990E+00 | .46900E+00 | .25716E+U0 | .54988E+00 | .40278E+00 | .19602E+00 | 44990E | .47655E+00 | .19539E+00 | .54988E+00 .47023E+00 | .13848E+00 | .44990E+00 | .46188E+00 | .13664E+00 | .54488E +00 | •4/2405+00 | .81406E-01 | .44930E+00 .46507E+00 | - | .549881+00 | |
| . 50117c + 00 | .40504E+00 | .43301c+00 .50000c+00 | • 433016 400 | .426c2c+u0 .600u0c+u0 | .42661E+00 | .363381+00 | .50000E+00 .448/4E+00 | 358015400 | 0000000 | .44211E+UO | .238/5E+00 | .50000E+00 | • 462 59E +00 | .28448E+UO | 00 00E | .45527E+U0 | .22940E+U0 | . 500 00E +00 | • 4 / 0 34E + 00 | .22601E+U0 | .60000e +00 .463.9E+00 | .16428E+00 | .50000E+00 | .47710E+00 | .16105E+UU | . 600 00E + 00 | • 4 / 0 0 0 E + 0 0 | .11103E+00 | . 46093L+00 | 100.00 | . 550000 + 60 | .4/3026+00 |
| . 4 4 6 6 2 K + 4 0 0 | .42661E+00 | .3c3s8E+00 .50000E+00 | 00.35.05. | .35801E+00 .60000L+00 | .44211E+00 | .208/5E+U0 | . 50000E +00 . 46209E +00 | 284481+60 | .60000E+00 | .455276+00 | .22940E +u0 | . 500000E+00 | .4/034E+U0 | .22601E+00 | • 6 00 00 E + 00 | •40339E+00 | .lo428E+UU | .50000L+00 | • 4 (/ IUE + UU | .10155£+U0 | .60000E+00 .4/005E+00 | .11103E+00 | . 50000E +00 | .40093E+00 | .10939E+00 | . 600000E+C0 | • 4 (302E +00 | . 508±0E-01 | .40346E+00 | | . 6 J 0 C 0 E + C 0 | .47631c+uC |
| .43301c+00 | . 43301E+00 | .367/1E+00 .40900c+00 | • 424046400 | .36338E+00 .50000E+00 | .44874E+UO | .29219E+60 | .46761E+00 | 2 4875r ±00 | . 500 COE +00 | .46209E+00 | .23214E+00 | • 40000 E+00 | .47595E+00 | .22940E+00 | . 500 UDE + UO | .47034E+00 | .16624E+00 | . 40000E +00 | • 48250E+00 | .16428E+60 | .50000E+00 .47710E+00 | .11236c+00 | .40000 = +00 | .48667E+00 | .11103L+00 | . 500000 + 000 | • 400456 + 00 | .51420r-01 | .48922E+00 | | . 50000 E+00 | .463461+00 |
| .50869E+00 | .411936+00 | .43818E+60 .40000E+00 | . 43616 6* 00 | .433G1E+00 .50000E+00 | .43301E+00 | .36771E+00 | .4 CO CO E + O O .4 5 4 O 9 E + O O | 323381+00 | .50000E+00 | .44874E+00 | .29219E+00 | .40000E+00 | .46761E+UO | .28875E+00 | .50000E+00 | .46209E+00 | .23214E+00 | .40000E+00 | .4 (595E+UI) | .22940E+00 | .50000E+00 .47034E+00 | .16624E+00 | .40000E+00 | .45280E+00 | .16428E+00 | .50000E+00 | .477106400 | .11236E+00 | .48667E+00 | 111036400 | .50000E+00 | .46093[+00 |
| ~ ~ | 20 | 891 | 1 | & / - | 7.5 | 6 | 73 | o | · - | 74 | 10 | 9 | 75 | 10 | 7 | 9/ | 11 | ا 6 | 2 | 11 | 7.8 | 12 | 9 | 62 | 12 | ~ c | 0 | 13 | 81 | 13 | ~ | 82 |



| 25737E+00 68652E-01 11592E-02 68650E-01 2013dE+00 | 14281E+00 18657E+01 .37208E-01 18932E+01 1444E+00 | 18408E+01 13766E+00 24571E+00 12875E+00 18773E+01 24918E-01 | 11207E+00 78718E+00 .30955E-01 79534E+00 12027E+00 | 77776E+U0 10595E+U0 13112E+U0 99330E-U1 79953E+U0 | 91464E-01 44965E+00 -20087E-01 45461E+00 95719E-01 | .44540E .84744E |
|---|--|---|--|--|--|--|
| .51205E-02 .50281E-01 .34136E-03 .50568E-02 | .10071E-01 .71884E-01 .49646E-02 .99241E-02 .71544E-01 | .12241E-01 .81470E-01 .70742E-02 .12049E-01 .81128E-01 | .10692E-01 .76256E-01 .24818E-02 .10514E-01 .76133E-01 | .120026-01 .813086-01 .301916-02 .117956-01 .810516-01 | .95033E-02 .71750E-01 .12293E-02 .93347E-02 .71656E-01 | .10013E-01 .73261E-01 .13252E-02 |
| .130846-01 .576656-01 .998256+00 .13936-01 | .96551E+00 .16759E+00 .20072E+00 .96003E+00 .19613E+00 | .82413E+00 .15071E+00 .54598E+00 .82057E+00 .17604E+00 | .65404E+00 .12904E+00 .74527E+00 .65193E+00 .15219E+00 | .51621E+00 .11540E+00 .848c5E+00 .51490E+00 .13551E+00 | .41053E+00 .10519E+00 .90576E+00 .40963E+00 .12357E+00 | .33077E+U0 .90803E-U1 .93852E+U0 |
| . 25528E-01 .44940E+00 .40608E+00 .25218E-01 .54948B+00 | .93526e+00 .64985c+00 .40619c-01 .91676c+00 .74982c+00 | .89172c+00 .64985e+00 .14770c+00 .37408e+00 .74982e+00 | .81845E+00 .64985E+00 .23312E+00 .80226E+00 .74962E+00 | .72/67E+00 .64985E+00 .29908E+00 .71327E+00 .7982E+00 | .63369E+U0 .64985E+U0 .34957E+GU .62115E+U0 .74982E+U0 | .54366E+UU .64785E+UU .38564E+UU |
| . 50810L-01 . 5000C0E+60 . 48346E+00 . 50000L-01 . C00C0E+00 | .936 (5E+00 .700 (0E+00 .000 (0E+00 .916.2E+00 .800 00E+00 | .91671E+00 .70050E+00 .90350E-01 .89691E+00 .8000E+00 | .85047F+00 .7000E+00 .14635E+00 .83210E+00 .40000E+00 | .771506+00 .70006+00 .26565+00 .75404+00 .80006+00 | . 670562 + 00 . 700002 + 00 . 327052 + 00 . 600002 + 00 | .56526E+00 .70000E+00 .30571E+00 |
| . 00000E+00 . 500000E+00 . 40412E+00 . 00000E+00 | .91671E+00 .7000CE+00 .90350E-01 .87691E+00 .80000C+00 | .85047£+00 .70000£+00 .17635£+00 .83210£+00 .8000£+00 | .771506+60 .7000L+60 .205656+00 .754446+00 .80000E+00 | .6/026E+v0 .70000E+v0 .32705E+v0 .62607E+v0 | .50526E+00 .70000E+00 .30571E+00 .57202E+00 | .47214L+00 .70900L+09 .37853E+00 |
| . 000000 = +00 . 40000 = +00 . 48990 E + 60 . 00000 = +00 . 50000 = +00 | .93354C+00 .60000C+00 .90120E-01 .91671E+00 .700C0E+00 | .866 07E +00 .600 00E +00 .19995E +00 .850 47E +00 .700 00E +00 | .78566E+U0 .600UE+U0 .27052E+U0 .77150E+U0 .700U0E+U0 | .64266.00 .600006.00 .333056.00 .700006.00 .327056.00 | .69600E+00 .60000E+00 .37242E+00 .56526E+00 .70000E+00 | .50117E+00 .60100E+00 .40524E+00 |
| .51420E-01 .4000E+00 .4892E+00 .50810E-01 | .95394E+00 .60000E+00 .00000E+00 .93675E+00 .70000E+00 | .93354E+00 .60006+00 .93120E-01 .91671E+00 .7000E+00 | .86607£+00 .6000£+00 .19995£+00 .85047£+00 .70000£+00 | .78566+00 .60006+00 .27052E+00 .77150E+00 .7000E+00 | .68286E+09 .60000E+09 .33365E+00 .67056E+00 .37705E+00 | .59600E+00 .59600E+00 .37242E+00 |
| 14 83 7 7 | 6 4 2 8 8 B L C | 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | 88 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 | 9 4 4 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 9 8 6 |



| 102 | 101 | 0 7 7 | 0 - 1 - | 100 | 7 0 7 | 0 77 | 1 1 1 | 7 0 7 | 100 | 0 1 1 | 0 1 1 | 10 |
|--|--|--|--|--|--|---|--|--|--|--|--|---------------------------------|
| 85893E-01 45744E+00 .61012E-02 | 82755E-01 33948E+00 .13906E-01 | 34497E+U0 84695E-01 48778E-01 | 33787E+U0 81273E-U1 33427E-U1 | 80106E-U1 34635E+U0 .57024E-U2 | 780976-01 29434E+00 .92829E-02 | 29961E+U0 78985E-U1 30987E-U1 | 29368E+00 77363E-01 20947E-01 | 76848E-01 30010E+00 .20579E-02 | 76376E-01 27183E+00 .62936E-02 | 27698E+U0 766b3E-01 17137E-U1 | 27160E+00 76297E-01 11315E-01 | 76146E-01 27707E+00 |
| | | | | | • • | | | | | | | |
| .98329E-02 .73059E-01 | .77037E-02 .65067E-01 .70667E-03 | .75645E-U2 .64991E-U1 .64751E-U3 | .69996E-U2 .62631E-U1 .61405E-03 | .68716e-02 .62556e-01 .60579e-03 | .74321E-02 .63660E-01 .59929E-03 | .72964E-02 .63506E-01 .59147E-03 | .58729E-02 .58973E-01 .44480E-03 | .57654E-02 .50896E-01 .44022E-03 | .64105E-02 .60211E-01 .46998E-03 | .62985E-02 .60054E-01 .46479E-03 | .52319E-02 .56976E-01 .37576E-03 | .51356E-02 .50875E-01 |
| .33015=+00 .11618L+00 .93675E+00 | .26721E+00 .94371E-01 .95901E+00 | .266/7E+00 .11097E+00 .95735E+00 | .21937e+00 .91641e-01 .97133E+00 | .21894E+U0 .10773E+U0 .96977E+U0 | .17545E+00 .89588E-01 .98040e+00 | .17522E+00 .10523E+00 .97849E+00 | .13707E+00 .850c0E-01 .986c4E+00 | .136 d5 E + 00 .10345 E + 00 .98518 E + 00 | .10286L+00 .87001E-01 .99088E+00 | .10272E+00 .10228E+00 .98944E+00 | .71405E-01 .46253E-01 .99371E+00 | .71303E-01 .10146E+00 |
| .53290E+U0 .74982E+U0 .37601E+U0 | .45973E+00 .64945E+00 .41249E+00 | .45063£+00 .74962£+00 .40433£+00 | .30879e+UU .64985e+UO .43046e+UO | .3&110E+00 .74942E+00 .4<194E+00 | .31836E+00 .64985E+00 .44466E+00 | .31206±+00 .74942±+00 .43586±+00 | .25295E+00 .64985E+00 .45520E+00 | .24795E+UU .74962E+UU .4462UE+UU | .19219E+00 .64985E+00 .40253E+00 | .18839E+00 .74942E+60 .45338E+00 | .13440L+00 .64945E+00 .46770E+00 | .13175E+60 .74982E+60 |
| . 572 02 L + 00 . 800 00 E + 06 . 35 7 81 E + 00 | .49214E+00 .700c0:+00 .39353E+00 | .48151c+00 .800c0c+00 .36972c+00 | .41893c+00 .700006+00 .41893c+00 | .40968E+00 .80000E+00 .40968E+00 | .35156E+UC .700COE+UO .43414L+UO | .34347:+00 .80000:+00 .42476:+00 | .27936E+00 .70000L+00 .44766L+00 | .2 /352E+U0 .800v0L+U0 .4574Lc+U0 | .221,48+00 .700,00£+00 .455,04£+00 | .21714(+00 .80600±+06 .44521±+00 | .158941+00 .70005±+00 .46158±+00 | . 19590L + UC . 800 UCE + UO |
| .401216+00 .800006+00 .33992e+00 | .418932+00 .70000=+00 .418932+00 | .409686+00 .800006+00 .40908E+00 | .35155c+00 .706c0c+00 .43414c+60 | .34397L+UU .8UOUOE+UO .42476E+UU | .27936L+00 .7000E+00 .44706E+00 | .2 /3.25 + 60 .8.0005 + 60 .4.5741 E + 90 | .221946+00 .700006+00 .405046+00 | .21714E+00 .80000E+00 .44521E+00 | .15894£ + 00 .70000£ + 00 .40158£ + 00 | .15550L+00 .8000GE+00 .40101L+00 | .10742E+00 .70006E+06 .40529E+00 | .10510L+00 .80000L+00 |
| .49214E+00 .70000E+00 .34854E+00 | .425628.400 .660008.400 .42601e+00 | .41893E+00 .70000E+00 .41893E+00 | .358 Uli + UO .600 UOE + UO .44211E + UO | .35156E+00 .70000E+00 .43414E+00 | .28448E+U0 .60000E+U0 .45527E+U0 | . 27936E+U0 .7U0U0E+U0 .447U6E+U0 | .22601L+00 .600c0E+00 .46339E+00 | .22194e+00 .70000E+00 .45504E+00 | .16105L+00 .60000L+00 .47005E+00 | .15894£+00 .70000£+00 .40158£+00 | .10939E+UO .6UGUOE+UO .47362E+UO | .10742E+00 .70000E+00 |
| .56526E+00 .70000E+00 .36571E+00 | .50117E+00 .600C0E+00 .40564E+00 | .49214E+00 .70000E+00 .39853E+00 | .42662L+00 .60000L+00 .42661L+00 | .41893E+U0 .7U0U0E+U0 .41893E+O0 | .35801£+00 .60000E+00 .44211E+00 | .35156E+00 .70000E+00 .43414E+00 | .28448E+00 .60000E+00 .45527E+00 | .27936£+00 .70000£+60 .44766£+00 | .22601E+00 .60000E+00 .46339E+00 | .22194E+09 .70000E+00 .45504E+00 | .16185E+00 .60000E+00 .47005E+00 | .15894£+03 .76060E+00 |
| 96 | 7 8 97 | 7 9 98 | 8 8 6 7 | 8 9 100 | 9 8 101 | 9 9 | 0. ° € 1 ° € 147 | 10 9 104 | 11 8 105 | 11 9 106 | 12 8 107 | 12 9 |



| 13 | .10939E+00 | .50060E-01 | .4 >160E-01 | .10742E+00 | .79010e-01 | .41734E-01 | .59064E-02 | 75785E-01 |
|------|-------------|---------------|--------------|---------------|------------|------------|------------|------------|
| 80 | .60000E+00 | .60000E+00 | . 70000E +00 | .70000E+00 | .64985E+00 | .85819E-01 | .58448E-U1 | 26468E+00 |
| 109 | .47382E+00 | .47631E+00 | .40773E+00 | .465 c9E + 00 | .47080E+00 | .99544E+UU | .41959E-03 | .27733E-02 |
| 13 | .10742E+00 | .49160E-01 | .40100E-01 | .10510E+00 | .77448E-01 | .417416-01 | .57977E-02 | 27066E+00 |
| 6 | .70000E+00 | . 700 00E +00 | .80000E+00 | .80000E+00 | .74982c+00 | .10097E+00 | .58261c-01 | 75856E-U1 |
| 1 10 | .46529E+00 | .46773E+U0 | .45703£+00 | .45523E+UO | .46149E+00 | .99401E+00 | .41551E-03 | 90339E-02 |
| 14 | .50060E-01 | .000 u0E + 00 | .00000E+00 | .49100E-01 | .24806E-01 | .13052E-01 | .49797E-02 | 26466E+00 |
| 80 | • 60000E+00 | .60000E+00 | .70000E+00 | . 700 UOE +UO | .64985E+00 | .85672E-01 | .50056E-01 | 74860E-01 |
| 111 | .47631E+00 | .47647E+UO | .40837L+00 | .467/3E+00 | .47236E+00 | .99624E+U0 | .352116-03 | 14001E-03 |
| 14 | .49160E-01 | .000 u0E +00 | .00000E+00 | .48100E-01 | .243166-01 | .12991E-01 | .48882E-02 | 74861E-01 |
| 6 | .70000E+00 | .70000E+00 | .80000£+00 | . 80000E+00 | .74982E+00 | .10004E+00 | .55916E-01 | 27066E+00 |
| 112 | .46773F+00 | .46837E+00 | .45826E+00 | .45703E+00 | .46302E+00 | .99484E+00 | .34946E-03 | 69016E-03 |



| | | | | | | | | • | | | | | |
|------|--|--|--|--|--|--|--|--|--|--|--|--|--------------------------|
| 973 | 15883E+U0 | 19703E+01 | 18954E+01 | 14302E+00 | 12539E+00 | 83314E+00 | 80654E+00 | 11163E+00 | 10341E+00 | 47637E+00 | -,46315E+00 | 97042E-01 | 93445E-U1 |
| | 193U7E+U1 | 16172E+00 | 15974E+00 | 19524E+01 | 82417E+00 | 14033E+00 | 12436E+00 | 84157E+00 | 47041E+00 | 11144E+00 | -,10259E+00 | 48170E+U0 | 35428E+U0 |
| | .54269E-01 | 15495E+00 | 34037E+00 | 30608E-01 | .46672E-01 | 21452E+00 | 18447E+00 | .53465E-02 | .29912E-01 | 11671E+00 | -,88188E-01 | .99147E-U2 | .14861E-U1 |
| C.21 | .97532e-02 | .95575e-02 | .11826E-01 | .11570E-01 | .10306E-01 | .100c8E-01 | .11553E-01 | .11275E-01 | .91384e-02 | .89129E-02 | .96231E-02 | .93816E-02 | .74020E-02 |
| | .71152e-01 | .70725e-01 | .80704E-01 | .80198E-01 | .75945E-01 | .75697E-01 | .80700E-01 | .80262E-01 | .71502e-01 | .71298E-01 | .72786E-01 | .72444E-01 | .648/7E-01 |
| | .47754e-02 | .40322E-02 | .67383E-02 | .65053E-02 | .24193E-02 | .23574E-02 | .29167E-02 | .28341E-02 | .12157e-02 | .11887E-02 | .13034E-02 | .12720E-02 | .711/5E-03 |
| 214 | .95368E+00 | .945 93 E + 0 0 | .81614E+00 | .41074E+00 | .64938E+00 | .64617E+00 | .513266+00 | .51123E+00 | .40852E+U0 | .40719E+00 | .32939E+00 | .32843E+U0 | .20614c+00 |
| | .22618E+00 | .257 92 E + 0 0 | .20308E+00 | .23283E+00 | .17592E+00 | .20125E+00 | .156786+00 | .17958E+00 | .14306E+U0 | .16393E+00 | .13454E+00 | .15422E+U0 | .12853c+00 |
| | .19835E+00 | .1967 4 E + 0 0 | .54070E+00 | .53712E+00 | .73984E+00 | .73619E+00 | .843796+00 | .84047E+00 | .90147E+00 | .89851E+00 | .93456E+00 | .93185E+U0 | .95533c+00 |
| 47 | .89515E+00 .84978E+00 .40532E-01 | .87019E+00 .94974E+00 .45236E-01 | .85347E+00 .84978E+00 .14136E+00 | .82968E+U0 .94974E+U0 .13742E+U0 | .70335E+00 .84978E+00 .22312E+00 | .70151E+U0 .94974E+00 .21690E+U0 | .69646E+U0 .84978E+U0 .28625E+U0 | .6/704E+00 .949/4E+00 .27627E+00 | .60651E+00 .84978E+00 .33458E+00 | .58960c+00 .94974c+00 .32525E+00 | .52034E+00 .84978E+00 .36910L+00 | .50503E+00 .94974E+00 .35E81E+00 | .44001E+30 .84978E+60 |
| 4-7 | .693 t3: +00 | .86603E+00 | .8/393r+00 | .84750L+00 | .810/7E+00 | .706261+00 | .73550E+00 | .71326£ +00 | .63926E+00 | .61993E+00 | .55794E+UO | .54107£+00 | .40917E+00 |
| | .900 t0t +00 | .10000E+01 | .90000E+00 | .10000E+01 | .900C0E+00 | .100005+01 | .90000E+00 | .10060£ +01 | .90000E+00 | .10000E+01 | .9UO UOE+UO | .100c0£+01 | .90000E+00 |
| | .000 t0t + 00 | .00000E+00 | .91850r-01 | .89080E-01 | .18718E+00 | .101522+00 | .25325E+00 | .24559£ +00 | .31179E+00 | .30236E+00 | .34864E+UO | .33810£+00 | .37973L+00 |
| 7.3 | .8/3932+00 | .84750E+00 | .81077L+00 | .70626E+00 | .73550£+00 | .71326E+U0 | .63926E+U0 | .619932+00 | .5J794E+60 | .541072+00 | .40917L+U0 | .47498L+00 | .33937E+JO |
| | .900002+00 | .10000E+01 | .90000E+00 | .10000E+01 | .90000£+00 | .1U000E+U1 | .9U0UUE+U0 | .100002+01 | .96000E+00 | .100002+01 | .5v0U0L+u0 | .10000L+01 | .9JOUGE+UO |
| | .918002-01 | .87080E-01 | .10718E+00 | .1dlb2E+00 | .20325£+00 | .24559E+U0 | .31179E+U0 | .302352+00 | .34304E+00 | .33410E+00 | .37973L+U0 | .30844L+00 | .39737L+UO |
| 77 | .89691E+00 | .87343E+00 | .83210E+U7 | .81077E+U0 | .75464E+00 | .73550E+U0 | .65607E+00 | .63926E+00 | .57262E+00 | .557945+00 | .481512+00 | .46917E+00 | . 40908E+00 |
| | .80000E+00 | .90000E+00 | .800v0E+U0 | .9U0U0E+U0 | .80960E+00 | .90000E+U0 | .80000E+00 | .90000E+00 | .30000E+00 | .90000E+00 | .80000E+00 | .900v0E+00 | . 80000E+00 |
| | .94270E-01 | .91850E-01 | .19210E+U0 | .18718E+U0 | .25991E+00 | .25325E+U0 | .31999E+00 | .31179E+00 | .35761E+00 | .34464E+00 | .38992E+00 | .37993E+00 | . 40968E+00 |
| 2.1 | .91652E+00 | .89303E+60 | .89691E+00 | .87393£+U0 | .83210E+00 | .81077E+00 | .75484E+00 | .73550E+00 | .65607E+00 | .63926E+00 | .57262E+00 | .55794E+30 | .45151E+00 |
| | .80000E+00 | .90000L+00 | .84000E+00 | .90000£+00 | .80000E+00 | .90000E+00 | .80000E+00 | .90000E+00 | .80000E+00 | .90000E+00 | .80000E+00 | .900C0L+09 | .80000L+00 |
| | .00000E+00 | .00000E+00 | .94270E-01 | .91850£-01 | .19210E+00 | .18718E+00 | .25991E+00 | .25325E+00 | .31999E+00 | .31179E+00 | .35781E+00 | .34864E+60 | .38992E+00 |
| ۵. | 11 113 | 1 12 114 | 2 11 115 | 2 12 116 | 3 11 117 | 3 12 118 | 4 11 119 | 4 12 120 | 5 11 121 | 5 12 122 | 6 11 123 | 6 12 124 | 7 11 125 |

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| 36080E+00 | 97270E-01 69119E-01 | 35124E+U0 933U2E-01 509b5E-01 | 90772E-01 36324E+00 .75268E-02 | 89694E-01 30818E+00 .13815E-01 | 31483E+00 91289E-01 41935E-01 | 30647E+00 88974E-01 28412E-01 | 88006E-01 31587E+00 .56902E-02 | 87392E-01 28457E+00 .99345E-02 | 29102E+00 87909E-01 23462E-01 | 24409E+U0 86972E-U1 146U2E-U1 | 86678E-01 29133E+00 .32386E-02 | 86052E-01 27709E+00 .37690E-02 | 28423E+00 86138E-01 96325E-02 |
|---------------|-----------------------------|--|--|---|--|--|--|--|---|--|--|---|---|
| •72142E-02 | .64724L-01 | .67228E-02 .62451E-01 .62211E-03 | .65515E-02 .62313E-01 .61141E-03 | .71380E-02 .63308E-01 .61310E-03 | .69555E-02 .63072E-01 .60265E-03 | .56398E-02 .54790E-01 .46459E-03 | .54949E-02 .5x670E-01 .45820E-03 | .61611E-02 .5y8b0E-01 .48797E-03 | .60025E-02 .59641E-01 .40017E-03 | .50231E-02 .50752E-01 .39655E-03 | .46942E-02 .56620E-01 .39263E-03 | .56708E-U2 .50047E-01 .43715E-03 | .55247E-02 .57812E-01 .43210E-03 |
| .20544E+00 | .14733E+UU .9524UE+UU | .21858E+00 .12400E+00 .96781E+00 | .21803E+00 .14308E+00 .96540E+00 | .17491E+00 .12191E+00 .97701E+00 | .17446E+00 .13988E+00 .97468E+00 | .13653E+00 .11948E+00 .98336E+00 | .13622E+00 .13754E+00 .98109E+00 | .10258E+00 .11847E+00 .98764E+00 | .10237E+00 .13596E+00 .98541E+00 | ./11/1E-01 .11748E+00 .99052E+00 | .71105E-01 .13403E+00 .98831E+00 | .41704E-01 .11694L+00 .99226E+00 | .41540E-01 .13414E+00 .99009E+00 |
| .42774E+UU | .94974E+00 .30379L+00 | .37211c+90 .84978c+00 .41200£+00 | .36174E+00 .94974E+00 .40051E+00 | .30471E+00 .84978E+00 .42559E+00 | .29621E+00 .94975E+00 .41372E+00 | .24210E+00 .84978E+00 .43568E+00 | .23535e+00 .94974E+00 .42353e+00 | .18395E+00 .84978E+00 .44269E+00 | .17882E+00 .94974E+00 .43035E+00 | .12864L+00 .84978E+00 .44764E+00 | .12505E+00 .94975E+00 .43516E+00 | .75624E-01 .84978E+U0 .45061E+U0 | .73516E-01 .34974E+00 .43505E+00 |
| . 454 38E +00 | . 100 c0 c + c1 | .39937E+00 .90000E+00 .39937:+00 | .367.002+00 .100006+01 .367.00.+00 | .33515E+00 .90300E+00 .41308E+00 | .325 u2E+00 .100 u0E+01 .40136L+00 | .26632L+v0 .9v0v0E+v0 .42620L+v0 | .25826E+UU .10000E+U1 .41331E+U0 | .21158E+00 .90000E+00 .43380E+00 | .20518E+00 .10000E+01 .42068E+00 | .15152E+60 .9000E+00 .44004E+00 | .14694E+00 .10000E+01 .426/3L+00 | .10241L+00 .900.00E+09 .44357E+00 | . 99310c-01 .10600E+01 .43016c+00 |
| 00+305705. | .10000E+01 .30730E+00 | .33515L+00 .90000E+00 .41308E+00 | .325u2e+u0 .1u0u0e+u1 .4u136L+u0 | .20632E+00 .90000E+00 .42620E+00 | .25826E+v6 .10000L+01 .41331L+00 | .21158E+00 .900C0E+00 .45380E+00 | .2.518c+00 .100006+01 .4206de+00 | .10152E+00 .90000E+00 .44004E+00 | .146,44L+00 .10000L+01 .426/3E+00 | .10241E+00 .4000E+00 .44357E+00 | .99310E-01 .10000E+01 .43016E+00 | . 408/0c=01 . 40000c+00 . 445/0c+00 | .4J4D0L-01 .1J000E+01 .4J242E+06 |
| .39937L+UU | . 900001 +00 . 39937 +00 | .34397c+00 .80000c+00 .42476c+00 | .335158+00 .90000E+00 .41338E+00 | .273.2E.+00 .800.0E.+00 .43741L.+00 | .265.32E+00 .90000E+00 .42620E+00 | .21714E+00 .80000E+00 .445.1E+00 | .211562+00 .900306+00 .433302+00 | .15550E +00 .80000E +00 .451612+00 | .15152£+u0 .90000c+u0 .44004£+u0 | .10510E+00 .90000E+00 .45523E+00 | .102412+00 .90000c+00 .44357E+00 | .43100E-01 .80000E+00 .45763E+00 | .46870E-01 .90900E+00 .44550E+00 |
| *46917E+U0 | .90060E+00 .37993E+00 | .40988E+00 .80000c+00 .40988E+00 | .39957E+00 .90000E+00 .39937E+00 | .34397E+00 .80000E+00 .42476E+00 | .33515L+CO .900v0E+CO .41388E+OO | .27332E+09 .800c0E+00 .43741c+00 | .26632E+00 .90000E+00 .42620E+00 | .21714E+00 .800C0E+00 .44521E+00 | .21158E+00 .9U000L+00 .433E0L+60 | .15550E+00 .8C000E+00 .45161L+00 | .15152E+60 .90000E+60 .44004E+00 | .105106+00 .80000E+00 .45523L+00 | .162416+00 .900006+00 .443576+00 |
| 7 | 12 126 | 8 11 127 | 8 12 128 | 9 11 129 | 9 12 130 | 10 11 131 | 10 12 132 | 11 11 133 | 11 12 .134 | 12 11 135 | 12 12 136 | 13 11 137 | 13 12 138 |



| 27705E+00 855A2E-01 | 17241E-U2 | 85565E-U1 28422E+00 22173E-02 | 18265E+U0 20237E+U1 .74322E-U1 | 20795E+U1 18759E+U0 20849E+U0 | 19718E+01 19478E+00 45905E+00 | 16524E+00 20585E+01 30669E-01 | 14684E+00 87831E+00 .67158E-01 | 84764E+U0 17359E+U0 29497E+U0 | 84725E+00 15385E+00 25303E+00 | 13067E+00 90333E+00 .11636E-01 | 12288E+00 50209E+00 .44606E-01 | 50818E+00 13726E+00 15997E+00 | 48886E+U0 12523E+U0 121U2E+U0 |
|--------------------------|------------|---|--|--|--|--|---|---|--|--|--|---|--|
| .47816E-02 | .3/342E-03 | .46583E-02 .55594E-01 .36915E-03 | .93353E-02 .70273E-01 .45329E-02 | .90835E-02 .69825E-01 .43481E-02 | .11279E-01 .79621E-01 .63010E-02 | .10951E-01 .79005E-01 .60008E-02 | .97965E-U2 .75410E-01 .23454E-U2 | .94885E-02 .75096E-01 .22600E-02 | .10956E-01 .79746E-01 .27911E-02 | .10595E-01 .79164E-01 .20819E-02 | .86547E-02 .71050E-01 .12103E-02 | .83617e-02 .70777e-01 .11756E-02 | .91057E-02 .72044E-01 .12803L-02 |
| .12966E-01 | .99308E+00 | .12840E-01 .13382E+00 .99092E+00 | .93643E+U0 .29185E+U0 .19474E+U0 | .92479E+00 .328.2E+00 .19229E+00 | .80410E+00 .26391E+00 .53270E+00 | .79588E+00 .29759E+00 .52727E+00 | .64218E+00 .22859E+00 .73168E+00 | .63726E+00 .25845E+00 .72602E+00 | .50875E+00 .20417E+00 .83635E+00 | .50562E+00 .231c2E+00 .831c0E+00 | .40552E+00 .18655E+00 .89465E+00 | .40339E+U0 .21149E+U0 .89025E+U0 | .32723E+00 .17566E+00 .92849E+00 |
| .23744E-01 .84978E+00 | .45210E+00 | .23042E-01 .94974E+00 .43949E+60 | .84159E+00 .10497E+01 .43750E-01 | .80896E+00 .11496E+01 .42052E-01 | .80241E+00 .10497E+01 .13290E+00 | .77130E+00 .11496E+01 .12775E+00 | .73648E+00 .10497E+01 .20977E+00 | .70793E+00 .11496E+01 .20154E+00 | .65479E+00 .10497E+01 .20912E+00 | .62940c+00 .11496c+01 .25869c+00 | .57022E+00 .10497E+01 .31456E+00 | .54611c+00 .11496c+01 .30236c+00 | .46921E+60 .10497E+01 .34701E+00 |
| . 468 70E-01 | .44570E+00 | .45450e-01 .100c0E+01 .43242E+00 | .83516E+00 .11000E+01 .00000E+00 | .80000c+00 .12000c+01 .00000c+00 | .817500+00 .11000c+01 .85900c-01 | .762896+60 .120006+01 .822606-01 | .75824L+00 .11000E+01 .17505E+00 | .72631E +00 .12000E+01 .16768E+00 | .667.4E+00 .11000E+01 .236.4E+00 | .65858L+00 .12000L+01 .22637L+00 | .59784E+00 .11000E+01 .29159E+00 | .572072+00 .120002+01 .27931E+00 | .>21/9E+00 .11000E+01 .32605E+00 |
| 0000000. | .44651E+U0 | .0000000+00 .100000+01 .43301e+00 | .81730E+60 .11060E+01 .85900E-01 | .78289e+00 .12000e+01 .82280e-01 | .758242+00 .11000=+01 .17505E+00 | .72631E+00 .120002+01 .10768E+00 | .6 J784E+00 .11000E+01 .23684E+00 | .658888+00 .12000E+01 .22657E+00 | .547846+00 .110006+01 .291596+00 | .5/267E+U0 .12000E+U1 .2/931E+U0 | .521792+00 .11000c+01 .326052+00 | .49942:+00 .12000c+01 .312.22:+00 | .4387/c+00 .116006+01 .33531c+00 |
| . 000 00E +00 | .45326E+00 | .00000E+00 .90000E+00 .44651E+00 | .84750E+U0 .1U0U0E+U1 .89060E-U1 | .81730c+00 .11000c+01 .85900t-01 | .78626E+00 .10000E+01 .18152E+00 | .75824E+00 .11000E+01 .1755E+00 | .71326E+00 .10000E+01 .24559E+00 | .68764E+00 .11000E+01 .23684E+00 | .61993E+00 .10000E+01 .302s6E+00 | .59784E+00 .11000E+01 .29159E+00 | .54107E+00 .10000E+01 .33810E+00 | .521791+00 .110v01+01 .32605±+00 | .45498E+U0 .1U9U0E+U1 .35844E+U0 |
| .48100E-01 | .45763E+U0 | .46870E-01 .900u0E+60 .44590E+00 | .86603E+60 .10000E+01 .00000E+00 | .83516E+00 .11000E+01 .00000E+03 | .84750±+00 .10000±+01 .89980E-01 | .81730E+00 .11000E+01 .85900E-01 | .78626E+09 .10000E+01 .18152E+00 | .75824E+00 .11000E+01 .17505E+00 | .71326E+00 .10000E+01 .24559E+00 | .68784E+00 .11000E+01 .23684E+00 | .61993E+60 .10000E+01 .30236E+00 | .59784E+00 .11000E+01 .29159E+00 | .54107E+60 .10000E+01 .33810E+03 |
| 14 | 39 | 14 12 40 | 1 13 41 | 1 14 42 | 2 13 43 | 2 14 44 | 3 13 45 | 3 14 46 | 4 13 | 4 14 48 | 5 13 49 | 5 50 | 6 13 51 |



| 11502E+00 | 11220E+00 | 38639E+00 | 37270E+00 | 10878E+00 | 10727E+00 | 33599E+U0 | 32403E+00 | 10532E+00 | 10501E+00 | 31245E+00 | 30043E+00 | 10418E+00 |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|---|-----------------|-----------------|-----------------|-----------------|-----------------|
| 51813E+00 | 37851E+00 | 11872E+00 | 11332E+00 | 39126E+00 | 32650E+00 | 11019E+U0 | 10716E+00 | 33787E+00 | 30131E+00 | 10592E+00 | 10464E+00 | 31293E+00 |
| .18433E-01 | .30637E-01 | 92806E-01 | 68153E-01 | .16074E-01 | .21138E-01 | 58258E-U1 | 39703E-01 | .95512E-02 | .14596E-01 | 31981E-01 | 17898E-01 | .35531E-02 |
| .87920E-02 | .69998E-02 | .67567E-02 | .63562E-02 | .61337E-02 | .67467E-02 | .65093E-02 | .53293E-02 | .51410E-02 | .58214E-02 | .50160E-02 | .47464E-02 | .45778E-02 |
| .71597E-01 | .64546E-01 | .64357E-01 | .62163E-01 | .61997E-01 | .62805E-01 | .62513E-01 | .58534E-01 | .58400E-01 | .59400E-01 | .59147E-01 | .56480E-01 | .50340E-01 |
| .12457E-02 | .73579E-03 | .71938E-03 | .64975E-03 | .63609E-03 | .63582E-03 | .62252E-03 | .49586E-03 | .48844E-03 | .51826E-03 | .51045E-03 | .43316E-03 | .42784E-03 |
| .32576E+00 | .2 6464E+00 | .26350E+00 | .21726E+00 | .21642E+00 | .17393£+00 | .173296+00 | .13585E+00 | .13538E+00 | .10212E+00 | .10176E+00 | .70895e-01 | .70558E-01 |
| .19917E+00 | .16783E+00 | .19045E+60 | .16300E+00 | .18504E+00 | .15933E+00 | .18086+00 | .15668E+00 | .17786E+00 | .154d5E+00 | .175x6E+00 | .15302e+00 | .17448E+00 |
| .92423E+00 | .94903E+00 | .94567E+00 | .96241E+00 | .958blE+00 | .97178E+00 | .968126+00 | .97826E+00 | .97470E+00 | .98265E+00 | .97914E+00 | .98558E+00 | .982i3E+00 |
| .47024E+00 | .41368E+00 | .39765E+00 | .34985E+00 | .33629E+00 | .28647E+00 | .27537E+00 | .22762E+00 | .21879L+00 | .17294E+00 | .16624E+00 | .12094E+00 | .11625E+30 |
| .11496E+01 | .10497E+01 | .11496E+01 | .10497E+01 | .11496E+01 | .10497E+01 | .11496E+01 | .10497E+01 | .11446E+01 | .10497E+01 | .11496E+01 | .10497L+01 | .11496E+01 |
| .33356E+00 | .37118E+00 | .35679L+00 | .38735E+00 | .37233E+00 | .40012E+00 | .35401E+00 | .40961E+00 | .39373E+00 | .41620E+00 | .40007E+00 | .42086L+00 | .40454E+00 |
| .49902E+UU | .43877E+00 | .42030E+00 | .37350E+00 | .35777k+00 | .31343E+00 | .30024E+00 | .249 c6 + + + + + + + + + + + + + + + + + + | .23857E +u0 | .19787E+00 | .169542+00 | .14170k+00 | .135/36+00 |
| .12U-UE+U1 | .11000E+01 | .12000E+01 | .11000E+01 | .12000k+01 | .11000E+01 | .12600E+01 | | .12006E+J1 | .11000E+01 | .12000E+01 | .11060k+01 | .12000c+01 |
| .31232E+U | .35531E+00 | .34035E+00 | .37350E+00 | .35777k+00 | .38706E+00 | .37076L+00 | | .38180E+U0 | .46509E+00 | .388012+00 | .41153k+00 | .39420c+00 |
| .42030L+00 | .37350±+00 | .35777E+00 | .31343E+00 | .30024E+60 | .249666+00 | .23857±+00 | .19787£+00 | .18954E+00 | .141/0c+00 | .13573£+00 | .95770E-01 | .91740c-01 |
| .12000E+01 | .11600±+01 | .12000E+01 | .11000E+01 | .12000E+01 | .11000c+01 | .12000E+01 | .11000E+01 | .12000E+61 | .11000c+01 | .12000£+01 | .11000E+01 | .12000c+01 |
| .34035E+00 | .37350±+00 | .35777E+00 | .34706E+00 | .37076E+00 | .39858E+00 | .30100L+00 | .40569E+00 | .36861E+00 | .41153k+00 | .33426£+00 | .41403E+00 | .39735E+00 |
| .43877E+UO | .38730E+00 | .37350E+U0 | .32502£+00 | .31343E+00 | .25826E+00 | .24906E+00 | .20518E+00 | .19787E+U0 | .14694e+00 | .14170c+00 | .99310E-01 | .95770E-01 |
| .110UOE+U1 | .100v0E+01 | .11000L+J1 | .10000£+01 | .11000E+01 | .10000E+01 | .11000E+01 | .10000E+01 | .11000E+U1 | .10666+01 | .11000c+01 | .10000E+01 | .11000c+01 |
| .35531E+UO | .38730£+00 | .37350L+U0 | .40136£+00 | .38706L+00 | .41331E+00 | .39658E+00 | .42068E+00 | .40509E+U0 | .42673L+00 | .41153c+00 | .43016E+00 | .41463E+00 |
| .52179E+U0 | .45498E+00 | .43877E+00 | .36730E+00 | .37350£+00 | .32502E+00 | .31343E+00 | .25826E+00 | .24966E+00 | .20518E+00 | .19767£+00 | .14694E+69 | .141706+00 |
| .11000E+01 | .10000E+01 | .110C0E+01 | .10000E+01 | .11000£+01 | .10000E+01 | .11000E+01 | .100C0E+01 | .110006+01 | .100c0E+01 | .11000£+01 | .10000E+01 | .110006+01 |
| .32605E+00 | .36844E+00 | .35531E+60 | .38730E+00 | .37350£+00 | .40136E+00 | .38706E+00 | .41331E+00 | .39858E+00 | .42n68E+03 | .40569£+00 | .42573E+00 | .411536+00 |
| 6 14 152 | 7 13 153 | 7 14 154 | 8 13 155 | 8 14 156 | 9 13 157 | 9 14 158 | 152 153 | 10 14 160 | 11 13 161 | 11 14 162 | 12 13 163 | 12 14 104 |



| 12933E-02 | .40660E-03 | .98480E+00 | .40857E+00 | .39945E+00 | . 400000 | .41758E+00 | .41701E+00 | 168 |
|------------|-------------|------------|------------|----------------|-------------|---------------|------------|-----|
| 30357E+00 | .55250E-01 | .17319E+U0 | .11496E+01 | .12000r+01 | .12000r +01 | .11000E+01 | .11000E+01 | 14 |
| 10337E+00 | .43567E-02 | .128546-01 | .21456E-01 | .41900E-U1 | • 60000E+00 | .00000E+00 | .43830E-01 | 14 |
| 37618E-02 | .41069E-03 | .98822E+00 | .42505E+00 | • 41701E+00 | .41758E+v0 | .433 UIE +UO | .43242E+00 | 167 |
| 10339E+00 | .55421E-01 | .15253E+00 | .10497E+U1 | .110 v0L +v1 | .11000E+01 | .10000E+01 | .10000E+01 | 13 |
| 29321E+00 | .45172E-02 | .12840E-01 | .22322£-01 | .43830E-01 | .00000E+00 | . 00000E + 00 | .45450E-01 | 14 |
| 13463E-01 | .46392E-03 | .983946+00 | .40723E+00 | .39736E+00 | .34945E+UO | .41701E+00 | .41483E+00 | 166 |
| 10386E+U0 | .5 /293E-01 | .17364E+00 | .11496E+01 | .12000E+01 | .1-000L+U1 | .11000E+U1 | .11000E+01 | 14 |
| 30358E+U0 | .516794-02 | .41312E-01 | .68341E-01 | .91740E-U1 | .41900E-01 | .43830L-01 | .95770E-01 | 13 |
| •76684E-U2 | .47113E-03 | .98737E+00 | .42365E+00 | .414c3E+00 | .41701E+00 | .43242E+U0 | .43016E+00 | 165 |
| 29333E+00 | .57556E-01 | .15291c+00 | .10497E+01 | •110 cu = + u1 | .11000E+01 | .10000E+01 | .10000E+01 | 13 |
| 10373E+U0 | .53576E-02 | .41436E-01 | .71098E-01 | .95770E-UI | .43830k-Ul | .45450L-UI | .99310E-01 | 13 |



| 975 975 | 22103E+00 21565E+01 .10084E+00 | 22359E+U1 22951E+UU 28226E+UO | 20778E+01 25177E+00 61434E+00 | 20059E+00 22108E+01 39262E-01 | 18219E+00 96117E+00 .99881E-01 | 96919E+00 22998E+00 40906E+00 | 90666E+00 20387E+00 34590E+00 | 16206E+00 99884E+00 .26612E-01 | 15546E+00 55061E+00 .70403E-01 | 55702E+00 18187E+00 22485E+00 | 52634E+00 16421E+00 16638E+00 | 14536E+00 57580E+00 .33798E-01 | 14331E+U0 41212E+U0 .47916E-U1 |
|---|---|--|--|---|---|--|--|--|--|---|--|--|---|
| FL C21 | .88015E-02 .69428E-01 .42490E-02 | .84851E-02 .69143E-01 .40165E-02 | .10580e-01 .78372e-01 .5/658e-02 | .10164E-01 .77785E-01 .53842E-02 | .91410E-02 .74789E-01 .22799E-02 | .87481c-02 .74543E-01 .21815E-02 | .10186E-01 .78546E-01 .26543E-02 | .97244E-02 .77931E-01 .25144E-02 | .80298E-02 .70502E-01 .12288E-02 | .76538E-02 .70265E-01 .11866E-02 | .84364E-U2 .71125E-U1 .12885E-U2 | .80337E-02 .70660E-01 .12384E-02 | .64810L-02 .641/3L-01 .70457L-03 |
| 777 | .91027E+00 .36822E+00 .16927E+00 | .89197E+00 .41232E+00 .18544E+00 | .78560E+00 .33459E+00 .52046E+00 | .77249E+00 .37595E+00 .51177E+00 | .63103E+00 .29154E+00 .71869E+00 | .62296E+00 .32895E+00 .70973E+00 | .501u2E+U0 .26133E+U0 .824u7E+U0 | .49645E+00 .29558E+00 .81619E+00 | .400/6E+00 .23933E+00 .86437E+00 | .397.30E+00 .2/118E+00 .87670E+00 | .32384E+00 .22557E+00 .91843E+00 | .32132E+00 .25581E+00 .91176E+00 | .26266E+00 .21581E+00 .94061c+00 |
| 4 × × × × × × × × × × × × × × × × × × × | .7/179E+00 .12496E+01 .40119E-01 | .72939E+00 .13495E+01 .37915E-01 | .73587E+00 .1249bE+01 .12108E+00 | .69544E+00 .13495E+01 .11518E+00 | .67540E+00 .12496E+01 .19236E+00 | .63829E+00 .13495E+01 .15181E+00 | .60049E+00 .12496E+01 .24601E+00 | .56749E+00 .13495E+01 .23325E+00 | .52293E+00 .12496E+01 .25847E+00 | .49420E+00 .13495E+01 .27262E+00 | .44864E+00 .12496E+01 .31823E+00 | .42399£+00 .13495£+01 .30075£+00 | .37938E+0U .12496E+01 .34039E+00 |
| 7 | .75993E +00 .13000E+01 .00000E+00 | .71414E+00 .14000E+01 .00000E+00 | .74308E+60 .13000E+01 .78160c-01 | .69887E+00 .14000E+01 .73450E-01 | .68994E+00 .13000E+01 .15928E+00 | .64836c+00 .14000E+01 .14969E+00 | .62588E+00 .13000E+01 .21551E+00 | .56817E+00 .14000E+01 .20252E+00 | .54399£+00 .13000£+01 .20532£+00 | .51121c+00 .14000E+01 .24933c+00 | .47479E+U0 .130CUE+U1 .290G8E+U0 | .44613E+00 .14000E+01 .27866L+00 | . 3%925£+00 .135050£+01 .3235£+03 |
| 7.3 23 | .74368c+00 .15000c+01 .70160c+01 | .69837E+00 .14000E+01 .73450E-01 | .68994E+00 .13000L+01 .19928E+00 | .64836E+00 .14000E+01 .14969E+00 | .6258884.00 .130008+01 .215518+00 | .58817E+00 .14000E+01 .20252E+00 | .54399E+00 .13000E+01 .20532E+00 | .51121E+00 .14000E+01 .24933E+00 | .4/479E400 .13000E+01 .2/608E+00 | .44618L+00 .14000E+01 .27330E+00 | .39925E+00 .13000E+01 .32330E+00 | .37519L+00 .14000L+01 .30362E+00 | .33905e+vO .13960e+v1 .3.205e+vO |
| 72 | .78289E+U0 .12000E+U1 .82240E-U1 | .74308E+UO .130U0E+U1 .78100L-U1 | .72631E+00 .12000£+01 .10708E+00 | .68994E +00 .13000E+01 .15928E+00 | .65888E+00 .12000e+01 .22687E+00 | .62558E+00 .13000E+01 .21551E+00 | .57267E+00 .12000E+01 .27931E+00 | .54399E+00 .13000E+01 .20532E+00 | .49982E+00 .120u0E+01 .31232E+00 | .47479E+00 .13000E+01 .29608E+00 | .42030E+00 .12000E+01 .34035E+00 | .39925E+00 .13000E+01 .32330E+00 | .357778+00 .120008+01 .35777e+00 |
| Y1 Z1 | .80000E+00 .12000E+01 .00000E+00 | .75993E+00 .13060E+01 .00060E+00 | .76289E+U0 .120U0E+U1 .8228GE-01 | .74368E+U0 .13000E+01 .78160E-01 | .72631E+00 .12000E+01 .16768L+00 | .68994E+00 .130C0E+01 .15928E+00 | .65888E+00 .12000E+01 .22687E+00 | .62568E+00 .13000E+01 .21551E+00 | .57267e+00 .12000e+01 .27931e+00 | .54399E+00 .13000E+01 .26532E+00 | .49982E+00 .12000E+01 .31232E+00 | .47479E+00 .13000E+01 .29668E+00 | .42030E+00 .120C0E+01 .34035E+00 |
| Zα | 1 16 169 | 1 17 170 | 2 16 171 | 2 17 172 | 3 16 173 | 3 17 174 | 16 175 | 4 17 176 | 5 16 177 | 5 17 178 | 6 16 179 | 6 17 180 | 7 16 181 |



| 42259E+00 | 131575E+UU | 00.57.7.7. | 40140E+00 | 14729E+00 | 94692E-01 | 13868E+U0 | 431d4E+00 | .20727E-U1 | 13842E+00 | - 455 42F+00 | .34304E-01 | 36873E+00 | 14351c+UO | 80040E-U1 | - 350b2F+00 | 13952E+00 | 54726E-U1 | | 13613E+00 | 37236E+00 | .17787E-U1 | 13587E+U0 | 32739E+U0 | .213146-01 | 34181E+U0 | 13767£+U0 | 46238E-U1 | 32581E+U0 | 13538E+00 | 26605E-U1 | 13437E+00 | 34289E+00 | .10203E-01 | 13305E+UO | 31497E+U0 | .10015E-U1 | | 33052E+00 | -134046+00 -134046+01 | 10 - 10 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 |
|-------------|--|------------|------------|----------------|-------------------|------------|------------------|------------|------------|---------------|-------------|-------------|------------|-------------|-------------|---------------|------------|---------|--------------|---------------|------------|------------|------------|-------------|------------|------------|------------|------------|------------|-------------|------------|-------------|------------|------------|------------|------------|--------|-------------------------|--------------------------|---|
| .61677E-02 | .70507F-03 | | .56807E-02 | -61842E-01 | •/UZUDE-U3 | .559406-02 | .61722E-01 | .68723E-03 | •62399E-02 | . 672175-01 | .6 ×128E-03 | .54341E-02 | •61940E-01 | ·67611E-03 | .49275E-02 | .56277F-01 | .50262k-03 | | .46854E-02 | .58196E-01 | .55447E-03 | .53822E-02 | | .581306-03 | .511666-02 | .58662E-01 | .5/120k-u3 | .43872E-02 | .50217£-01 | .50162E-03 | .41712E-02 | .50132E-01 | .44711E-03 | .49522E-02 | .57032E-01 | .5337E-03 | | .4/06/E-02 50/46E-01 | 10-346-01 | ・フトラフィーショ |
| .20021E+00 | 001710173 | | .21535E+U0 | 00+321602 | • 45375E+00 | .21397E+U0 | .2 3 d U5 E + 00 | .94739E+00 | .17251E+00 | 205046+00 | .96343E+00 | .17137E+U0 | .23206E+00 | .95729E+U0 | .13475E+UO | .20107F+00 | .97014E+U0 | 3 6 | •13372E+00 | .22914E+00 | .90414E+UO | .10126E+00 | .19939E+00 | .974672+00 | .10005E+00 | .22659E+00 | .968788+00 | .702036-01 | .19/02E+U0 | .977/2E+UO | .698866-01 | .224/6E+00 | .971906+00 | .41092E-01 | .19692E+U0 | .97956E+U0 | | .40792E-01 | .973516+00 | 00.1400 |
| .30653E+00 | • 36169E+30 | | .320d4E+00 | * 124 90E * UI | •3226E+00 | .30321E+00 | .13495L+Ul | .33570E+UU | .26272E+30 | 174451 | . 30694E+00 | .24828E+00 | .13495E+Ul | .34678E+U0 | .208745+00 | .12496E+Ul | .37564E+30 | | •19728E+00 | .13495E+U1 | .35500E+00 | .15860E+U0 | .12496£+01 | .38169E+00 | .14989£+UO | .13495E+Ul | .36072E+U0 | .11091£+00 | .12496E+U1 | .38595E+00 | .10482£+00 | .13495E+01 | .30475E+00 | .65149c-01 | .12496E+Ul | .38d51E+00 | | • 61617E-01 | - 15495E+01 | 00.1-4-00. |
| .37519c+00 | 10000000000000000000000000000000000000 | | .33905E+00 | *130 CCE + CT | .339026+00 | .319376+00 | .140002+01 | .319576+00 | .20520E+00 | 1 40 00 + 401 | .35219E+UU | .20802E+00 | .14000E+01 | . 33077£+00 | .22003E+00 | .130 c0t + v1 | .36208c+00 | 6 | .21297E+UU | .14000E+01 | .34062L+00 | .18005t+00 | .13000E+01 | .36715E+00 | .16920£+00 | .14000t+v1 | .346>02+00 | .12874£+U0 | .13000E+01 | .3 74462+00 | .121176+00 | .140 JOE+01 | .35189c+00 | .87140c-ul | .13000L+01 | .377461+00 | | 10-405018 | 0.00 4 4 2 / 4 5 5 4 | 00.20-170 |
| . 319376+00 | .34937L+vC | | .20520c+00 | TO LO COLL | • 32214E+UU | .268921+00 | .14000L+01 | .32097E+00 | .226632+00 | 130001401 | .36266 +UG | .212971+00 | 0 | .34082E+00 | .15965£ +v0 | .13000c+01 | .30915E+00 | \$ • | . 10920L+00 | .14000E+01 | .34690E+00 | .128946+00 | .15000c+01 | .3 7446E+UO | .1<117E+00 | .14000L+U1 | .35169E+UU | .8/140E-J1 | .15000E+01 | .3/740E+UO | .81890r-01 | .14000E+01 | .35472E+00 | .39850t-01 | .13000r+01 | 3/4441+00 | | .37450E-01 | 00+1000+1• | 00.407070. |
| .33985E+00 | .33985E+UO | | 300246+00 | 12000E +01 | • 3 / U / OE + UU | .28520F+00 | .13000c+01 | .35219E+UO | .23857£+00 | -12000F+01 | .30160E+U0 | .22663t +00 | .13000c+01 | .362c8E+00 | .18954E+00 | .12000E+01 | .38861E+00 | | . 18005E +00 | • 13000E + 01 | •36915E+00 | .135736+00 | .12000E+01 | .39420£+00 | .12894E+U0 | .13000E+01 | .374466+00 | .91740E-U1 | .12000E+U1 | .39736E+UO | .87140E-01 | .13000£+01 | .37746E+UO | .419806-01 | .12000E+01 | .34945E+00 | 10.000 | . 14060F=01 . | 3 79446 +00 | |
| .39925E+00 | .32330E+00 | | .35777E+00 | •12000E+01 | • 35///E+UU | .33985E+UO | .13000E+01 | .33985E+00 | .30024E+U0 | 12000 +01 | .37076E+U0 | *58520E+00 | .13000£+01 | .35219E+00 | .23857E+00 | .12000E+01 | .38180£+00 | | .22663E+00 | .13000E+01 | .36268E+00 | .18954E+00 | .12000E+01 | .36861E+00 | .18005E+00 | .13000E+01 | .36915r+00 | .13573E+00 | .12000£+01 | •39420E+00 | .12894E+00 | .13000E+01 | ·37446E+00 | .91740E-01 | .12000E+01 | .39736E+00 | 0.150 | .14050F+01 | .37746F+U0 | 22.12.11 |
| 7 1 | 187 |) | ω, | 101 | 183 | 80 | 17 | 184 | 0 | 16 | 185 | 6 | 17 | 186 | 10 | 16 | 187 | • | 01 | 17 | 188 | 11 | 16 | 189 | 11 | 17 | 190 | 12 | 16 | 191 | 12 | 17 | 192 | 13 | 16 | 193 | , | 17 | 194 | |



| 314776+00 133866+00 665456-02 133846+00 | 43108E-02 26617E+00 23501E+01 .14072E+00 24694E+01 30123E+00 | 22254E+01 35177E+00 83269E+00 26111E+00 2438BE+01 | 24578E+00 10949E+01 .16084E+00 33719E+00 | 99472E+00 29853E+00 48726E+00 21846E+00 11594E+01 | 21683£+00 64115£+00 .11900£+00 64560£+00 26950£+00 33435£+00 58438£+00 24056£+00 |
|---|--|--|--|--|---|
| .41747E-02 .55095E-01 .47934E-03 .39664E-02 | .475226-03 .813056-02 .690966-01 .396336-02 .773216-02 .695056-01 | .90946E-02 .77337E-01 .51558E-02 .91642E-02 .77219E-01 | .83039E-02 .74446E-01 .22719E-02 .78003E-02 .74671E-01 | .92006E-02 .77396E-01 .25481E-02 .80037E-02 .77079E-01 | .72267E-02 .70134E-01 .13235E-02 .67384E-02 .70240E-01 .12781E-02 .75756E-02 .75756E-02 |
| .12936E-01 .19543E+00 .96043L+00 .12850E-01 .22317E+00 | .97469E+U0 .868.37E+U0 .46105E+U0 .18U57E+U0 .836.96E+U0 | .75541E+U0 .42246E+U0 .56047E+U0 .73233E+U0 .47777E+U0 | .61234E+00 .37202E+00 .69760E+00 .59769E+00 .42327E+00 | .48955E+U0 .33532E+00 .80492E+00 .47958E+00 .38320E+00 | .39269E+00 .30832E+00 .86645E+00 .3542E+00 .35342E+00 .85203E+00 .31778E+00 .29120E+00 |
| .20470c-01 .12496c+01 .33980c+00 .19346c-01 | .30834E+00 .68077E+00 .14494E+01 .35388E-01 .62447E+00 .15492E+01 .32401E-01 | .64408E+00 .14494E+01 .10751E+00 .59540E+00 .15492E+01 | .59574E+00 .14494E+01 .16969E+00 .54647E+00 .15492E+01 | .52966+00 .14494+01 .217706+00 .485866+00 .15492c+01 | .40126£+00 .14494£+01 .25445£+00 .42311£+00 .15492£+01 .23340£+00 .37572£+00 |
| .396cce-01 .150c01+01 .37944L+00 .37456-01 | . 356582 + 00 . 681442 + 00 . 150002 + 50 . 600002 + 50 . 16005 + 61 . 16005 + 61 | .047296+00 .150006+01 .68030c-01 .587176+00 .160006+01 | .600 > 1 & + + + + + + + + + + + + + + + + + + | .54476E+00 .15000E+01 .18758L+00 .49416E+00 .10000E+01 | .47348E+00 .1500GE+01 .23093E+00 .42950E+00 .15000E+01 .20948E+00 .413.5E+00 .15000E+01 |
| .000000.00 .1.0000.00.01 .37997c+00 .000000c+09 | .357072+00 .647294+00 .1,0002+01 .580304-01 .58717+00 .180001+01 | .60051E+60 .15005E+01 .13604E+00 .54473E+00 .10000E+01 | .544766+00 .150006+01 .157586+00 .494166+00 .100006+01 | .4/348E+00 .15000E+01 .23093E+00 .42950E+00 .15000E+01 | .41325E+00 .12000E+01 .22823E+00 .37437E+00 .10000E+01 .23424C+00 .34720E+00 .120000E+01 |
| . 120000 + 00 . 12000 + 01 . 40000 + 00 . 90000 + 00 . 13000 + 01 | .698.7E+00 .698.7E+00 .140.00.4.01 .7345.0E-01 .647.29E+00 .150.00E+01 .640.30E-01 | .64836E+00 .14000E+01 .14969E+00 .60051E+00 .13864E+00 | .58817E+U0 .1400C+U1 .20252E+U0 .54476E+U0 .150C0E+U1 | .51121E+00 .14500E+01 .24933E+00 .47348E+60 .15600C+01 | .44618E+00 .14000E+01 .27860E+00 .41325E+00 .15900E+01 .25823E+00 .37519E+00 .140000E+01 |
| .419anE-01 .120c0E+01 .39945E+00 .398H0E-01 | .37944E+00 .71414E+00 .14000E+00 .00000E+00 .66144E+00 .1500E+01 | .69887E+00 .14000E+01 .73450E-01 .64729E+00 .15000E+01 | .64836E+00 .14000E+01 .14969E+00 .60051E+00 .15000E+01 | .56817E+00 .140C0E+01 .20252E+00 .54476E+00 .150C0E+01 | .511211+00 .14000E+01 .24933E+00 .47348E+00 .15000E+01 .23093E+00 .44618E+00 .14000E+01 |
| 14 16 195 14 17 | 196 1 197 197 19 | 2 18 199 2 19 | 3 18 201 3 19 202 | 203 203 4 19 204 | 205 105 205 205 205 205 |



| 973 | 20233E+00 | 20403E+00 | 48379E+00 | 44625E+00 | 19676E+00 | 19874E+00 | 42200E+00 | 39066E+00 | 19497E+00 | 195 66E+00 | 34025E+00 | 36101E+00 | 19431E+00 |
|-------|-----------------|----------------|------------------|----------------|----------------|----------------|-------------|--------------------|-----------------|-----------------|-----------------|--------------------|-----------------|
| | 67455E+00 | 46721E+00 | 22947E+00 | 21442E+00 | 50302E+00 | 40001E+00 | 20970E+00 | 20234E+00 | 42941E+00 | 364 69E+00 | 19956E+00 | 19643E+00 | 39218E+00 |
| | .69448E-01 | .82230E-01 | 19957E+00 | 13549E+00 | .56076E-01 | .59023E-01 | 12250E+00 | 78740E-01 | .37772E-01 | .35498E-01 | 69416E-01 | 39005E-01 | .15952E-01 |
| C.2.1 | .70518c-02 | .5dllle-02 | .54023E-02 | .52670E-02 | .4 8941E-02 | .55866E-02 | .51874E-02 | .44092E-02 | .40929E-02 | .48145E-02 | .44674E-02 | .3 y 2 36 E - 0 2 | .30401E-62 |
| | .70033c-01 | .63967E-01 | .64107E-01 | .61693E-01 | .61850E-01 | .61730E-01 | .61667E-01 | .5a194E-01 | .58357E-01 | .50495E-01 | .50466E-01 | .5 c 1 c 3 E - 0 1 | .50207E-01 |
| | .13021c-02 | .91582E-03 | .89906E-03 | .83859E-03 | .82595E-03 | .82520E-03 | .81208E-03 | .70964E-03 | .70622E-03 | .72194E-03 | .71696E-03 | .6 5 2 y 1 E - 0 3 | .65270E-63 |
| 214 | .31323E+00 | .25768E+00 | .25422E+00 | .21204£+00 | .20922E+00 | .16986E+00 | .16700E+U0 | .13279E+U0 | .13121E+00 | .99802E-01 | .98604E-01 | .69452E-U1 | .68541c-01 |
| | .33441E+00 | .27901E+00 | .32076E+00 | .27143£+00 | .31220E+00 | .26557E+00 | .3U5u7E+U0 | .20133E+U0 | .30093E+00 | .25848E+00 | .297/0E+00 | .25651E+U0 | .29590E+00 |
| | .88885E+00 | .92507E+00 | .91241E+00 | .93861£+00 | .92669E+00 | .94901E+00 | .93723E+U0 | .956U7E+U0 | .94458E+00 | .96045E+00 | .949>5E+00 | .90404E+U0 | .95268E+00 |
| 2 P | .30300E+00 | .33463E+00 | .30690E+00 | .20300E+00 | .2>9>9k+00 | .25173c+00 | .21257E+UU | .10412E+06 | .16889e+00 | .13989E+00 | .12832E+00 | .97831E-01 | .89738E-01 |
| | .15472E+01 | .14494E+01 | .15492E+01 | .14494E+01 | .15492k+01 | .1+494c+01 | .15492E+U1 | .14494E+01 | .15492e+01 | .14494E+01 | .15492L+01 | .14494E+01 | .19492c+01 |
| | .20749E+00 | .30024E+00 | .27542E+00 | .31332E+00 | .28741k+00 | .32366c+00 | .29089E+U0 | .33133E+00 | .30393e+00 | .33667E+00 | .30863E+00 | .34043E+00 | .312c8c+00 |
| 4.7 | . 100 00 + 00 | .34750E+00 | .31522E+00 | .29560E+00 | .208332+00 | .24824e+00 | .22518E+00 | .197£5E+00 | .17893L+00 | .150/1L+00 | .14215 = + 00 | .11222E+U0 | .101c0E+00 |
| | . 100 00 + 01 | .150000E+01 | .16006c+01 | .15000E+01 | .10000E+01 | .150c0e+01 | .10000E+01 | .15060E+01 | .10000E+01 | .150/0L+01 | .10000 E + 01 | .15000E+U1 | .100c0c+01 |
| | . 234 24 E + 00 | .20140E+00 | .25526c+00 | .29560E+00 | .20833£+00 | .30654e+00 | .27807E+00 | .31507E+00 | .28635E+00 | .32150E+00 | .29140 E + 00 | .32592E+UU | .295c5E+00 |
| 7 7 | .3 +5 +2 +0 0 | .15000c+06 | . 2 0833 £ +00 | .2 4824E + 00 | .22510E+00 | .19725E+00 | .1 (875=100 | .156/1E+00 | .14215t+00 | .11222E+00 | .10180E +v6 | . 1.5500-01 | .000000E-01 |
| | . Lagger +0 1 | .15000c+01 | . 1 00 00 £ + 01 | .15000E + 01 | .10000E+01 | .15900E+61 | .10000=101 | .15000E+01 | .10000t+01 | .15000E+01 | .10000E +v1 | .1.0000-+01 | .10000L+01 |
| | . Lagger +0 1 | .29500c+0 | . 200 33 £ + 00 | .30654E + 00 | .27807E+00 | .31507L+00 | .20635±100 | .32130E+00 | .29146t+00 | .32592E+00 | .29505E +v0 | .3.8541.400 | .27802L+00 |
| 7 7 | .347501400 | .31937e+00 | .29580E+00 | .26802E+00 | .24824E+00 | .212972+00 | .19725E+00 | .109_0E+v0 | .15671E+00 | .12117E+00 | .11222c+u0 | .818902-01 | .75856=-01 |
| | .150006401 | .14000e+01 | .15000E+01 | .145060+01 | .15000E+01 | .14000±+01 | .15000c+01 | .140v0E+v1 | .15006E+J1 | .14000E+61 | .150u0c+u1 | .140002+01 | .150001+31 |
| | .281406400 | .31937e+00 | .29500E+00 | .33097E+00 | .30654E+00 | .34002E+00 | .31507E+00 | .34090E+v0 | .32130E+00 | .35169E+00 | .32592c+00 | .354722+00 | .320.41+00 |
| 71 | .413251+00 | .37519E+60 | .34750E+00 | .31937E+00 | .29580L+00 | .26802E+00 | .24824E+00 | .21297E+00 | .19725E+U0 | .10920E+U9 | .15671E+60 | .12117E+00 | .11222E+60 |
| | .15000L+01 | .140C0E+01 | .150C0L+01 | .140C0E+01 | .15000L+01 | .14060L+01 | .15000E+01 | .14000E+01 | .15000E+U1 | .14000E+U1 | .15000L+01 | .14000E+01 | .15060L+01 |
| | .25823L+03 | .30302E+00 | .28140E+00 | .31937E+00 | .29580L+00 | .33097E+00 | .30654E+00 | .34002E+00 | .31567E+O0 | .34690E+00 | .32130E+00 | .351d9E+00 | .32592E+00 |
| Z 0. | 6 19 208 | 7 18 209 | 7 19 210 | 8 18 211 | 8 19 212 | 9 18 213 | 214 | 1 10 18 2 15 | 10 19 216 | 11 18 217 | 11 19 218 | 12 18 219 | 12 19 220 |



| 973 | 19449E+00 | 37953E+00 | 35092E+U0 | 19412E+U0 |
|-----|-----------------|-----------------|-----------------|-------------------------|
| | 35132E+00 | 19507E+00 | 19419E+U0 | 37944E+U0 |
| | .10687E-01 | 30468E-01 | 87129E-U2 | 335U8E-U2 |
| 170 | .44260E-02 | .410/8E-02 | .3/330E-02 | .34629E-02 |
| | .5cozze-61 | .50582E-01 | .54940E-01 | .5>046E-01 |
| | .60697e-03 | .67806E-03 | .63305E-03 | .63472E-03 |
| 47 | .40424E-01 | .40050E-01 | .12726E-01 | .12559e-01 |
| | .25534E+00 | .29415E+00 | .25473E+00 | .29347e+00 |
| | .96031E+00 | .95492E+00 | .90093E+00 | .95509e+00 |
| 77 | .5/511c-01 | .52754E-U1 | .15056£-61 | .10503E-U1 |
| | .14494e+01 | .15492E+J1 | .14494£+01 | .15492E+U1 |
| | .34269e+00 | .31435E+UU | .34383£+00 | .31539E+U0 |
| +7 | .7505001-01 | .000000-01 | .34/10k-ul | .10000L+01 |
| | .150501+01 | .10000-01 | .15000k+ul | .10000L+01 |
| | .328546+00 | .29802:+00 | .33026k+u0 | .29959E+00 |
| 2 7 | . 19720201 | .31470L-01 | .000000E+00 | . U U U U U U U E + U U |
| | . 150002 +01 | .10000L+01 | .10000E+01 | . I U U U U E + U I |
| | . 35026E+00 | .29599L+06 | .33072E+00 | . 3 U Ü U U E + U Ü |
| 77 | .47400E-v1 | .347.0E-01 | .600000E+00 | .000000±+00 |
| | .140v0E+01 | .15000E+01 | .14000E+01 | .15000±+01 |
| | .3909dE+00 | .33026E+00 | .35707E+00 | .330/2±+00 |
| 21 | .81690L-01 | .758501-01 | .374806-01 | .347131-01 |
| | .14000L+01 | .15000:+01 | .140e06+01 | .15000E+01 |
| | .35472L+00 | .32854.+00 | .35658=+00 | .33026E+00 |
| ٠ م | 13 18 221 | 13 19 222 | 14 18 223 | 14 224 |



| 47 D | 973 973 | 41274E+60 20529E+01 .21348E+00 | 28476e+01 441u0E+00 58335E+00 | 24380E+01 55630E+00 11700E+01 | 38055E+00 28133E+01 .10862E-01 | 38253E+U0 13406E+U1 .29720E+00 | 13340E+01 58871E+00 97539E+00 | 11346E+01 51751E+00 73560E+00 | 33843E+00 14823E+01 .17024E+00 | 36081E+00 74660E+00 .24243E+00 | 78184E+U0 49026E+U0 50879E+U0 | 661546+00 42790E+00 37396E+00 | 33243E+00 84532E+00 .16190E+00 | 35317E+00 575ubE+00 .17c59E+00 |
|------|------------|--|--|--|--|--|--|---|--|---|---|--|---|--|
| ۹. | ۲۲ (21 | .72619e-02 .70838e-01 .38789e-02 | .67685E-02 .74249E-01 .36899E-02 | .85615E-U2 .77836E-01 .46531E-02 | .74675E-02 .8U2U1E-01 .41750E-02 | .72224E-02 .75582E-01 .25416E-02 | .655116-02 .780986-01 .249576-02 | .79160E-02 .7/290E-01 .26776E-02 | .71098E-02 .78824E-01 .25247E-02 | .61743E-02 .708/1E-01 .1/171E-02 | .55099E-02 .72739E-01 .17257E-02 | .64442E-02 .70229E-01 .1/135E-02 | .57259e-02 .714/2E-01 .10943E-02 | .49291E-02 .64672E-01 .13409E-02 |
| ۲, | 7.7. | .7%308E+00 .005006E+00 .104%6E+00 | .72918E+00 .00732E+00 .15157E+00 | .69945E+00 .54332E+00 .46369E+00 | .65022E+00 .62500E+00 .430c0E+00 | .57655E+00 .48595E+00 .65685E+00 | .54303c+00 .5c778c+00 .6l8c6E+00 | .465y8E+U0 .442c8E+U0 .766U9E+U0 | .44315E+00 .52221E+00 .72864E+00 | .37649E+U0 .41008E+U0 .830/1E+U0 | .36051E+00 .48716E+00 .79543L+00 | .30617E+00 .38900E+00 .80807E+00 | .29441E+u0 .464u3E+U0 .83546E+U0 | .24895E+UO .373c8E+UO .89344E+UO |
| 4 | 47 | .52815c+50 .10409c+01 .29013c-01 | .47701±+00 .17404±+01 .24826±-01 | .53217k+00 .1c469k+01 .80141k-01 | .45537e+00 .17484e+01 .75421e-01 | .48844E+00 .10489E+01 .13913E+00 | .41795E+00 .17484E+01 .11905E+00 | .43426E+00 .10489E+01 .17849E+00 | .3/159£+00 .17454£+01 .15273£+00 | .37818E+60 .10489E+01 .20862E+00 | .32300E+00 .1/404E+01 .1/601E+00 | .32445E+00 .10469E+01 .23014E+00 | .2/762E+00 .1/464c+01 .19693c+00 | .27436e+JU .10407e+J1 .24617e+UD |
| | ٠, 7 | .bze/8t + 00 .1/0.0t+01 .00000t+00 | .435092+0U .10000E+01 .00000E+00 | .51552L+00 .17000E+01 .54160E-01 | .42057E+00 .16000E+01 .44030E-01 | .47626E+00 .17000L+01 .11042E+00 | .395/4c+00 .180.00c+01 .913.00c-01 | .43306E+00 .17000E+01 .14939E+00 | .35900e+00 .16000e+01 .12301e+00 | .377.9e+00 .170.00e+01 .1d392e+00 | .31202E+00 .1000GE+01 .15218E+00 | .52912E+00 .17000E+01 .20506E+00 | .2 /233E + 00 .10006L + 01 .1/617E + 00 | .2/6/6E+UD .1/UUDE+U1 .2E9.11E+UU |
| 1 · | 7 7 | .3.2522.400 .170002.401 .541002.41 | .4205/c+00 .15000c+01 .44830c-01 | .4 /8266+00 .1 /0006+01 .110426+00 | .39574c+00 .10600c+01 .91300c-01 | .43300E+UU .17000E+v1 .14939E+UO | .3>900c+00 .1a00JE+01 .123c1c+00 | .3/709E+00 .1/000E+01. .10392E+00 | .31202c+00 .10000c+01 .15218c+00 | .32912L+00 .17000L+01 .20506E+00 | .2 /233E+00 .10000E+01 .1/017E+00 | .27678E+UU .17000c+Ul .22411c+UU | .2.9.00£+00 .109.00£+01 .10544£+00 | .170.00 +00 .170.00 +01 .25001+00 |
| × | 177 | .53717c+00 .15000c+01 .61710c-01 | .51552E+U0 .170U0E+01 .54160E-01 | .544/3E+U0 .1cOUOE+U1 .125/6E+U0 | .47046E+00 .17040E+41 .11042E+00 | .49416E+U0 .16UC0L+U1 .17015E+U0 | .43306E+00 .17000E+01 .14939E+00 | .42950E+00 .1c000E+01 .20948E+00 | .37709E+U0 .179U0E+U1 .18392E+U0 | .37407L+00 .100C0E+01 .23424E+00 | .32912E+U0 .170U0c+U1 .2U566E+U0 | .31522c+00 .10000c+01 .25526c+00 | .2 /n /oc+v0 .1 /0/00c+v1 .2<411E+v0 | . 261312+00 . 196002:+01 . 205332+00 |
| T X | 7.7 | .60000E+00 .10000E+01 | .52678E+60 .17000E+01 .00000E+00 | .58717E+00 .16000c+01 .61710E-01 | .51552E+00 .17000E+01 .54180E-01 | .54473E+U0 .160U0E+01 .12576E+U0 | .47826E+00 .17000E+01 .11042E+00 | .49416±+00 .16000£+01 .17015£+00 | .43366E+00 .17000E+01 .14939E+00 | .42950E+U0 .16000L+01 .20948E+U0 | .377u9t+00 .170c0t+01 .16392E+00 | .37487E+00 .1LOvOE+01 .23424E+00 | .32912E+v3 .17000E+01 .20506E+00 | .31522c+00 .1c0C0c+01 .25526c+00 |
| Z. | Z Q. | 1 21 225 | 1 22 226 | 2 21 22.7 | 2 25 228 | 3 21 229 | 3 27 230 | 7 1 1 5 5 1 5 5 1 5 9 1 | 4 22 232 232 | 5 21 233 | 22 22 234 | 6 21 235 | 6 22 22 236 | 7 21 237 |



|) | 598×1E+00 41811E+00 | 344 YUE+UO | 52565E+U0 38540E+U0 21773E+U0 | 33818E+U0 65205E+U0 .14752E+U0 | 35256E+U0 44431E+U0 .12615E+U0 | 52555E+00 34141E+00 21533E+00 | 46205E+00 30436E+00 1242E+00 | 34394E+U0 54853E+U0 .10442E+U0 | 35142E+00 43715E+u0 .77009E-u1 | 44862E+U0 36125E+U0 12349E+U0 | 42900E+U0 35415E+U0 62575E-U1 | 34780E+U0 49498E+U0 .54249E-U1 | 35120E+U0 42177E+U0 .33550E-U1 | 47254E+U0 35214E+U0 45454E-U1 |
|---|--------------------------|------------|--|--|--|---|--|--|---|--|---|---|---|---|
| 1 | .43679E-62 | .13816E-02 | .44600e-02 .62397e-01 .12747e-02 | .3y455e-02 .63854e-01 .13097e-02 | .47231E-02 .61939E-01 .12570E-02 | .41723E-02 .63025E-01 .12890E-02 | .37251E-02 .56857E-01 .11574E-02 | .32875E-02 .60149E-01 .12006E-02 | .40640E-02 .5b740E-01 .11627E-02 | .35841E-02 .59739E-01 .12013E-02 | .33110E-02 .5c721E-01 .11032E-02 | .29191E-02 .57893E-01 .11496E-02 | .37352E-02 .50dzdE-01 .11261E-02 | .32917e-02 .5/701e-01 .11673e-02 |
| ; | .24014E+00 .447clE+00 | .86159E+00 | .20516E+00 .36432E+00 .90839E+00 | .19613E+00 .43094E+00 .87706E+00 | .16463E+00 .32692E+00 .91951E+00 | .15931E+00 .42837E+00 .88945E+00 | .12474E+UU .3510UE+UU .92725E+UO | .12401c+00 .42232c+00 .89784E+00 | .90841E-U1 .348U0E+U0 .93248E+O0 | .93924E-01 .41023E+00 .90347E+00 | .67214E-01 .34547E+00 .93602E+00 | .65114E-01 .41534E+00 .90733E+00 | .34472-01 .34378+00 .73414E+00 | .301324-01 .41370E+00 .90901E+00 |
| ; | .23477E+00 .17404E+01 | .21004E+00 | .23202E+03 .16489E+01 .25689E+00 | .19054E+00 .17484E+01 .21982E+00 | .16949E+00 .16459E+01 .26537E+00 | .102582+00 .174842+01 .22707E+00 | .15096E+00 .16489E+01 .27106E+00 | .12918E+00 .17484E+01 .23246E+00 | .11470E+00 .16489E+01 .27603E+00 | .94146E-01 .1/484E+01 .23520E+00 | .80210c-01 .16459c+Jl .27912c+OU | .60636E-01 .1/404E+01 .23684E+00 | .4/154k-01 .104c9k+01 .2o097k+00 | .40350E-01 .1/404E+01 .24042E+00 |
| | . 10000c+01 | .10548±400 | .235586 +00 .170.00 +01 .23558E+00 | .194946+00 .106006+01 .19494E+00 | .19770L+00 .170-06+01 .24414e+00 | .103>9k +00 .160 00e + 01 .202 01e + 00 | .157.0c+00 .1700c+31 .25141E+00 | .12999E+00 .1c000E+01 .20803E+00 | .12461E+00 .17000E+01 .2559E+00 | .10327E+00 .10000E+01 .21174E+00 | .893c0E-Ul .170c0E+Ul .25957E+U0 | .73900c-01 .160-00c+01 .21479c+00 | . 00410E-01 .170.00+01 .20105E+00 | .49900E-01 .16000E+01 .21601E+00 |
| 1 | .19494L+06 .10000L+01 | .17474E+UO | .1/7/00.100 .1/000£+01 .2.4414E+00 | .10359E+00 .10000L+01 .2020L+0 | .15710L + 00 .17000L + 01 .25141E + 00 | .129391+00 .160001+01 .20803E+00 | .12461E+U0 .17UU0E+U1 .25589E+U0 | .10327E+00 .10600E+01 .21174E+00 | .0 y380E-01 .1 /0 u0£+01 .25957E+00 | .73900E-01 .10000E+01 .21479E+00 | .60410E-01 .1/000E+01 .20105E+00 | .49960E-61 .10000E+01 .24651E+00 | .2/tosc-01 .1/tose+01 .20303E+00 | . 2 - 3 - 4 - 4 - 4 - 4 - 4 - 4 - 4 - 4 - 4 |
| 1 | .43558c+30 | .23558E+00 | .225131+00 .100-06+01 .278076+00 | .19770E+60 .17000L+01 .24414L+00 | .178931+00 .160001+01 .28035E+00 | .15710c+00 .17000c+01 .25141c+00 | .142151+00 .16000E+01 .29146E+00 | .124611+00 .17000+01 .255691+00 | .10100L+00 .10000L+J1 .29505L+00 | .89300E-01 .17000E+01 .25957E+00 | . 003000-01 . 10000-01 .29802E+00 | .60410L-01 .17000L+01 .20105L+00 | .31470L-01 .10000L+01 .29909L+00 | .27050e-cl .170c0c+Jl .20JO3E+U0 |
| | .27676e+00 .17000E+01 | .224116+00 | .20833L+00 .16060E+J1 .20833L+60 | .23558L+00 .170¢0k+01 .23558L+00 | .22518E+v0 .16000E+u1 .27807E+u0 | .19770c+00 .17000c+01 .24414c+00 | .17893E+UÖ .160C0L+U1 .24635E+U0 | .15710±+00 .17060£+01 .25141E+60 | .142151+00 .16000E+01 .29146E+00 | .12461E+00 .17000E+01 .25589L+00 | .10180E+00 .16000E+01 .29565E+03 | .89340E-01 .17000E+01 .25957E+00 | .68800E-01 .10000E+01 .29802E+00 | .66410L-01 .17040L+01 .24165L+00 |
| | 7 | 238 | 8 21 239 | 8 22 240 | 9 241 | 9 22 242 | 10 21 243 | 10 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 | 2 11 21 245 | 11 22 246 | 12 21 247 | 12 22 24 H | 13 21 249 | 13 22 250 |



| 42000E+00 35100E+00 11407E-01 35054E+00 47263E+00 69129E-02 85412E+00 31933E+01 | 32826E+U1 85409E+U0 80341E+U0 27613E+U1 12693E+U1 | 79667E+U0 32434E+U1 12984E+U0 10060E+U1 20081E+U1 | 16725E+01 14187E+01 15017E+01 14007E+01 10088E+01 | 84137E+00 217c4E+01 .44785E+00 12347E+01 13134E+01 |
|--|---|--|--|---|
| .31472E-02 .55457E-01 .10670E-02 .27754E-02 .56563E-01 .11339E-02 .61704E-02 | .52762E-02 .10336E+00 .19002E-01 .70461E-02 .87848E-01 | .54022E-02 .15106E+00 .15190E-01 .57441E-02 .85453c-01 | .44910c-02 .15335c+00 .10502c-01 .61282c-02 .84509c-01 | .45683E-02 .14446E+00 .15315E-01 .46933E-02 .78404E-01 |
| .122286-01 .343216+00 .939186+00 .113978-01 .412686+00 .910716+00 .95256+00 | .38257E+00 .91936E+00 .91715E-01 .56715E+00 .73290E+00 | .34702E+00 .84063E+00 .27334E+00 .48421E+00 .07912E+00 | .30112E+00 .80851E+00 .39372E+00 .40167E+00 .63397E+00 | .25090e+00 .84293e+00 .47595e+00 .33009e+00 .59700e+00 |
| .148006-01 .104696+01 .261906+00 .126706-01 .174046+01 .241216+00 .373446+00 .373446+00 | .20594£+00 .1933£+01 .10707e-01 .39606E+00 .14472E+01 | .19635c+00 .1933se+01 .32523e-01 .32660e+00 .16472e+01 | .18022E+00 .19332E+01 .51333E-01 .29055E+00 .10472E+01 | .16023E+00 .19333E+01 .62857e-01 .25302E+00 .18472E+01 |
| | .000000E+00 .20000E+01 .00000E+00 .30007E+00 .19000E+01 .32150E+01 | . 600 006 + 00 . 200 006 + 00 . 600 006 + 00 . 763 496 + 00 . 190 006 + 01 | .0000000000000000000000000000000000000 | |
| . 170000 + 001 . 20337 + 001 . 20337 + 100 . 10000 + 00 . 10000 + 00 . 20527 + 00 . 30527 + 00 . 30527 + 00 | .03 ye-02 .000000 + + + + + + + + + + + + + + + + | . 1916-01 . 0.0000E+00 .20000C+00 .2571/E+00 .19600C+01 | .11ce-60c000c+00 .2c000c+01 .0c000c+01 .22352c+00 .140c0c+01 | .116=-0. .00000=+00. .20000=+01. .00000=+00. .17507c+00. |
| .00000E+00 .10000E+00 .00000E+00 .17000E+00 .17000E+01 .20339E+00 .42657E+00 .14930E+01 | -Pudk Fill .30557E+00 .19000E+01 .32120C-01 .39574E+00 .18000E+01 | -Pouk FII 0A0. 20349E+00 .19000E+01 .30400E+01 .30900E+00 | QUAL. .2>/17L+U0 .1>000E+U1 .1Y00E+U1 .88550E-U1 .31202E+00 .14000L+U1 | -PLOR FII QUAD. .22352E+00 .19000E+01 .10902E+00 .2723E+00 .18500E+01 .18500E+01 |
| .314901-01 .100001+01 .299992+09 .276501-01 .170001+01 .203031+00 .435891+00 | QUESTIONABLE FUINT -PLUK FILL MARNING LUND THIN QUAD. 1 .31225c+60 .39597c 24 .19000c+01 .19000c 254 .00000c+00 .32120c 2 .42657c+00 .39574c 23 .14000c+01 .18000c 25 .44830c-61 .91300c | QUESTIONACL FUINT -PUU 2 .30557E+U0 .2 24 .190U0E+U1 .1 256 .32120E-U1 .6 3 .39574E+U0 .3 23 .16000E+U1 .1 257 .913.0E-U1 .1 | 00ESTIONABLE FOINT - WARNING LUNG THIN QU 3 .26349c+00 24 .15000c+01 258 .65450c-01 4 .359c0c+00 23 .12361E+00 | QUESTIONABLE FOINT WARNING LUNG THIN QU 4 .257176+00 24 .196006+01 260 .885506-01 5 .312026+00 23 .16000€+01 261 .152186+00 |
| 14 251 252 252 252 23 23 253 | 0 UESTI WARNIN 1 24 254 23 255 255 255 | 0UESTI WARNIN 2 24 24 256 3 23 | 000ESTI WARNIN 3 24 25 258 4 23 259 | QUESTI WARNIN 24 260 260 23 23 |

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| | 10049E+01 15428E+01 92873E+00 | 88779E+U0 166U4E+U1 72763E+U0 | 94401E+U0 15340E+U1 .87257E+U0 | 14317E+01 95446E+00 .96607E+00 | 77595E+00 15619E+01 57432E+00 | 70620E+UU 10820E+U1 44064E+U0 | 11754E+01 115u6E+01 .956e6E+00 | 15705E+01 74424E+00 .73356E+00 | 68292E+U0 15648E+U1 36251E+U0 | 62316E+00 10921E+01 25950E+00 |
|---|---|--|--|---|--|--|---|--|---|--|
| | .33720e-02 .13359e+00 .14192e-01 | .40399E-02 .70021E-01 .60364E-02 | .33858E-02 .12500e+00 .13517e-01 | .36721E-02 .70855E-01 .59185E-02 | .25206E-02 .11636E+00 .12962E-01 | .33058E-02 .60130E-01 .59179E-02 | .22347E-U2 .11024E+U0 .12624E-01 | .34872E-02 .60657E-01 .59462E-02 | .23391E-U2 .1U524E+GO .12379E-U1 | .27426E-02 .63857E-01 .59113E-02 |
| | .21010E+UU .82529E+UU .52417E+UO | .27236E+00 .27322E+00 .77201E+00 | .17371E+00 .81220L+00 .55691E+00 | .22337E+UO .555u7E+UO .80125E+UO | .14384£+UO .8U313£+UO .57818£+UO | .15440E+U0 .54326E+U0 .81897E+00 | .11965E+U0 .79705E+U0 .59194E+U0 | .14906E+00 .53415E+00 .83214E+00 | .9 6709E-01 .79230E+00 .60242E+00 | .11089E+00 .5274E+00 .84151E+00 |
| | .1,454£+00 .1,433£+01 .70973£-01 | .217086+00 .104726+01 .103986+00 | .11971c+00 .19353c+01 .04913c-01 | .10356E+U0 .16472E+U1 .10470E+U0 | .10123E+00 .19353E+01 .90827E-01 | .15524E+U0 .18472E+U1 .1/188E+U0 | .85610E-01 .19333E+01 .94783E-01 | .12/12=+00 .104/2E+61 .1//54E+00 | .701036-01 .174335-01 .979106-01 | .10100c+00 .15472c+01 .10176c+00 |
| | . 000 00 + 00 . 200 00 + 01 . 000 00 + 00 | .195.94.400 .190.05.401 .121.90£.400 | . 600 00E +00 . 200 06E +01 . 000 00E +01 | .164 05E+00 .196 00E+01 .15264E+00 | . 600 cot + 00 . 200 cot + 01 . 000 cot + 00 | .13904E+00 .19000E+01 .13904E+00 | .200000E+00 .20000E+01 | .117191+00 .190001+01 .14471+00 | . 0 0 0 0 0 0 + 0 0 . 2 0 0 0 0 0 + 0 1 . 0 0 0 0 0 + 0 0 | .931201-01 .190601+01 .14902i+00 |
| . / / / / / / / / / / / / / / / / / / / | . 200000E+01 . 20000E+01 | .104051+00 .19600E+01 .13284E+00 | .560E-02 .33406L+06 .23606E+01 .63806E+01 | ./4JE-04 .139C4E+U6 .170C0E+U1 .139C4E+U0 | .06/E-02 .00000E+00 .20000E+01 | .//2E-04 .11719E+00 .14000L+01 | .531E-02 .00000E+00 .2000E+01 .0000E+01 | .474E-04 .93120L-01 .19002E+01 .14902E+00 | .030E-02 .00000E+00 .20000E+01 | .35cE-64 .7350c-01 .1900c+01 .151cE+00 |
| -Punk FIII | .19500c +00 .19000c +01 .12190c +00 | .22900E+00 .10000E+01 .13544E+00 | 1 -PUUK FIT QUAD. .104C5E+UU .190U0E+UI .13264E+U0 | -Pudk Flf .19494E+00 .16000E+01 .19494E+00 | GUAU. .13904E+00 .13906E+01 .13904E+01 | -PUGK FIT .103594+00 .100006+01 .20201e+00 | QUAD. .11719E+00 .19500E+01 .14471E+00 | -Punk FII .12799E+00 .18000E+01 .20803E+00 | -PUDK FIT QUAD. .93 206-01 .190606+01 .14702+09 | -Pudk FII .103c7c+bu .100c0b+01 .21174c+09 |
| QUESTIONABLE POINT | . 22352 E+ U0 . 19600 E+ U1 . 10902 E+ C3 | .27233L+00 .16000E+01 .17017L+00 | QUESTIONABLE POINT MARNING LUNG THIN Q 6 .195.9L+03 24 .150.0L+01 254 .12190E+00 | QUESTIOMABLE POINT 7 .229.00E+00 23 .10000E+01 265 .18544E+03 | MARNING LGNG THIN G 7 .16405E+00 24 .19000E+01 266 .13244E+00 | QUESTIONABLE POINT 8 .19494E+00 23 .18000E+01 257 .19494E+00 | QUESTIONABLE FOINT WARNING LUNG THIN G 8 .13964 e+00 24 .19000 e+01 258 .13964 e+00 | QUESTIONABLE POINT 9 .16359L+00 23 .180v0E+01 269 .262UIE+00 | QUESTIONABLE POINT WARNING LGNG THIN Q 9 .11719L+00 24 .1900G+61 270 .14471E+00 | QUESTIONABLE POINT 10 .12999E+00 23 .16000E+01 271 .20803E+00 |
| Q UES | 262 | 6 2 6 3 | QUES WARN 6 24 204 | a UE S 7 23 265 | 0 UES WARN 7 24 266 | 9 UE S 8 23 267 | QUES WARN 8 24 208 | 0 UES 9 23 269 | 0 UES WARN 9 24 270 | Q UE S 10 23 271 |



| | | | | | 4.5.5 | | | 0 -1 1 | |
|------------------------------|--|--|--|---|---|---|--|--|---|
| | 13555E+U1 88654E+U0 .82197E+U0 | 16551E+U1 62401E+U0 .44811E+U0 | 62834E+00 156e0E+01 205e2E+00 | 58241E+00 16979E+U1 13373E+U0 | 14894E+U1 702U7E+U0 .54270E+U0 | 16950E+U1 56850E+U0 .14975E+U0 | 61982E+00 15603E+01 78520E-01 | 56408E+00 16994E+01 21115E-01 | 15587E+U1 62676E+U0 .17925E+U0 |
| | .10205e-02 .10004e+00 .12173E-01 | .2y8u0t-02 .630u3t-01 .5y32bt-02 | .197046-02 .97626-01 .120516-01 | .24301E-02 .61271E-01 .59100E-02 | .1c042e-u2 .95034e-u1 .11952e-c1 | .2/385E-U2 .60826E-U1 .57297E-02 | .1u046E-02 .93525E-01 .11907E-01 | .23085E-02 .59805E-01 .59098E-02 | .15194e-02 .92502e-01 .11871e-01 |
| | ./6359E=01 ./bac9E+00 .b09/6E+00 | .861.94-01 .522686+00 .847646+00 | .5/5U5E-U1 .76645E+Ü0 .61477E+00 | .61297E-01 .51903E+00 .85219E+00 | .405c0E-ul ./64d3E+00 .61839E+00 | .35048L-01 .51709E+00 .85482E+00 | .22963E-01 .74373E+00 .62008E+00 | .11119L-01 .51673E+00 .85608E+00 | .735406-02 .783256+00 .021006+00 |
| | .55700E-01 .19333E+01 .10023E+00 | .70740E-01 .10472E+01 .10466E+00 | .42320c-01 .19333c+01 .10165c+60 | .536672-01 .104725+01 .106/55+00 | .29597E-01 .19333E+01 .10299E+00 | .31549E-01 .16472E+01 .10798E+00 | .1 /4 UUE - U1 .1 93 3 3 5 + U1 .1 U3 U 7 E + U0 | .9900ak-02 .104/2k+01 .14800k+00 | .54633c-02 .1933c+01 .10401c+06 |
| | . 000 001 + 00 . 200 001 + 01 . 000 001 + 00 | .73966-01 .190002+01 .15108-+00 | . 000 00E + 00 . 200 00L + 01 . 000 00E + 00 | .52500E-01 .19000E+01 .19306E+00 | . 000000 + 00 . 20000 + 01 . 00000 + 40 | .35810c-01 .17000c+01 .15510c+00 | .000 CUE + CU .200 CUE + C1 | .163 /UL-C1 .190 /UL+C1 .15591E+UU | . 000 COL+00 . 200 UDE+01 . 000 COL+01 |
| . 6211-02 | . 30000e+00 . 20000e+00 | . 16 JE - 04 .5 _ 9 J - 04 . 1 7 0 J - 04 . 1 J 3 G D + 0 J | .00000E+00 .00000E+00 .20000E+00 | . 3916-04 . 37310-01 . 17000-01 . 17510-40 | .011f-02 .00000E+00 .20000E+01 .00000E+01 | . 1146-64 . 103966-01 . 190008+01 . 195916+00 | .070E-02 .00000E+00 .20000E+01 | .902E-04 .00000E+06 .19000E+01 .15612E+00 | .58/E-02 .00000c+00 .20000c+01 .00000c+00 |
| -Four ril | .73750E-01 .1950AL+01 .15168E+00 | -Puük FIT .73900E-Ul .1000UE+Ul .21479E+U0 | -Pudk rII UAD. .52900c-UI .19300c+UI | -PUUK FI] .499ene-JI .180c0e+UI .21051E+CO | -PUOR FIT QUAD. .35810c-01 .19000c+01 | -PUOK FII .22do0E-vl .1d0v0L+01 .21/u4r+v0 | -PUUK FII QUAJ. .16390E-01 .19000E+01 .19591E+00 | -PUUK FII .000000=+00 .14000=+01 .21774=+00 | -PLUK FII GUAD. .000.00E+U0 .1900UE+01 |
| QUESTIONAGE POINT - FOUR FIT | .19000E+01 | QUESTIONAGLE F014T 11 .10327£+60 23 .150.00£+01 273 .21174£+05 | QUESTIONABLE PUINT -PUGK WARNING LUNG THIN QUAU. 11 .73980k-01 .52' 24 .19000k+01 .15' 274 .15168E+00 .15' | 12 .739.00L-C1 23 .160.00L+01 275 .21479E+00 | QUESTINGABLE POINT MARNING LUNG THIN O 12 .52980E-01 24 .19000E+01 276 .15306E+00 | QUESTIONABLE POINT 13 .49980e-01 23 .10000e+01 277 .21651E+00 | QUESTIONABLE FOINT -POUK FITT WARNING LUNG THIN QUAD. 13 .35810E-01 .16390E 24 .19000E+61 .19000E 278 .15510E+00 .15591E | 14 .22860=-01 23 .16000E+01 279 .21764E+00 | QUESTIONABLE POINT MARNING LUNG THIN Q 14 .16390E-01 24 .19000E+01 280 .15591E+03 |
| QUES | 10 24 272 | a UES' 11 23 273 | Q UEST WARN: 11 24 274 | 0 UEST 12 23 275 | 0 UEST WARN; 12 24 276 | 0 UEST 13 23 277 | Q UEST WARN] 13 24 278 | 0 UEST 14 23 279 | Q UEST WARN] 14 24 280 |



970

47

57

XYZ POTENTIAL FLOW PRUGNAM SECTION 4. VENSION 4

SAMPLE PRUBLEM TRIAXIAL ELLIPSOID

SULID ANGLE = 12,500 7 7



| 7 9 | •/lɔヒ+00 | 9 7 | •>29E•00 | • + U + E + 6 U | P 5 | .135E+01 |
|------------------------------|--|--|---|-------------------|--|--------------------------|
| ⁴ 3 | • - 3 = E + 0 C | ינטטטן וים • ייט וואבר • ייט וואבר • ייט וואבר • ייט ייט ייט ייט ייט ייט ייט ייט ייט י | · + 32E + 00 | .467E+00 | b 1 | 341E+GO |
| ſ | .7276+00 | 7 | .575E+00 | *17APFULATI | 1 | • 126E + 0 1 |
| SUM DE CHANGES .p6u5zf+00 | .132196+60 .67071E-01 .25180E-01 .94774E-02 .35680E-02 | .U Y VELUCITY=-1.0 SUM OF CHANCES .J1142E+01 .22746E+01 .16621E+01 | .12150E+01 .b3c2uE+00 .6442cE+00 .474645E+00 .3469bE+00 .25362E+00 | Luc1 | Sum OF CHANGES • 15305E+02 • 34163E+01 • 75055E+00 • 16725E+00 | .81712E-02 .13059E-02 |
| ITERATION S | 07t0 2~0 | OCITY= | ± v o ~ p → c | 11 X VELOCITY= | I TERATION S | 00 2 |

XYZ PUTENTIAL FLOW PROGNAM SECTIUM 4. VERSION 4 SAMPLE PRUPLEM TRIAXIAL ELLIPOUID



.12E-04 .11E-04 .11E-04 4 1E-05 .34E-05 .24E-05 .22E-05 .21E-00 . 2 ZE -00 12E-04 7 JE -0 5 64E-05 50E-05 4 1E-05 .93E-05 93E-05 74E-05 74E-05 .64E-05 60-379 5 UE -05 50E-05 .41E-05 .34E-05 27E-05 .27E-05 .17E-05 17E-05 .12E-05 .12E-05 67E-06 67E-06 ,12E-04 11E-04 10E-04 94E-05 .94E-05 74E-05 62E-05 50E-05 4 1E-05 34E-05 34E-05 27E-05 27E-05 22E-05 22E-05 16E-05 RUKMAL .11600 . 6969 .02428 .0112€ 00450 99860 .07440 07470 03692 .11610 .09673 .07488 .07485 .05488 .05887 .04586 .03697 .03095 .02959 .02959 .01944 .01944 . 01494 .01492 . 00177 .00774 00459 00141 .00140 05002 **U5878** 04584 16980 0295c 02427 02425 01943 .04587 01127 09844 04581 02759 01942 01494 01493 DURCE -.87898 -.90759 -.42917 -.74947 -.90766 -.93663 89096 -.91358 -.42996 -.04440 -.64477 -. 834 YU 41217 -.14072 --12134 -.42806 -.64396 -.64307 -.74933 -.834c0 -.83430 -.87891 -.93600 -.94595 -. 44604 84004.--.96247 -.96248 06696.-87696.-.90628 .40865 640477 -.12208 --124/3 - 4 30 45 -.74971 -.75008 -.8342B -.8/841 -.87931 21104.--. 40789 -,93669 -.93707 01946.--.94618 1.37073 1.40332 28662 16618 .05093 .1955 .1754B . 28213 .28213 . 32261 .35430 .. 33116 1.38110 0719E. 1.39171 1.39497 1,39501 1.40021 1.40024 1.40088 93004 • 1 16667. .30614 . 16894 . 17130 19490. ..00053 .19022 .20234 44797 · .. 32277 . 32291 .35454 .35430 . 57073 .37008 .3812U .38120 .34563 49066. .76670 . 65564 .32200 . 35448 19561. 34165 6714c. 36348 10053 67467 67179 30195 24368 17148 14399 10036 62840 27348 29610 52701 47848 30105 52807 24330 14403 0.1823 27423 69969 01036 5 2 4 4 3 30128 24265 14401 63728 69827 69775 6 2000 51679 40604 43440 30100 19147 01033 30312 63441 64519 62011 60647 19110 30201 17154 00012 21700 99000 00555 11403 51500 U0017 00000 N0624 6/810 01025 10700 26200 00100 00126 01500 26000 00112 00035 04450 74770 05189 02411 00442 01303 70200 **47000** 00407 00038 00112 17770 03132 64810 21410 90510 りこといり ეივივ ロマチャロ 550TO ICITO **りゃんりつ** 70510 00663 00464 U17400 ---1.02127 -1.0-148 -1.10790 -1.33706 -1.33/10 -1.30954 -1.32450 -1.3/346 -1.30755 -1.37004 -1.39905 -1.40319 -.00.702 -.42622 -. 7,701 -1.02198 -1.10018 -1.24/09 516661--1.33/28 --42322 446344-4.14555 -. 79610 -1.24741 -1.24751 -1.5004/4 -1.30460 -1.30751 -1.3,661 -1.39905 -1.40320 -.00240 -.42700 -- 17845 -1.02209 -1.10050 -1.24/08 -1.304,4 -1.31709 -1.30902 -1.503/0 -1.3/043 -1.31dy -1.30711 -1.10/04 -1.3/047 -1.30/00 10013 02160 22644 31517 30954 40/06 40004 45505 4/036 40000 40713 477TB 447754 47645 45666 47409 00100 50000 15495 54450 31310 51133 30676 45152 24502 4 26 05 4 24 10 40500 40121 46875 115377 40429 40147 45276 46745 31617 30001 45371 7444.5 2.277 30374 44610 4170 1000 4050 4015 55650 64640 14447 66650 14977 24445 14997 14997 14447 14997 14997 24145 24995 14447 66650 64640 555.40 64640 1477 04020 55550 54640 64640 14997 24975 34943 34992 34942 24445 14997 14997 55550 64640 24995 34648 34942 34645 24445 34+43 54642 24775 34645 34645 34645 14661 24646 .14173 93526 76344 86304 33655 .33571 .08332 .02970 .04416 4 8232 4 7803 57327 14208 50602 57471 48598 48477 41100 20741 20674 20317 20206 98124 96829 85808 75759 66484 57038 40478 94030 76731 66989 40997 91312 85211 65975 33145 20009 86521 66821 35401 26539 26335 A FLUW PT.



10E-04 .916-05 4 4 4 E - 0 5 10E-05 .11E-05 .21E-00 74E-05 .12E-05 .67E-00 .67E-00 12E-04 60E-05 73E-05 67E-00 60E-00 21E-00 60E-05 44E-05 21E-00 21E-00 92E-05 6 1E-05 61E-05 4 YE -05 4 TE-05 34E-05 34E-05 27E-05 21E-05 22E-05 22E-05 12E-04 1 UE-04 1 UE-04 90E-05 90E-05 4 YE -05 40E-05 40E-05 33E-05 .01125 .01123 .00778 00142 00141 00141 11487 11487 00746 00747 00747 00747 00747 00747 . 05869 .02422 .07442 .02949 .05860 .04578 . 03084 .00456 04550 .07459 01492 . 00 17 . 00777 . 0045a . 60450 .00141 .00143 11584 11539 .09824 06/60 .0457 . 13688 . 02 45 4 .01937 .01491 -.87933 -.96049 -.90906 -.80713 -.84725 -.37974 -.43250 80658--.90200 -.64567 -.64644 94047.--.83568 -.40803 -.94622 -.94634 +6606-.30829 -.13703 -.64742 -.96243 -.90935 85606.-179600 . 80318 .34752 04065. -.12768 -.13164 -.43455 -.75127 -.90842 -.93687 -,43742 -.96202 -.14217 -.43707 -.44035 -.64931 -.75308 -.83606 -.83629 -.90244 1.37105 1.40035 1.19090 1.37089 1.39567 1.40344 17620 .. 00 379 . - 28284 . 6 6 3 1 4 .32310 . 35467 .. 38146 1.40054 1.40100 1.40340 .39083 .78157 .79460 .19070 1.28371 . 4033 . 32200 .34179 26190 .32330 ..39171 1.37511 .. 46031 . 32 368 . 32464 45004 .4033 16166. .06901 . 20015 424870 .7807. .4008 .3552 .61550 10015 21007 62850 69310 52522 30032 24174 14328 10005 05049 01653 26740 20505 61914 01831 61746 54349 42538 64059 43606 30210 30119 30081 19005 19052 14304 04660 68212 90819 01844 21234 63227 05847 01027 02202 68713 52121 43376 30059 16609 .03120 .03803 04106 02902 01912 02356 01444 01346 0000202 14079 00106 00652 00584 00339 UULUU 20479 11936 00016 04626 00447 00062 404CT 1,111 65010 01052 00422 00131 17503 14002 11764 00700 24520 01412 22007 20527 00452 07906 0.5541 04150 02450 0/143 -1.37964 -.00300 -. ชบปั*า*ย -1.02505 -1.16964 -1.24620 -1.30527 -1.31014 -1.30/63 -1.33770 -1.40328 -.10138 V04/0.--.43313 445044--1.24004 -1.33/34 -1.53724 -1.35979 -1.39676 -1.31477 -1.40333 -.44006 44018.--1.02670 -1.1/156 -1.24400 -.003+2 -1.023/4 -1.10901 -1.305.7 -1.35978 -1.3/652 -1.37002 -1.39971 0-0400--.45466 -. 40602 -1.02302 -1.1/055 -1.305 J -1.33610 1.2491--1-3057 3 9206 42500 40900 40128 40608 49550 49170 90000 15217 15016 23700 30815 30017 31103 41930 44351 45703 45200 40213 4 (655 41548 40507 04/06 14770 14477 23312 29908 34157 41249 24015 3 04 06 35534 47074 47023 04002 27316 34205 04943 410014 4.0022 22851 40006 40430 44440 54458 .549c8 .44990 54408 34995 34992 44990 54938 .54707 54968 64905 54908 44470 54.408 64905 74902 74982 64905 54145 06665 944440 06655 64105 74982 54468 04.64.5 54308 54.108 066.55 54936 94990 547cB 04664 54988 04444 74962 64455 74962 64105 14101 .08032 .02556 .02522 .93526 06226 02503 91876 83203 74973 73973 65290 64424 54014 55014 47347 25716 .19539 80226 72767 71327 90657 40057 34560 84172 81845 62115 84326 3,801 20002 45973 32366 13664 87408 54366 36879 08141 63309 A FLUE PT. 67 71 72 73 74 77 77 77 77 77 77 78 83 83 2 C 8



| | UKM AL | 27E-0 | 7 I I C | 77 | 10E-0 | 0F-0 | 1E-0 | \neg | . 6 be -0 c | Ð | .21E-00 | N | .12E-04 | •11E-04 | .99E-05 | • 98E-05 | .87E-05 | • 87E-05 | •71E-05 | .70E-05 | .5 yE -0 > | .59E-05 | .48E-05 | . 4 bE -05 | • 40E -05 | .39E-05 | •33E-05 | .33E-05 | .26E-05 | .26E-05 | .21E-05 | .21E-05 | .16E-05 | .16E-05 | •11E-05 | .11E-05 | •65E-06 | •64E-00 | .21E-06 | 21E-0 | 11E-0 | 1E-0 | 7E-0 | 5E−0 | o F - 0 | 4F-0 | •6 9E -05 | ae −0 | .5 dE-05 | 7E-0 |
|--------|-------------|---------|---|---------|-------|--------|---------|--------|-------------|---------------|---------|--------|---------|---------|---------|----------|---------|----------|---------|---------|------------|-----------|----------|------------|-----------|---------|---------|----------|---------|----------|---------|---------|---------|---------|---------|----------|----------|---------|---------|--------|--------|--------|--------|--------|---------|--------|-----------|--------|----------|---------|
| | OKCE | 0143 | 2410 | .01480 | 0112 | 0112 | 7200 | 11 | 45 | 0045 | 14 | 41 | 34 | 7 | 69 | 962 | 36 | 35 | 9 | 6/ | 0454 | 20 | 036 | U365 | 0293 | .02920 | 0540 | 0240 | ~ | \sim 1 | മ | .01478 | _ | 0111 | ~ | 0077 | 0 | 2 | 0014 | 0013 | 1116 | 0 | | 44 | - | 27 | 78 | 5 | 7 | 7677O. |
| | ء ر | 9086 | 7,7,7, | 977 | .9464 | 1946 | 9011 | 9015 | ი3 ს | .9632 | 469 | 9 | 823 | 43 | 352 | 335 | 149 | 157 | 444 | .449 | 651 | 53 | 754 | 755 | .83 | 878 | .840 | 801 | 606. | 910 | 8 F 6 | 956. | .947 | .947 | .961 | -965 | .963 | 406. | 0 6 | 9 70 | 27 | 714 | 315 | 207 | . 16 | .180 | .424 | 1.7 | 0 | G 000 |
| | 700 | . 3810 | 21000 | 1.9 | 13951 | 5666. | +004 | .400 | 0104. | .4011 | . 4034 | .4035 | 4206 | 4244 | 045 | . 815U | .0722 | .0700 | 9707. | .20 Jb | .2849 | 8 C A 7 8 | . 3245 | 0628. | 355 | 3558 | .3714 | .3718 | .3820 | . 3821 | . 3421 | 4765. | . 3953 | 3925 | • 4005 | . 4008 | .4012 | | • 4036 | .4037 | 576 | 69486. | 8269 | 0440 | 8O. | . U863 | .2059 | 0.602. | | . 2006 |
| | 7 / | 7, | | . 10948 | 424 | 5 | 67 660. | 7 | 7 p | -4 | .01825 | .01014 | . 20171 | .25811 | 61510. | 8040g. | .6/7/3 | 09019. | .600613 | .60158 | .51346 | 01616. | .43177 | 676750 | .35703 | .355/1 | .29733 | .29590 | .23966 | .23870 | • 16868 | .18700 | .14212 | .14152 | 55850. | 0/850. | . 058 U4 | 60240. | .01807 | .01772 | .25206 | 407 | 62666. | .50203 | 0.2 | 226 | 196 | 3 | | 2 |
| | : ح | 0.421 | 7 7 | 10 | 0.25 | 14. | βC | 0.7 | 2 | 300 | olo | -4 | 10400. | .34316 | 50 CC2. | 7 | , C | ا د | _ | prod | .03217 | 0 | 00700. | .0/149 | 96/40. | .004/2 | \circ | _ | 96670. | .03424 | .02271 | 97970. | 9 | 670 | _ | 3 | w. | ~ : | 770 | ر د | 0 | V |) | 334 | 200 | , I c | ı | 140 | 9 | 01671. |
| | Χ · | . 300L | 1 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - | | 11000 | 1.3010 | 1.3700 | 1. | 1.3140 | 1. | 1.4033 | 1.4034 | 1200 | • | .4047 | 4/17 | 81543 | 71 | 1.001 | 1.0340 | 1.1/20 | 1.1/44 | -1.25058 | 1.2515 | -1.30091 | | _ | -1.33802 | ~ | _ | _ | _ | 1.30 | 1. 30B | 1.33/ | 1.3972 | 1.4000 | 1.400 | 1.4035 | 1.4030 | ~ | 20339 | - | 2 | - | .8371 | 1.0381 | 1.0450 | 1 / | 1.179 |
| | 7 | 7 4 4 5 | 200 | 1 3 | 4025 | ري | 7. | 45845 | 00 | $\overline{}$ | V | ~ | 2 | .64524 | _ | 137 | 13 | 91 | 67907. | 17017. | 34 | 67676. | 00 | ئ | . 3 y4 dú | 03 | 77 | 2 | Ω | 21 | 5 | 23 | 7 + 5 | 00 | 7 5 | 35 | 0 | 36 | 52 | 39 | 43 | 7, | 32 | 77 | 27602. | 70 | 5 | : 0 | .31420 | 2 |
| | > | , , | | - ; | 6433 | 7410 | 6490 | 490 | 047) | 470 | 6470 | 4.70 | 164 | 51656. | ~ | 4 | 4 | 5/556. | J | 7 | J | 41646. | 87648. | b) 656° | ~ | 5/656. | 164 | 1646 | 165 | - 5 + | 7.7 | 5/656 | 247 | 497 | 764 | . 949 15 | 49. | 6.5 | 49/ | 1656. | 1640. | .149 | 1640. | .1490 | 1.6 | .1470 | 1650. | 14 | 16,6 | 1.14904 |
| | ~ | 3 | ٦. | 1 ~ | ~ | ٠.٥ | 7 | .13175 | .07901 | .07745 | .02401 | .02432 | .89515 | .8/019 | 65347 | 87678 | .78335 | .76151 | 949690 | .67704 | 3 | ဘ | Ň | _ | 4 | \sim | 3.7 | 36 | \circ | Jr. | ₹ . | സ | О. | 7 | \sim | ~J 1 | _ | 0 | \sim | \sim | 1 | | 024 | 713 | 64 | 079 | 24% | 567 | | 481 |
| X FLUN | P.I. | 101 | 163 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 | 171 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 | 131 | 132 | 133 | 134 | 135 | 1.36 | 13/ | 138 | 139 | 140 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149' | 150 |



| X F1 11 X | | | | • | | | | | | |
|-------------|----------|-----------|---------|----------|--------|----------------|--------------|----------|---------|--------------|
| - - - | *(| >- | 7 | × > | × * | 4,2 | 22 | 6.0 | SOURCE | |
| 51 | .48921 | 1.04970 | 7 | 12526 | ,00 | .4 40 23 | 1676. | 72752 | 0305 | • 47F-0 |
| 52 | 470/4. | ·1490 | ر. ب | 1.2.4 | 1 4 | 64774. | .360 | . 700 | 0363 | |
| 53 | .41303 | 440. | 17 | 1.3002 | 0021 | .35301 | 3506 | .840 | 02.42 | 3.9E-0 |
| 54 | .34765 | .14 | 0 | 1, 30,11 | 10/ | | 166. | .841 | 291 | 38E-0 |
| 55 | .34985 | 640. | .30735 | 7) | 2.4 | .29401 | 312 | 883 | 0239 | m |
| 99 | .33629 | .141 | 12 | 1.3404 | 200 | . 4 | .372 | . 464 | 0239 | 32E-U |
| 57 | .23647 | 0. | 9 | 1.3014 | 8 d | . 23732 | 386. | .911 | 0192 | 26E-0 |
| 98 | .2 (537 | ٦. | 40 | 1.3019 | 430 | .23554 | . 38 | .912 | 191 | 5E-0 |
| 59 | .24762 | ٥. | 50 | 1.3190 | 20 | | 96. | .439 | 147 | 1E-0 |
| 20 | .21879 | | J. | 1026.1 | 333 | .18557 | .39 | .940 | .01472 | 1E-0 |
| 51 | .17244 | | 97 | 1.300 | 777 | .14001 | 75. | 644. | 111 | 10E-0 |
| 52 | .10624 | •14 | 0 | 1.500 | 150 | .13904 | 95. | 646. | 0111 | 15E-0 |
| 53 | .12094 | ₽O. | 0.7 | 1.341 | V | .09815 | . 40 | .962 | 71100. | 1E-0 |
| 54 | .11625 | .14 | 2 | 7 | 11110. | 16740. | .40 | .903 | 0076 | 1 1E-0 |
| 55 | .07110 | • 04 | 63 | 1.400 | - 3 | .05740 | 0.40 | 406. | 0045 | 64E |
| 56 | .00834 | • 14 | ~ | 1.400 | ~ | . 02704 | . 40 | 606. | 4 | 3E-0 |
| 167 | .02232 | .04 | 5 | 1.403 | \sim | | . 40 | 07.5. | 0013 | 20E |
| 168 | .02146 | .14 | 20 | 1.404 | - | $\overline{}$ | 04. | _ | . 00139 | 20E |
| 109 | .77179 | . 24 | | 0 + 7 . | 4120 | ~ | . 5 B | _ | E801 | 116 |
| 170 | .72939 | . 34 | | 107. | 104 | .22907 | 63 | 10 | .10013 | 1 OE |
| 171 | .73507 | .24 | | .534 | 3/14 | · 1 | 086000 | m | 4560 | 376 |
| 172 | ++669. | . 34 | | .503 | 4104 | .54889 | 88 | ~ 1 | .09187 | ш |
| 173 | .67540 | .24 | | . 444 | 17.50 | | .09 | .196 | 0770 | 82 |
| 174 | 62863. | . 34 | | 200. | ဂဗ္ဗဂ | ~ | .10 | -0 | 0711 | BUE |
| 175 | .60094 | .24 | | . 0 v | 51 | ш, | . 21 | .469 | 0572 | |
| 176 | .56747 | .34 | | -1.00054 | 370 | 5 | . 21 | .401 | 0566 | |
| 177 | .52293 | • 24 | | .102 | 7 4 | 7 | 67. | 609 | 0447 | |
| 178 | 07764. | ٠ 34 | | 1001. | 114 | 2 | 67. | .6 /0 | .04450 | |
| 179 | •44804 | •24 | | .2503 | υ2 υ | 4 1 | .32 | .763 | 0363 | |
| 180 | .44399 | • 34 | | . 2090 | - | 7 t | ، ع ک | .707 | . U3b05 | |
| 181 | .37938 | . 2. | | .3100 | V | 1 | ξς . | .844 | .02903 | |
| 182 | .35853 | • 34 | . 32109 | .312 | 470 | 34 | 35 | _ | . 02894 | .37E-05 |
| 183 | •37024 | • 24 | | .3414 | V | ζo | .57 | .886 | . 02385 | |
| 104 | .30321 | ٠ 34 | | . 3724 | 97/ | 20 | .37 | 828 | 36 | |
| 165 | .26272 | . 24 | | . 3626 | 96 | 23 | , 3d | .913 | 91 | |
| 186 | 248 | ٠ 3 4 | | 5505. | 504 | 73 | 35. | 4 | .01705 | |
| 187 | .208/4 | , 7, | | 3000 | 7/5 | ງ ເ | .34 | .941 | 46 | |
| 1 c 8 | .19723 | . 34 | | . 3011 | V | η Ω | . 445 | .942 | 46 | |
| 607 | 00001. | 47. | 0 1 | ٠, | 507 | ς ₁ | . 39 C | 950 | 07 | |
| 06.1 | . 14983 | • 10 0 | 00 | .3690 | 77 | ~ | 065. | 950 | 0 | |
| 191 | 15011. | . 24 | გ | ٠, | 7 7 4 | <u>></u> | . 40 t | .904 | 9/ | |
| | .10482 | • 34 | 4 | . 3783 | 1270 | 7 | .40 | 4 | 9 | ш |
| | .00520 | • 5 4 | 20 | .4000 | 1 J 2 | 0.5 | · 402 | • 465 | 5 | Z. |
| 194 | .06162 | .349 | . 30717 | _ | 677 | .055/3 | 70 | .906 | 44 | E-0 |
| | .02047 | • 2 4 | 2 | 64049 | 035 | \neg | • 4044 | .972 | 14 | シドー 0 |
| | .01935 | • 34 | USO. | . 4040 | 040 | - | .4045 | .973 | 014 | >E −0 |
| | 0 p | 444 | اد زار | 345. | 5. | - | 6973 | 19616. | 032 | E -0 |
| | 7 | . 54 | # | .4616 | 117 | • 20206 | 63 | 07 | 77 | 7E-0 |
| 199 | 2 | 447 | 3 | ,000. | 0 | V | 10 | Ω | 83 | α III |
| 2 0 0 | .5 45 40 | 1.54919 | . 07801 | 1.64901 | | 60644. | | 41060. | .08708 | |
| | | | | | | | | | | |



| | VNOKMAL | . 7 a£ -0 | 0 F = 0 | 63E-0 | 2E-0 | •54E-05 | 2E-0 | 4E-0 | 3E−0 | o E −0 | υE −0 | 1E-0 | 1E-0 | 5E−0 | 5E-0 | OE-0 | yE+0 | 156-0 | 14E-0 | 0E-0 | 0E-0 | 60E-0 | 7E−0 | 1 y E - 0 | ž | Z E | 8 5 E | 8 LE | S. | 73E | λ E | 60E | 7E | 끸 | 7 | 111 | 111 | ш | .36E-05 | ш | ш | 꾸 | 4E | 7 | | 4 | 4 | OE | Ø | 0 € −0 | 7-10 |
|--------|------------|-----------|---------|---------|---------|---------|--------|---------|------------|---------|-------|-------|--------|---------|--------|--------|---------|--------|---------|--------|--------|--------|------------|-----------|--------|---------|--------|--------|---------|--------|--------|---------------|--------|-------------|-----------|-----------|--------|--------|---------|-----------|--------|--------|---------|---------|--------|-------|------------|--------|--------|--------|---------|
| | SOURCE | .0700 | 0664 | 50 | 20 | •04400 | 34 | 7 | 25 | 57 | 33 | 34 | 5 | 36 | 35 | 5 | 4 | 9 | . 01087 | 76 | 5 | 44 | 44 | E | 13 | .09427 | 65 | 0832 | 773 | 0661 | 57 | 34 | 70 | 54 | 70 | 45 | 333 | 277 | 4 | 526 | 18 | 82 | 76 | 41 | 137 | 107 | 104 | 4 | 20 | 043 | 04.7 |
| | ره | 24240 | .278 | 6445 | .515 | 0/8 | .087 | .771 | .779 | . 450 | .854 | .890 | .891 | .915 | .915 | .940 | .941 | .950 | .950 | .905 | 406. | 996. | .966 | ~ | .973 | .20744 | _ | .004 | 139 | .328 | 404 | 54409 | 56903 | 704 | 73108 | 78849 | 80709 | 668. | 80g | .874 | 868. | . 416 | 1 α | .941 | .942 | 2 | 066. | 963 | . 403 | 765 | 240 |
| | 200 | .1146 | 7 | . 4240 | 01620 | 1 | 7667. | .3310 | .3328 | .3001 | .3617 | .3748 | .3754 | 45 BE . | .3836 | 1666. | . 39 32 | 3905 | .3906 | 8401B | 9104. | . 4023 | .4022 | .4047 | .4040 | .6559 | 760 B | .0024 | .0674 | 1567 | . 1852 | .2466 | .2608 | . 3053 | .3157 | 6188. | .3445 | ,36,0 | .3672 | . 3703 | .3700 | . 3844 | 5 de 0 | . 34 32 | 7665. | .3903 | . 39 to to | . 4012 | 407 | 6104. | 4014 |
| | ٧ ٢ | .00227 | .5/343 | .52103 | 15056. | .47919 | .40324 | .40240 | .3 y 0 4 B | . 33544 | 12 | 1 | .27251 | •26619 | \sim | .17341 | - | .13452 | 13127 | 27560. | .071/0 | .05479 | .05361 | .01730 | .01606 | . 18219 | .15452 | .45135 | .341.52 | .53435 | .47519 | 59664. | 145627 | . 44041 | .40441 | .37203 | .34504 | .31292 | .27104 | .26117 | .24317 | 120 | . 19811 | 6/4 | 7 | 77 | 180 | 283 | 021 | Ŋ | 3 |
| | ۲, | 477 | 3 | 320 | 100 | 170 | 976 | 1011 | 1480 | 014 | 541 | دان | 724 | 2 | 171 | 83 | ಲ | 2 | 410 | 447 | .02800 | | | .00451 | 91400° | | \sim | 80766. | .~ | - | 7 | 7 | J | - | 1 | LC | 7 | 7 | 16101. | \supset | 7 | 2 | 7 | 740 | 141 | 1 C C | 000 | 5.3 | 3 | 2, | 1 2 2 |
| | × > | 4010b | 00% | . 000 | 144 | 171 | 1,186 | 2011 | 1007. | 9745 | τ, | .3430 | .3+42 | .3030 | +36+£ | . მისი | .3014 | 70000 | .3095 | .3444 | .376, | .4012 | 4017 | .4040 | 1.404 | 1075. | . 6575 | ~ | . 8103 | . 441v | 7916. | 1.0 | 1.130 | 1.20 | 1 . 2 2 7 | 1.613 | 1.204 | 1.320 | . 3616 | 1.3 | 1.300 | 1.305 | 1.30/5 | 1.301 | 1.3067 | 5 | 1.5304 | 1.3700 | 1.33 | . 4006 | 1.4(1)) |
| | 7 | .10909 | 3 | 111 | 110 | 67462. | 334 | 1007 | 257 | 300 | 2754 | 313 | 207 | 23 | 5 | 37 | 303 | 330 | | 0 | 27 | 7, | 1 4 | 43 | 51 | 67 | 47 | 3 | 5 | 139 | 113 | 1/8 | 20 | 2 ∪8 | 1 78 | 3 | 150 | 246 | 0.7 | 56 | 61 | 502 | 2.2 | / 1 | 32 | 2 | 30 | 5 | .23384 | 0 | |
| | > | .4443 | . 54.11 | 64443 | . 5491 | .4443 | 1669. | 6444. | 16,59. | 64443 | 1649. | 64443 | 1646. | 64443 | . 5491 | .4493 | 1669. | 66.44 | 1646. | 64449 | 16,54. | .4493 | . 541 | 64413 | . 5491 | .6489 | . 7484 | .6487 | . 7484 | •6489 | .7484 | 6446 | .7484 | 6496 | . 7484 | 4 6 4 E Y | • 7484 | . 5484 | . 7484 | .6487 | . 7484 | .6467 | • 7484 | .6463 | . 7484 | •648 | • 7484 | .6404 | 7484 | 68484 | 7484 |
| | ~ | 35 | 4 | 67 | 3 | 1 | 63 | 5 | 363 | 34 | S. | 2 c 3 | 59 | 31 | 212 | 43 | 168 | 95 | 78 | 47 | 62 | 57 | 52 | 3 | 97 | 3 | 17 | 32 | 55 | 408 | 417 | 34 | 7.1 | 28 | 323 | 47 | 277 | 14 | 34 | 32 | 96 | 1 49 | c 2 | 50 | 5.0 | 4 | 9 6 | 000 | .00804 | .04715 | 40 |
| X FLOW | ٠, | 201 | 0 | \circ | \circ | \circ | \neg | \circ | \circ | 0 | - | - | - | - | - | - | _ | - | - | -4 | \sim | \sim | \sim | \sim | \sim | \sim | 2 | 2 | \sim | 2 | .m | \sim | 3 | 3 | ო . | າ : | ~ | 7 | 7 | ~ | 3 | J* | \$ | 3 | J* | J. | \$ | \$ | 248 | 3 | 5 |

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| | V NUKMAL | .19E-00 | .18E-06 | .75E-05 | .54E-05 | •6 0 € -0 > | .5 UE-05 | . 6 JE-05 | .40E-05 | .53E-05 | .39E-05 | .40E-05 | .34E-05 | • 4 1E -05 | .29E-05 | .35E-05 | .24E-05 | .2%E-05 | .20E-05 | .23E-05 | .16E-05 | •16E-05 | •13E-05 | •14E-05 | .99E-06 | .97E-06 | .60E-06 | .5 4E-06 | .41E-0b | .18E-06 | ·13E-06 |
|--------|----------|----------|----------|---------|-----------|-------------|-----------|-----------|----------|----------|----------|----------|----------|------------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|----------|-----------|----------|----------|---------------|----------|----------|----------|
| | SOURCE | .00133 | .00131 | .07431 | • 04460 | . 06 76 2 | .04050 | .05616 | .03420 | .04656 | .02820 | .03720 | .02311 | .03024 | .01898 | .02469 | .01572 | . 02045 | .01295 | .01057 | .01049 | .01292 | • 00 k 31 | 62600. | .00621 | . U0678 | • 00444 | • 00389 | .00243 | .00121 | . 00080 |
| | c P | 47176 | 07.07 6 | 20124 | 63526 | 34377 | 08607 | 53124 | 75728 | 6/250 | 81647 | 78182 | 86725 | 835 07 | +9668 | 80076 | 67086- | 40683 | 64654- | 42403 | 40343 | 04446- | 106/6- | 95166 | 98586 | 403/4 | 90 566- | 96422 | 44667 | 91,896 | 99972 |
| | ABS.V | 1.4041Y | 1.40 364 | 1.09001 | 1.27077 | 1.15921 | 44047 • I | 1.23755 | 1.32563 | 1.24325 | 1.34770 | 1.53485 | 1.36647 | 1.35465 | 1.37028 | 1,37141 | 1.38935 | 1.30089 | 1.39625 | 1.38710 | 1.40140 | 1.39445 | 1.40080 | 1.39702 | 1.40 > 20 | 1.40134 | 1.41247 | 1 4 4 0 1 5 1 | 1.41.304 | 1.40313 | 1.41411 |
| | 7, | .01504 | 41410. | ·11499 | 9+9¢0. | .30024 | .14603 | .5 1973 | .19033 | 67715. | .19101 | .34016 | .10116 | .29203 | .15903 | 10247. | .13952 | 64607* | .11974 | .17160 | •09800 | .13654 | 05570. | .10352 | • 000 12 | .67255 | 668800 | .04242 | .02474 | .01323 | .00794 |
| | > * | 550000 | .00/03 | 10010. | . 40611 | 02400. | .46702 | . 403JB | 40106. | 30206. | 46617. | .20117 | 96477. | 00477. | .10078 | .1/809 | .14575 | .1450E | .11913 | 11541 | 80440. | 97607. | .0 /4 05 | .00012 | .02539 | .04001 | . 03678 | . 026/4 | .04179 | .00827 | 260000. |
| | × > | -1.40±09 | -1.400/4 | くてくらひ・- | / 5101.1- | 454/3 | -1.21/33 | -1.00017 | -1.20301 | -1.104c2 | -1.30424 | -1.2,405 | -1.33500 | -1.30342 | -1.35/01 | -1.30615 | -1.3/402 | -1.35769 | -1.30000 | -1.3/159 | -1.34408 | -1.30469 | -1.40657 | -1.34158 | -1.40601 | -1.378/0 | -1.41127 | -1.40062 | -1.41205 | -1.40304 | -1.41467 |
| | · a | 061020 | 17147. | .61941 | 1/ 070. | .05647 | -03500 | . 093 Jd | 66160. | •11945 | 90500. | .1392E | .01617 | . 15398 | 16500. | .10470 | .0000 | .1/108 | 8/750. | •1777 | .09791 | .18176 | .10023 | .10403 | 10105 | .10015 | 10279 | .15798 | .10307 | 3 | .10401 |
| | > | .6407 | 1.74943 | .647 | 69533 | .8472 | 1,93333 | 1.84725 | . 4333 | 1.64725 | • | 1.84724 | 1.93333 | 1.84725 | • | .8472 | 1.93333 | 1.64724 | .9333 | 1.84725 | 13, | .847 | 1.93333 | .8472 | 1.93333 | 1.84724 | .9333 | 1.84725 | .9333 | 724 | 1.93333 |
| | × | .01401 | .01267 | .37344 | .20594 | .35606 | .19635 | .32600 | 709 | .29055 | .10023 | .25302 | .13954 | .21708 | .11971 | .18355 | .10123 | .15524 | .02501 | .12712 | .07010 | .10100 | .05570 | > | .04232 | .05367 | 09670. | .03155 | .01740 | 660 | •00246 |
| X FLUX | - | 251 | 252 | 253 | 254 | 255 | 256 | 257 | 258 | 259 | 260 | 261 | 292 | 263 | 564 | 265 | 206 | 207 | 268 | 209 | 270 | 271 | 272 | 273 | 274 | 275 | 2.76 | 277 | 278 | 279 | 2 80 |

SAMPLE PROBLEM INJANIAL ELLIPSGIO

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| 2 | , W | 5 bE-0 | loe | .48E-0 | • 1 4E -0 | .43E-0 | .12E-0 | . 30E-0 | • 11E-0 | • 3 AE | .93E | 20E | • 8 2E −0 | 25E | . BUE | .24E | 36 | 2 2 E | 7 SE | 2 Z E | 7 1E | 2.1E | 7 0E | 21E-0 | 6 y E | .20E-0 | 6 yE -0 | .2 vE-0 | .92E-0 | 1 3E-0 | RUE-0 | E-0 | .71 | .97E-0 | 0 0 | • 80E -0 | 52E-0 | • / TE=0 | - 40E - | 6 2E -0 | 74. | .57E-0 | • | 5 JE -0 | .37E-0 | 5 UE-0 | .30E-0 | .50E-0 | 35E-0 | 4 o E - 0 |
|---|--------|-------------|-------|--------|-----------|--------|--------|---------|---------|---------|--------|---------|-----------|--------|----------|---------|--------|--------|-------------|---------|------------|---------|------------------------|------------|--------|----------|------------------------|------------------------|--------|--------|--------|--------|------------|--------|---------------|-------------|------------|-----------|----------|------------|--------|--------|---------|----------|---------|---------------|--------|--------|---------|-----------|
| SOURCE | .001 | 3500 | 0010 | - | 8 | 20 | ~ | 23 | 9 | • 00700 | Ω | | ٠. | .00184 | 9 | 17 | 5 | 17 | .0005c | .00170 | 5 | . ^ | 5 | 9 | 005 | 16 | 002 | 91 | 59 | ω R | 053 | 52 | 043 | 7 | 038 | 054 | 950 | V 4 0 0 | 250 | 040 |) (| 43 | 0 3 0 | 045 | 67 | 4 | 970 | 40 | 028 | 650 |
| a. | 5.0 | .2 /1 | 7 | | .2721 | -4 | .2/15 | .2708 | Ø | .2 102 | .2704 | Ŋ | .2094 | .2694 | .2696 | .2092 | .2094 | ァ | .2091 | .2687 | .2687 | S | .2089 | .2685 | .2088 | 984 | .2688 | .2084 | .2081 | .2632 | •5064 | .2654 | 2697. | .2063 | ر ا | 4997 | 0,507.0 | 0/07. | 0007. | 0/07: | .2082 | 9 o | .2082 | .2061 | 280 | .2000 | 2070 | 4405. | 2077 | 2064 |
| ABS - V | 70 | 1.12/56 | 43 | 0/2 | 1 28 | 14 | 0/7 | 273 | : /3 | 270 | 77 | 203 | 503 | 907 | 107 | 505 | 907 | 504 | 502 | 263 | 204 | 263 | 40 | 202 | 407 | 202 | 564 | 202 | 201 | 539 | 00 | 249 | 00. | 253 | ٠ د د | ر ا ا | C 2 | , vo |) () | 200 | 502 | 255 | 0.7 | 355 | 200 | 254 | 25.9 | 254 | 259 | 1253 |
| ٧ ٪ | 00700. | ς Ω 1 | 5 | 107 | 120 | 545 | 1790 | 547 | 077 | .02365 | 077 | 0231 | 5 | .02257 | . 667 39 | \circ | 672000 | .02161 | .00715 | .04100 | $^{\circ}$ | \circ | $\mathbf{\mathcal{I}}$ | $^{\circ}$ | \sim | .02124 | $\mathbf{\mathcal{I}}$ | $\mathbf{\mathcal{I}}$ | _ | .01979 | .034/3 | .04879 | .04100 | J : | \mathcal{L} | 66750 | → · | - | 00000 | ン 、 | .03764 | · · | \$1750. | S | 03000 | $\overline{}$ | - | 020 | 5 | 00 |
| > | | 1221. | 7 | .1475 | 12/21. | 1270 | 15/0 | .1207 | 1771 | 1971. | 1771 | .1266 | 1269 | .1264 | 1661 | .1263 | .1260 | 1666 | .1402 | .14 | .14 | 12 | 1. | 1. | .12 | -1.12006 | 16 | . 1-to | 1631. | 0677. | .124, | 1214 | 77. | 1771 | 1256 | . 1635 | 1250 | • L | 0021. | 1471. | 1250 | .1646 | 1655 | 174710 | .1254 | . 1242 | .1254 | 7 | .1253 | .1245 |
| > | ٥ | 04.1 | 0.405 | ve110. | - | - | * | | # | J | | •6010b | 00200. | 55C00. | .00158 | .004 75 | .00122 | .00306 | 5 4 C n O • | 005/900 | 01000. | 402CO. | 44000. | .00145 | ,0002d | • 00000 | 40000. | •00025 | .00001 | 65050. | 247000 | .073/1 | 01560. | 10660. | 00470 | 195000 | 54770. | 70470. | 17610. | .01862 | 20010. | 27410. | 96200. | .01162 | 1 1000. | . UUdud | 30400. | 44900° | 6,45000 | .00412 |
| - | 0.140 | 217 | 150 | 100 | 2464 | 400 | 191 | 153 | 3.60 | 50 | ~ | 90 | 36 | 34 | 3 | 3 | 20 | 2 | 70 | 00 | 5 | ~ | 1/2 | 3 | 7 | 36 | 7 | 69885. | .001c0 | 79040. | 15475 | 115317 | .24458 | 1/247. | 87676 | .31138 | | | 0.4 U | ∓ (| 321 | 77 | 0 ! | 4 | 502 | 57 | 175 | .41392 | 260 | 010 |
| > | 66650 | - J | | 444 | 5 | 464 | 49 | 2 | 65650. | 2 | 2 | . 14197 | 2 | ひかる | 5 | イカカ | 664 | 499 | 5550 | 14887 | 049 | .14957 | 4 | 14697 | 4 | 1 | 04 | 14997 | 24645 | 34443 | 4375 | 34625 | 24995 | 265,46 | 24652 | 24648 | 24442 | 34476 | τ. | ا 1 | 2 4 | ب 1 | 5 | 34 | 4 | 34 | .24995 | 3 | -T | 34 |
| A | 698968 | G & | 45 | .94050 | .80521 | *8C304 | .76924 | .70731 | .66989 | .60621 | .57471 | .57367 | 85 | 640477 | .41100 | 26605. | .33655 | .33571 | .26741 | .20674 | .20317 | .20266 | .14208 | .14173 | .00352 | .00332 | .02622 | •05616 | .98124 | | | | 82868 | | | | | | | | | 8 . | 06205 | 50 | 34 | 3 | 69 | .26335 | 2 | 0 |
| Y FLUW | - | 2 | ٣ | 4 | 2 | 9 | 7 | 80 | 0 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 07 | 71 | 22 | 23 | 47 | 57 | | ~ 17 | | 67 | 30 | 31 | 32 | 13. 13. | 4.0 | 35 | 50 1 | 3. | χη Ο 0 | 60 | 0 . | 7 7 | 74 | 43 | 44 | 45 | 46 | 47 | 4.8 | Q.4 | 90 |



| | - | 1 | × > | > | 7 > | E 2 . | _ | • | KMAL |
|-----------|---------|---------|---------------|-----------|----------------|----------|-----------|----------|-------------|
| 101 | * | ,00 | 470 | -1.12533 | 2 | 1. L2589 | 201 | .00279 | 34E-08 |
| 5 | | 3 | ناکال | -1.12421 | 20' | 1.12535 | . 206 | ~ | 47E-00 |
| | ~ | 3 | * (:0144 | -1.12531 | 36460. | 1.1256/ | 4.20729 | 002 | 34E-0 |
| - | า | 3 | 220 | -1.1414 | 0 | i.12530 | .266 | 003 | 40F-0 |
| * | - 4 | 3 | 2 | -1.12530 | 354 | 1.12560 | .267 | 200 | 34E- |
| 73 | | 7. | 300 | -1. 1.418 | 7 | 1.12529 | -200 | 7 | .40E-0 |
| (4.) | 4 | 30 | 047 | -1.11376 | .045.00 | 1.12099 | •256 | 0 | 10E-0/ |
| \circ | -4 | 7.4 | 136 | -1.10001 | 56160. | 1.11702 | .247 | 7 | .10t-0 |
| Œ. | 05555 | 11201. | 040 | -1.11007 | .00323 | 1.12252 | 200 | • 00074 | 14E-07 |
| - | 4 | 0 | | -1.11045 | .07764 | 1.11936 | . 252 | .01202 | 10E-0 |
| CT3 | ٧. | 2 0 | 3 | -1.11423 | 01410 | 1.12.554 | .202 | 96/00. | 12E-07 |
| \sim | 4. | 27 | | -1.11478 | •07575 | 1.12117 | 762. | . 00 987 | .14E-0 |
| O. | 4 | Ω C | .0440 | -1.16079 | .07514 | 1.12420 | .203 | \sim | 1 UE -0 |
| σ | 5 | 2 | - | -1.11700 | .09241 | 1.12630 | .259 | .00880 | .12E-0 |
| ~ | 4 | 0 | _ | -1.12104 | •07305 | 1.12440 | 26442 | 900 | .80E-0 |
| 47449 | 4 | 50 | 2920 | -1.11054 | . 09034 | 1.12286 | .260 | 007 | .10E-0 |
| 410ء | -V | 7 | - 4 | -1.12211 | .0/045 | 1.12460 | .2 54 | 005 | 77E-0 |
| 5271 | 54 | 12 | 0290 | 4. 11. 1- | \circ | 1.12.522 | .201 | 200 | .91E-0 |
| 1307 | 1 | 00624. | 0103 | -1.12237 | .06916 | 1.12464 | .264 | 0056 | .71E-0 |
| ,733 | 2 | 7 | 3220 | -1.1.906 | $^{\circ}$ | 1.12334 | .201 | 00 70 | • 8 3k −0 |
| 40057 | 4 | 443 | 0145 | -1.12247 | | 1.12461 | .2 04 | 0054 | .66E-0 |
| 1526 | 3 | 5 | 7 | -1.12014 | .00392 | 1.12343 | .2 62 | 0068 | 77E-08 |
| 1087 | ろんりゃ | 450 | 1.1 | -1.12226 | 06990. | 1.12461 | 407. | 0053 | .62E-0 |
| 366 | 5410 | 2 | 0570 | -1.12035 | .00264 | 1.12346 | 202 | 9900 | .73E-0 |
| 2001 | 044.440 | 00604. | 40000 | -1.12257 | .06616 | 1.12455 | \sim | 005 | • 6 ∠E -0 |
| 0716 | 775 | 2 | COTO | -1.12044 | _ | 1.12340 | .202 | 0004 | .72E-0 |
| 1805 | 494 | ŝ | 200 | -1.12200 | .06562 | 1.12423 | 204 | 51 | 54E-08 |
| 1539 | 543 | 2 | 075 | -1.16048 | .00100 | 1.12344 | .202 | 90 | 69E-0 |
| 3848 | 777 | 7 | 1 1 0 | -1.12201 | .00520 | 1.12451 | 204 | _ | 5 bE-08 |
| 3664 | ф Ф | 5 | 400 | -1.12054 | .0000 | 1.12345 | 202 | 63 | •68E-0 |
| 141 | 6,44 | 2 | 770 | -1.16264 | J | 1.12452 | 2 o 4 | 21 | .57E-0 |
| 0.32 | 4 ب | 5 | .00322 | -1.12056 | .000s | 1.12345 | 202 | .00632 | 66E-06 |
| 556 | 7 7 | رئ ا | 700 | -1.12204 | .06404 | 101711 | •504 | 50 | .57E-0 |
| 225 | 543 | 2 | 000 | -1.12059 | .08020 | 1.12346 | 20215 | 5.0 | 66E-08 |
| 526 | | ည ၁ | 925 | -1.07627 | .03747 | 1.11200 | 236 | 00 | .21E-0 |
| 676 | 763 | 4 7 C | 4777 | -1.06436 | . C4360 | 1.10585 | .275 | .01473 | .23E-0 |
| 172 | 64 | 477 | 40.0 | -1.10264 | 260 | 1.11538 | 544 | 44 | 18E-07 |
| 1408 | 7, | 1-14 | 7 | -1.09201 | 1083 | 1.11627 | .232 | 9 | .20E-0 |
| 1345 | 7 | 2,31 | 146 | -1.10862 | .1102 | 1.11020 | 95.20 | 18 | 16E-07 |
| 1526 | , T | 2285 | .11018 | ä | .1507 | 1.11449 | \sim | 30 | .1/E-0 |
| 1767 | 55 | 0 56 | 7 | _ | • 1 1 | 1.11997 | •254 | 2 | .1 JE-0 |
| 1327 | Ţ, | 156 | ٠,٦ | _ | 671. | 1.11099 | .247 | .01237 | 14E-0/ |
| 1369 | 2 | .34957 | 21740. | -1.1.4/4 | .10 | 1.12096 | 35 | * | • 12E-0 |
| 67115 | 5 | 770 | $^{\prime}$ | | • | 1.11049 | .251 | 10 | • 1 3E -0 |
| \sim | 7 | 000 | $\overline{}$ | ä | • 1 | 1.12141 | 257 | ρp | .1 UE-0 |
| \sim | 6.5 | 100 | 7 | _ | .14 | 1.11934 | .252 | 40 | 11E-07 |
| 2 | 7 | 177 | -4 | 1.1100 | 1023 | 1.12161 | .258 | 83 | 9 |
| 5003 | 20046. | 2 | ه اد | . 1 | 1071 | 1.11983 | 54 | . 00987 | 10E-07 |
| \approx | 7 | 346.04. | 00176. | 1.11/2 | 10053 | 1-1/174 | 258 75 | 200015 | X 0 - U : X |
| | | | | | | | | 4 | |



| | V NÜKMAL | 8 1E | 38/E-0 | 3 BUE-0 | 8 82E-0 | 7 70 | 2 8 2E -0 | b75E-0 | 3 BUE-0 | 773E-0 | 78E-0 | +73E-0 | 0-30E-0 | J24E | 324E-0 | 521E-0 | 121E-0 | 210E-0 | 018E-0 | 015E | 15E | J 13E | 713E | 711E | 4 11E | +10E | 1 10E | J 90E | 3 - 45E | a - 69E | 78 b E | Ι ~! · | - NoF | | 170°L | 1 7 0 · 1 | | 1,735 | - BOB | 70E | 2 24E | 42¢Ë | 216 | 19E | 1dE | 917E | | 15E |
|--------|----------|----------|---------|---------|---------|---------|--------------|---------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|-----------|-----------|-----------|----------|----------|----------|----------|-----------|----------|----------|----------|----------|---------------|-----------|------------|------------------|--------------|----------------|---------|---------|--------------|----------|----------|---------|---------|---------|---------|---------|-----------|--------|
| | SOURCE | 6/00. | 00 43 | F2200° | 2 | 91 | 0 | 32 | E6800* | 0075 | . 00891 | 0075 | .00685 | .02160 | .02468 | 75 | .02231 | 00 | 4 9 | 43 | 0103 | .01280 | .0146 | .0170 | . 01384 | . 01144 | .01311 | . 01110 | .0127 | 8 | .01247 | .0105 | 0170 | 0104 | OTTO OTTO | 2010 | 0110 | 3010. | 0102 | 0117 | 0279 | 0313 | 0252 | 284 | 60 | 0236 | 1 | .01870 |
| | می | 7 | | 57 | 55 | 50 | 50 | 59 | 5 | 59 | 55 | .259 | 55 | 90 | 90 | 19 | 202 | 32 | 672. | 665. | •278 | 244 | 36 | 46 | 2 | 48 | 47 | 657. | 43 | 0 | .243 | .250 | .244 | 062. | 1170 | 2 3 | 7.79 | 777 | . 3 | .245 | 101 | 132 | .102 | 157 | 204 | .105 | 3 - 0 | 0 |
| | ABS.V | 1.12,05 | 1.12020 | 1.12200 | 1.12056 | 1.12212 | 1.12039 | 1.12212 | 1.12045 | 1.12614 | 1.12045 | 1.12212 | 1.12040 | 1.09035 | 1.00921 | 1.10424 | 1,090,1 | 1.11009 | 1.10451 | 1.11347 | 1.10501 | 1.11550 | 1.11161 | 1.11607 | 1.11337 | 1.11741 | 1.11439 | 1.11774 | 1.11490 | 1.11005 | 1.11520 | 1.11017 | 1.11550 | 1.11.027 | 70071-1 | 1.11522 | 1.11836 | 1,11577 | 1.11035 | 19911 ** | 1.07/00 | 1.06400 | 1.08/43 | 1.07004 | 1.09759 | 1.08091 | _ | 0101 |
| | 7 A | 61640. | .11626 | .09801 | 114,1 | 91770. | .11405 | 06960. | .11345 | 27960. | .113 US | .09613 | .11276 | 26650. | 99960. | .12455 | .14112 | .14853 | .16901 | .14992 | .1/107 | .14632 | .10/10 | .14223 | .10257 | · 1 20 06 | .15873 | .15640 | .15600 | • 1 3444 | .15388 | .13296 | 41241. | 15106 | 06067 | 0.10.1 | 1 2042 | 0.004 | 13052 | .14930 | 38800. | 9070. | 158/6 | 7,6 | 106 | 134 | 5 | , |
| | > | -1.11724 | 7740 | 77. | 1. | • | • 1 <u>i</u> | ٠1، | . 1 . | • 1 T | 11. | 11. | 111 | -1.00,09 | -1.00256 | -1.00104 | -1.00057 | -1.07217 | -1.000171 | -1.049 70 | -1.0.0.18 | -1.10405 | -1.05617 | -1.10052 | -1.10004 | -1.10014 | -1.10222 | -1.10906 | -1.10343 | -1.10971 | -1.10431 | -1.11010 | 04 40T • T | -1.11039 | 1 1 2 | -1.11057 | 7007-1 | 10000 | -1.011-1-071 | -1.105/8 | -1.35008 | 30.5 | .0480 | 1.0001 | 0300. | 1.0019 | -1,000039 | 1 |
| | Y * | .01007 | 17.7 | 20710. | C/470. | 06600. | .01113 | .00000 | 00/00. | 10800. | .00451 | .00115 | 42100° | 36647. | 44475. | 10702 | 00212. | .12002 | 014440 | 447.00. | AATOT. | .003/7 | .07200 | 04840. | 67440. | .030/1 | 00750. | .02721 | 75500. | .6779. | .0.5/5 | 60110. | 556TO. | 90770. | 404409 | | 2/530 | 7 3 3 | 001 | 001 | . 30811 | . 34213 | 90657. | .20007 | .10300 | .10209 | (11240) | 1 |
| | v .1 | 30848. | .) | 250 | 07 244. | .46203 | 2 | J | | 2 | c 1 4 | 21 | 230 | .04053 | 7 | 1410 | 7.7 | 431 | 101 | こっしょ | 707 | 4440 | .32525 | 7 7 | . 32861 | 3 74 | ر س | -1 | 3 ' | 3 | 413 | 4550 | 535 | 75 |) .) ? | 0 - 10 1 | 100 |) 2 | 452 | 29.4 | 43 | - 1 | 1 | 1 7 | 150 | .20105 | V1507* |) |
| | > | ** | | Ŧ | 74 | , 9 | 1 | 7 | 4 | 4 | 4 | 4 | 1 | 87658. | 4 | 1 | 7 4 | 4 | 2 | 20 (1 | J | .64978 | -T | J. | T. | 4 | 4 | 4 | 7 | 1 | ્ર જ | 20 g | σ . Σ : | р 3 С | 7 3 | 56.140 | - 1 |) (L | - X | 7 | .04 | 14 | .04 | .1. | ۰ (۲ | .149 | 1.04970 | |
| | × | .31830 | 937506 | 54545 | .24745 | .19219 | .10839 | .13440 | .13175 | .07901 | .07745 | .02481 | .02432 | .89515 | 67028. | .85347 | .82963 | .78335 | 16107. | •69646 | •6//04 | .60651 | .53960 | .52034 | .50583 | .44001 | 47774 | .37211 | .30174 | .36471 | .29621 | .24210 | 55555 | . 18345 17882 | 70211 | 17505 | .07562 | 56570 | .02374 | .04368 | .84159 | .60896 | .80241 | .77130 | .736.48 | .70743 | 67,400 | |
| Y FLUK | | 0.1 | 20 | 03 | 0.4 | 05 | 90 | 20 | 0.8 | 60 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 70 | 17 | 22 | 23 | 47 | 55 | 97 | 27 | 28 | 67 | 30 | 41 | 36 | 2.5 | ר ע | 35 | 37 | . sc | 9.6 | 40 | 4 1 | 4.2 | 43 | 77 | 45 | 46 | 47 | , |



| 7. | 1,717 1,717 1,717 1,720 1,117 1,125 1,117 1,134 1,117 1,17 1,17 1,17 1,17 1,17 1,17 1, | 0.076.0 0.076.0 0.076.0 1.72.0 1.7 | | 30.735 30.735 30.735 40.012 30.401 30.401 30.200 10.0702 10.0703 10.0203 1 | 14964 14970 14970 14974 14969 14969 |
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| | 1/4/co 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 0.02/0.7 0.04/0.7 0.04/0.4 0.04/0 | 1004/02 1744/0 1 | 100010 | 14946 |
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| ٦. | | 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | | 25.05 .0000/8 -1.094950 .1.09425 .1.09426 .1.094 | 14964 40723 000078 -1.09799 114964 40723 000196 -1.097165 114964 40723 000196 -1.097165 114964 40857 000196 -1.097161 114964 40857 000124 -1.097161 11701 -1.097161 -1.097 |
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| | 00 | 94742 900001 90666 03115 00474 000474 000225 00225 | | 241340 - 34752 - 34752 - 347522 - 37312 - 341340 - 3413342 - 3213342 - 3413342 - 3413342 - 3413342 - 3413342 - 3413342 - 341340 - | 24946 .01012 .41390 -1.01392 .24997 .24948 .01711 .24994 -1.0108 .24994 .12108 .24994 .12108 .24997 .24994 .12109 .24995 .24997 .19101 .24997 .20101 .24997 .201325 .24997 .201325 .24997 .201325 .24997 .27202 .10448 .100474 .27202 .10448 .100474 .27202 .10448 .100476 .27202 .24997 .27202 .11711 -1.04302 .24996 .24997 .31823 .01748 .100924 .25997 .24948 .27202 .11711 -1.04302 .24948 .27202 .11711 -1.04302 .25999 .24948 .27202 .11711 -1.04302 .25999 .24948 .27202 .11711 -1.04302 .25999 .24948 .27202 .100912 .100924 .25999 .24948 .27202 .100912 .100924 .25999 .100912 .100924 .25999 .100912 .1009 |
| 1 | · · | 00001 00115 00115 000474 00040 002812 | | 241340 - 141342 - 141 | .34948 .0271 .41370 -1.0372 .249948 .12108 .32025 .249948 .1210 .32005 -1.00001 .120495 .32005 .12108 .24995 .19236 .19201 .1020 |
| 1 | ١ | .00001 .90000 .00115 .00474 .00474 | -1.60001 -1.03115 -1.03115 -1.00474 -1.00474 -1.004812 -1.004825 -1.004825 | 100001 - 09205 - 100001 - 100001 - 100001 - 100001 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 1000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 10000000 - 100000000 | .24997 .12108 .27959 -1.00051 .1 .34948 .11510 .32605 -90606 .2 .34948 .10510 .26752 -1.03115 .2 .34948 .10151 .26757 -1.00474 .2 .34998 .2.325 .10207 -1.02812 .2 .34948 .27202 .10448 -1.02812 .2 .34948 .27202 .11711 -1.04302 .2 .34948 .30075 .00912 .1 |
| ٦, | _ (| 0.5115 0.0474 0.0000 0.0000 0.0000 | | 25.00 - 320056 - 300066 - 3000 | .34948 .11210 .32605 -90606 .2 .24957 .19236 .20726 -1.03115 .2 .34948 .10101 .22727 -1.00474 .2 .34948 .2.325 .10207 -1.02812 .2 .24957 .20447 .10448 -1.00225 .2 .34948 .27202 .11711 -1.04302 .2 .34948 .30075 .00912 -1.00924 |
| | \sim | 00474 05000 05812 06225 | -1.00474 -1.00404 -1.002812 -1.00285 -1.04362 -1.04362 | 1001 | 24948 |
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| 7 | ~ | . 02812 .00225 .04362 .2 | -1.02812 -1.00225 -1.04362 -1.04364 | | .34948 .2.325 .10207 -1.02812 .2 .24957 .20847 .10448 -1.00225 .2 .34948 .27202 .11711 -1.04362 .2 .24957 .31823 .0746 -1.00924 .2 .34948 .30075 .00912 -1.0236 .2 |
| 7 | ~ | .04362 .2 | -1.04362 .2 -1.04362 .2 -1.06954 .2 | 7202 | .24927 .27262 .11711 -1.04362 .2 .24948 .27262 .11711 -1.04362 .2 .24957 .31863 .07746 -1.06964 .2 .34948 .30075 .09912 -1.0536 .2 |
| ٠, ٦ | A | .04366 | -1.04362 | 2027 - 11/11 - 120424 - 2 2027 - 11/11 - 120424 - 2 2027 - 2027 - 2027 | . 24948 . 31823 |
| - - | A 1.7 | . 009.4 | | | .34948 .30075 .00812 -1.00230 .2 |
| 1 | '\ | 5. 05240. | -1.02230 .2 | 2. 062c0.I- 21800. 6/006 | |
| -4 - | - 4 1 | 0/3/6 | -1.0/3/6 | 3.03.0 - 1.07.0 - 2.003. | 3. 01510.1- 52000. 2505. 76842. |
|) · | A . | 2. VEST | -1.05819 -1.05819 | 2. PIBCU-I- 00/20. CAR | • • • • • • • • • • • • • • • • • • • |
| · ,- | 9 1/ | 00136 | -1.000136 | 25. (2010) 1 - (210) 30 (2) (2) (2) | 2. 35 00.01 |
| - → | 1 ~ | .0/837 | -1.07837 .2 | 2. 728/0-1- 2000. AVO. | |
| 1. | ~ | . 00500° | -1.00308 .2 | 4678 .04175 -1.00308 .2 | .34948 .34678 .04175 -1.00508 .2 |
| 1 | 9 | 1.07975 | -1.07975 | 7504 -1.07975 . | .24957 .37504 .37504 .37504 . |
| 7 | . 4 |]. 8cdu0.l | -1.00059 . i | 600.1- lolto. | .34948 .3500 005ct. 1.04948 |
| J. | . 4 | 1.00006 | -1.00056 | 5. 340001- 11120. | 5. 30169 .11120 .05000 .75945. |
| .4 | 7470 | 1.00000 .247 | -1.00000 .247 | 5072 .023/7 -1.00006 .247 | •34948 •36072 •02317 -1.06666 •247 |
| → | 77 | 17. 61100.1 | -1.00119 .21 | 17. 61100.1- 7.64.0. 6860 | .24455 - 41600.1- 16410 34586. Fe445 |
| 1. | 54 | . 00754 .24 | -1.00754 .24 | 04/5 01040 -1.00794 .24 | |
| 7 | 2170 | 15. 00154 . 21 | 1.00124 . 21 | 15. 40100.1- 40000. 108 | .24945 • 4 • 4 • 4 • 4 • 4 • 4 • 4 • 4 • 4 • |
| | 24 | 1.00808 .24 | -1.0c808 .24 | 24 −1.00808 .24 | •3+9+8 •36717 •0896 •1.06808 |
| | 2167 | .00173 .2167 | 56 -1.00173 .2167 | 7912. 67100.1- 36200. 008 | .24457 .30400 .00256 -1.00173 .2167 |
| 1. | 2445 | . 00000. | 1.0000 . 2445 | . UUZUI -1.000000. | •34948 •36836 •1.00001 -1.000650 |
| • | 0927 | 5240. 05408. | 15 68430 .0927 | 7540 888430 .0427 | 5449. 05484.— AUICA. 96460. 36444 |
| | 100 | 2001. 3241 | 6001. devise- 70788 | 1001. devisi 1003. | .549.4 devision - 15754. 1605. |
| | 2 | .96303 .2380 | 18 92303 .2380 | 751 . 32918 92383 .2386 | 0852 19751 - 31865 19701. 05844. |
| | 202 | 202 | 40 80010 . 2005 | 1801 - 37240 8001U . 2005 | .54919 .01801 .2005. |



.10E-08 .33E-09 -.11E-00 . 43E-08 .34E-09 . 8 DE -09 .62E-08 .14E-08 .16E-08 .65E-08 .65E-08 . 60E-00 .82E-06 94E-08 2 3E-07 -.40E-08 . 20E-00 -.23E-08 .34E-00 -. 1 yE -0 y .50E-08 •56E-08 .57E-08 .12E-08 .63E-06 .1/E-08 87E-08 .2 st -07 .21E-07 .22E-07 .10E-07 .24E-07 . 2 3E-0 / .12E-07 .22E-07 .23E-07 . 1 3E-07 , 2 sE-07 .13E-07 2 3E-07 , 1 3E-07 136-07 22E-07 2 3E -07 -.63E-00 .12E-07 11E-0' 1 3E-0 / V NURMAL .03197 .02419 . U2358 . U2719 .02620 .02271 .05201 04207 02636 02506 , 12665 ,02299 .02640 .02018 05246 04414 03934 03225 03840 03167 03793 03087 .03890 03034 02887 .02312 , 02274 02259 .02604 ,05579 .06353 04475 04083 04825 03714 63533 03107 03090 UBobo 03054 03050 03724 DURCE -.148/3 -.17980 -.15075 -.13707 -.17413 .11904 -.16649 -.17829 -.16029 -.18118 -.15256 .31736 -.0452B 006/01--.07876 -.10216 -.146UB -.10539 -.15842 -.12078 -.13107 -.17001 --14241 -.17676 -.14607 -.15104 .10082 .15874 .05203 -.06473 .00367 -.08756 -.09407 -.01738 -.02876 -. 03196 -.1054B -. U 76 48 .04171 -.008c4 727.60. .02361 -.00764 -.02409 -.03611 -- 10412 1.08641 1.08204 1.06662 .04280 1.08549 1.07179 1.00019 .03186 . 99010 .01/90 1.06584 1607001 40504. .43660 16099. 96666 . 47364 .. 03075 1.03/78 .07055 1.05137 ..07630 19060 .. *0000· ..06380 1.08357 1.08479 1.07054 ..07273 .. 08682 . 22022 . 47843 .91721 .00-41 .. 02234 . 48012 .00381 1.04590 .00005 .. 04831 26110. .64784 .U1420 110000 . 615 dt31504 .10728 20200 30101 32205 27719 31543 27602 31933 11209 30104 34600 38024 4346937509 43109 30204 34055 33533 24154 33017 20738 32575 20301 20111 27472 31747 27800 30201 42706 38444 42205 34105 24603 31622 43549 3/141 42824 42513 30536 36351 50105 30542 30707 46324 -1.048c0 -1.02575 -1.02630 -. 42656 -1. U.d 3' -1.02905 -1.03714 -1.00757 -1.04141 -1.01330 -1.04406 -1.01708 -1.04709 -1.02092 -1.02319 -1.04404 -1.06462 -1.02040 74.050.1--. 73361 -. 61534 -- 70147 -.07591 **-**644465 -. 75500 -.90003 51010 ---. 43245 -.35026 -.9505 17618.--. 40340 -. 6,216 -. 47118 -, 90311 20/16--. 41142 5.70158 06/16-- , 10462 - . Jobus -. 403,1 -. 99771 (2)06.-- 4090 10100 90210 10740 14542 07770 01010 53484 24775 11364 Oceso 3250 600000 02720 00100 01510 51413 4444 45056 30910 53757 10508 1001 10011 600 / 4 01400 04704 04204 00333 00341 25247 りつりんり 00011 07273 00307 01334 7/040 30000 .25346 .34203 .31539 12506 19909 .11905 .25744 31332 21603 30024 27542 24084 3.306 33667 30833 31435 34303 00814 11844 15273 20002 23014 21004 25649 2/100 23246 61422 35153 30343 34043 0.2403 24510 13913 17351 1,0013 21957 21902 20537 22707 23660 40007 2001 . 44436 . 54919 .44936 . 54919 066550 .44936 .54919 4, 74.49. 67654. .44130 67645. . 54919 67649. .44936 67649 . 54919 .74843 . 74843 61666. .44936 .44936 . 54414 .44436 .44436 ..64872 .64892 .74843 . 14843 54849. .74843 .64872 . 74843 .64892 .64892 .74843 .64692 .64072 .74842 .54872 .74443 .64872 74844. .64016 1. 141.42 .7484 .16412 .13989 .12832 .09783 .55815 .23477 54647 52906 48586 40126 .30300 .23173 .43420 4431134572 .25959 12918 20300 53217 41745 37818 .32445 .10999 10258 30696 .08974 05275 01806 48844 .32360 237752 .23202 15096 11470 09815 16760. 47701 45537 19854 00864 00021 PT. 2002 2003 2005 2005 2007 2007 2008 2008 2008 2017 2015 2016 2018 219



| | V NUKMAL | .13E-07 | .24E-07 | .44E-07 | .71E-07 | .44E-07 | .65E-07 | .42E-07 | .62E-07 | .4 UE-07 | .55E-01 | .424-07 | .5 JE -07 | .42E-07 | .50E-07 | .41E-07 | .47E-07 | .40E-07 | .40E-07 | .37E-07 | . 45E-07 | .3 0E-07 | .44E-07 | .3 /E-07 | . 4 JE-07 | .30E-07 | . 4 3E-07 | .3 /E-07 | .42E-07 | .30E-07 | .42E-07 |
|---|------------|---------|----------|---------|---------|---------|-------------|------------|---------|----------|---------|---------|-----------|---------|----------|---------|----------|---------|---------|---------|---------------|----------|---------|----------|---------------|---------|-----------|----------|---------|---------|----------|
| | SOURCE | .03040 | .63043 | 64720. | . U845¤ | .06920 | . 08467 | 46190 | . 08234 | • 05 744 | .08234 | • 05205 | . 08086 | .04911 | .08064 | .04716 | < 9080 · | .04013 | .08013 | .04547 | .08051 | • 04460 | .0805 | 0.04442 | . 08036 | . 04384 | .08031 | .04362 | .08048 | .04340 | • 08044 |
| | a a | 10618 | 0.440 | .51100 | .43232 | .44115 | .79005 | .34100 | .73312 | .20302 | .68312 | .20036 | .64436 | .16233 | .61696 | .13310 | .54618 | 11406 | .50208 | 85640. | .57205 | .08743 | 60896. | .04032 | .52776 | .07483 | .55342 | .07156 | .55151 | .07003 | 92046. |
| | 463.4 | 1.05175 | 1.01/30 | 08963. | 044040 | .74756 | 64264. | .01130 | .51002 | .05012 | 74709. | .67423 | \$5969 | . 91524 | .61091 | .9310/ | .63547 | 64044. | 64585 | . 54401 | . 65418 | 70994. | • 66054 | 00654. | . 66501 | .56180 | .66789 | .96350 | 69699 | . 46435 | •67062 |
| | 7 4 | .36034 | 656750 | .11055 | . 64358 | 30695 | .24212 | 44004 | .34107 | 676940 | .41238 | .49136 | .45172 | .49600 | .4 75 60 | 99844. | .49251 | .45807 | .50244 | 604440 | *21074 | 00644. | .51619 | .45841 | * 2074 | .47801 | .52279 | .45841 | .52439 | .44827 | .5 25 22 |
| | <u>_</u> * | 10101 | +C071.0- | 12044 | 10106 | 30004 | 4 2 2 2 3 1 | 54547 | 40502- | 00360 | 30275 | 0.011 | 60955 | 75551 | 30097 | 14411- | 3/656 | 1.4001 | こうとうち・- | 80268 | 0166E | 41138 | 40596 | 41746 | 47 OT4 | 42100 | 40514 | 02439 | 46574 | 82503 | E4,975- |
| | Υ, | . 60426 | 12000. | .52620 | 10/06. | 40204 | 15156. | 26966. | 40707. | 64017. | .23407 | . 410/1 | 117500 | 12601. | 10636 | 6/901. | .13377 | 4111. | 0 11210 | 8088O. | .07125 | 00000. | 1-1/0. | .00168 | 418000 | 003460. | 6,4560. | 0.020. | .02213 | .00623 | 06000. |
| | 1 | .20170 | .241.1 | 11410. | .010/1 | .02877 | 50250° | . 0 + 3 ud | £6160. | .11942 | · Gusur | .1555 | 16010. | .1539∂ | .00491 | .10470 | .05083 | .1/138 | 007478 | .17754 | .07771 | .10176 | .10023 | .10400 | . 10165 | .10075 | .10249 | 10718 | .10307 | .10800 | .10401 |
| | _ | 1.04032 | 1.74843 | 1.84725 | 1.43333 | 1.84725 | 1.93333 | 1.84725 | 1.9333 | 1.84725 | 1.93333 | 1.84724 | 1.93333 | 1.84725 | 1.43333 | 1.84725 | 1.93333 | 1.84724 | 1.93333 | 1.84725 | 1.93333 | 1.84725 | 1.93333 | 1.84725 | 1.93333 | 1.04724 | 1.93333 | 1.84725 | 1.93333 | 1.84725 | 1.93333 |
| | ~ | .01401 | .01267 | .37344 | •5020 | 35606 | .19635 | .32660 | .10022 | •24055 | .16023 | .25302 | .13954 | .21708 | .11971 | .14356 | .10123 | .15524 | .00501 | .14712 | .07019 | .10100 | .05570 | .07674 | .04232 | .05367 | 07670* | .03125 | 04210. | .06991 | .00546 |
| 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |



| | NOKMAL | .30E-0 | . 30E-0 | • 8 LE -0 | 8 TE -0 | | • 4 O F | 1 OF 10 | 1000 | 0-387° | 1 OF -0 | 10E-0 | . 1 UE -0 | .10E-0 | .10E-0 | 0E-0 | .10E-0 | 0E-0 | .95E-0 | 5E-0 | .97E-0 | .97E-0 | 96E-0 | | 97E-05 | 47E-05 | .40E-0 | 96E-05 | .30E-0 | 30E-0 | .80E-0 | .80E-0 | 90E-0 | . 90E-0 | . 1 UE -0 | 1 vE-0 | .98E-0 | . 90E-0 | .1 UE -0 | 1 UE-0 | 1 UE-0 | .10E-0 | .10E-0 | UE-0 | 1 0ë-0 | 0E-0 | .45E | .45E-0 | 9/E-0 | 1100 |
|---|-------------|-----------|---|-----------|---------|---|---------|---------|--------|--------|------------|---------|-----------|--------|--------|--------|---------|---------------|---------|----------|---------|--------|--------|--------|--------|--------|--------|---------|--------|--------|--------|--------|--------|---------|------------------|--------|---------|--|----------|---------|--------|--------|--------|---------|--------|--------|--------|------------|--------|------|
| | URCE | 0445 | 0447 | 6611 | 7 7 7 V | 1540 | 1779 | 1778 | 1865 | 1804 | 1932 | 1932 | 928 | 1957 | 1979 | 6261 | 666T. | *19994 | 1981 | 1961 | 8661 | 1997 | 446 | 9661 | 9007 | 2006 | 2003 | . 20030 | 0445 | 0441 | 1197 | 9.5 | 1508 | 1500 | 1777 | 1775 | 1863 | 1862 | 1691 | 1930 | 27 | 1925 | 1978 | 116 | 866 | 746 | 51 | 1979 | 1997 | |
| 4 | ئ د د | 4.921 | 276. | 07776 | 3.218 | 7 | 001.1 | 602 | 100 | 054 | 323 | 320 | 502 | 900 | 90 | 704 | 817 | 15 | 8 40 | 808 | 437 | 935 | 80 | 967 | 696 | 987 | 78 | 9 | 23 | 676.4 | 3.222 | .227 | 1.713 | .721 | • 666 | •676 | 059 | 067 | 91 | S | かり | 547 | 669 | 693 | 811 | 0.4 | 8 | 110 | 30 | |
| | AUS. | 11 11 1 · | 0 4 4 4 3 5 | 1000 | 00000 | 7447 | - ^. | 4607. | 4470 | . 0208 | .0220 | 0 4 7 9 | 6615 | 6032 | 417 | 5437 | 210 | 4674 | 5312 | 3343 | 508 | 2548 | 703 | 1813 | 1045 | .11364 | 342 | .0502 | .4337 | .4330 | .0546 | 0050. | 73 | • 6476 | .2911 | 1462. | .0291 | .U3 32 | 6020 | 315 | 603 | 125 | 5401 | 540 | 344 | 914 | 341 | 474 | 479 | 1 |
| | 7 / | 726.7 | 225. | 77/07 | 77/17 | | | 0/3 | 4 2 3 | 474. | .273 | .274 | .117 | 1/8 | .119 | .120 | 910 | 0/0. | .045 | 040 | 025 | 970 | 017 | .013 | 0 C 4 | .005 | 000. | .001 | .362 | 2.383 | 1.714 | .716 | 1.008 | .071 | .612 | 9/9. | .426 | 675. | .276 | 617. | .160 | .103 | 122 | .164 | .077 | 000. | * | .020 | 970. | |
| | × , | # 1000 · | . U. C. | 27.470 | 20000° | 70.4:0 | 2000 | .05451 | 10710. | 00220. | .01712 | .05105 | .01655 | 60000. | .01039 | 64640. | .01241 | .04846 | 91910. | .04773 | .01234 | .04702 | .01010 | .04754 | 11510. | .04742 | .01573 | .04/55 | 36160. | 01440. | .0/653 | .10722 | 65050. | .12/14 | .07106 | .12860 | .0000 | 16507 | .00622 | .12102 | .003/2 | .115/4 | 66700. | . 116/1 | .00123 | .11459 | .0002 | 14611. | 96610. | |
| | × > | 7006. | • | • | • | • | 1.10047 | | • | 84556. | +06//- | 66611. | 00/60. | 0)300. | 91026. | 00876. | . 4.003 | 99675. | . 32713 | . 34 700 | . 24963 | 60047. | 016/1. | .1/403 | ·10324 | .10336 | 04000. | 4000° | 647775 | | • | • | 1.2335 | • | • | • | 6,4766. | .93125 | .71406 | .713.11 | 61869. | Tobbo. | 10176. | 179 | 7 | 7 | 327 | 340 | 5 | |
| | J. | 7.7 | 7 ; | 2 7 7 | 100 | 1 1 2 2 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 | .31617 | 315 | 30.9 | 10 | 407 | 4 06 | 436 | 454 | 3 | 3 | 3 | ນ ງ | 0 | S | 3 | 50 | 7. | 443 | 197 | ž | 64 | 18 | 7 | 0 | 154 | 153 | 244 | 7 | ال ال قرار في | 7 | ၁ | ლ ე | 2 | 7 | 32 | 57 | 7 | ~ T | 2 | 3 | 041730 | 3 | -; | |
| 1 | _ : | 77.50 | 7 | | 7477 | , , | 4.5.7 | 7 | 4440 | 664 | ハハカ | 1499 | 444 | 751 | 444 | 56.5 | 464 | 56.4 | 499 | ハイナ | 454 | 565 | 444 | 1499 | 665 | かこか | 175 | 1425 | 555 | 3497 | 664 | 3494 | 5459 | 3477 | 5467 | 3497 | イグフ | 2492 | 5422 | 3497 | 5494 | 655 | 2447 | 3449 | 444 | 46.5 | 244 | 555 | 6,1,1, | |
| | × : | υ υ | 200 | 7 . | 1,0 | 3 (| 76.9 | 767 | 679 | 668 | 574 | 573 | 485 | 454 | 11 | 60 | 3 | 335 | t 7 | 206 | 203 | 202 | 142 | 141 | £ 3 | 683 | 97 | 56 | 81 | 73 | 35 | 876 | 858 | 56 | 703 | 57 | 6.4 | 5 | 20 | 9 | 82 | 7 8 | 07 | Š | 34 | 31 | 25 | c 3 | 0 | |
| 7 | ٠١. | ٦, | 7 6 | n 4 | t u | ٠ 4 | ۰ ۲ | · 00 | · > | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 1.6 | 19 | 70 | 21 | 22 | 23 | 24 | 25 | 5.6 | 27 | 28 | 67 | 30 | 31 | 32 | 3.3 | 34 | 35 | 36 | 37 | 3.3 3.3 3.3 3.3 3.3 3.3 3.3 3.3 3.3 3.3 | 39 | 40 | 41 | 4.2 | 43 | 77 | 45 | 94 | 47 | 48 | 64 | |



| | V NUKRAL L CAELOR | - 405-05 | 9 /E-05 | 97E-05 | 90E-05 | YOE -05 | 31E-05 | 3 1E-05 | 00E-05 | buE-0> | 8 yE-05 | 84E-05 | 10E-04 | 10E-04 | 94E-05 | 96E-U5 | 1 UE-04 | 10E-04 | 10E-04 | 10E-04 | 10E-04 | 10E-04 | 10E-04 | 10E-04 | 95E-05 | 95E-05 | 97E-05 | 97E-05 | 90E-05 | 96E-05 | 47E-05 | 97E-05 | 90E-05 | 90E-05 | 30E-05 | 30E-05 | d 1E-05 | 81E-05 | 89E-05 | 89E-05 | 97E-05 | 99E-05 | 96E-05 | 98E-05 | 10E-04 | 10E-04 | 1 UE -04 | 1 UE-04 | 10E-04 | 10E-04 |
|--------|----------------------|----------|---------|--------|----------|---------|--------|---------|---------|----------|---------|---------|---------|---------|--------|---------------|---------------|--------|--------|---------------|---------------|---------|--------|---------|----------|--------|--------|--------------|--------|---------|------------|---------|---------|--------|--------|-----------|---------|----------|---------|---------|---------|---------|---------|---------|---------|--------|----------|---------|--------|--------------|
| 9 | 300KE | 197 | 5007 | 4007 | 2007 | 2001 | 441 | 0439 | .11926 | . 11097 | 64 | 1500 | 13 | 0/ | 09 | 57 | 28 | 976 | 954 | 322 | .0 | 4/6 | 0 | .+ | 918 | .19764 | .19946 | .19929 | .19931 | .19916 | . 20033 | . 20016 | . 20001 | .19984 | •04379 | .04357 | .11893 | 184 | 27 | 551 | 767 | 62 | .18549 | 0687 | 23 | 19 | 1950 | 1946 | 971 | 468 |
| 3 | 5 | 2 | 982 | 9/6 | 992 | 906 | 976. | .930 | .236 | .246 | .733 | 747 | 000 | .701 | 17 | 240 | 248 | 284 | 39 | 575 | 03 | 671 | 25 | 783 | 868 | 27 | 918 | 904 | 947 | 936 | 968 | 926 | 78 | 996 | 4.939 | 7 * 6 4 5 | 3.201 | .277 | 1.763 | 1.786 | •716 | .743 | 50 | .133 | 8 | 46 | 10 | 408 | 55 | 36 |
| 3 | 70.71 | ¢8/07• | .13042 | 15771 | 404 BU • | .11588 | • | • | | • | • | 1.05/47 | • | • | • | • | .83769 | .84569 | .6/869 | . 68893 | . 56274 | . 57335 | .45.01 | . 46478 | .36279 | .31156 | 19067 | . 20730 | .22341 | . 25130 | .17041 | +5107. | .14021 | .18210 | • | • | • | • | • | • | • | • | 1.65356 | • | . 65538 | .86783 | 66449 | .71494 | .58714 | .60674 |
| ` > | | 17 | 00000 | 00932 | 00290 | 00537 | 2.384 | | | -1.72314 | | | 600 34 | 66634 | 43380 | 02864 | 2a3Jy | 28869 | 18604 | 19212 | 12852 | 13338 | 08463 | -•088p | 67450 | 058/4 | 65460- | 638.77 | 02107 | 02520 | 01274 | 01722 | 00871 | 01322 | | | _ | -1.73002 | _ | - | 69305 | 70244 | 64944- | -,45545 | .2453 | .303/ | .196 | .2065 | 1345 | 4 7 |
| ; | | .11213 | • | _ | \circ | 901T1. | 61/ | 510 | 12892 | 1/005 | 404 | 20314 | 10575 | .20532 | 10615 | ,20074 | $\overline{}$ | _ | ~ | .14047 | $\overline{}$ | _ | | _ | _ | .10202 | | .10079 | | .17990 | .14503 | -1 | .14404 | 11907 | 290 | 7.70 | | 2125 | 24243 | 375 | .24514 | 40107. | 7 | 1 | 66862. | .2/305 | .22745 | | .24400 | ~ |
| | -17407 | | .10364 | 14001. | .01029 | £+050. | 17604. | 45654. | 1.12227 | 1.11011 | 1.22016 | 1.2.102 | 1.02201 | 1.0,012 | 47676. | 0,4074. | .71251 | BC011. | 61450. | + C 5 5 5 5 4 | .52652 | 75676. | .41801 | . 41752 | . 34/05 | .32548 | .24898 | 654744 | .17450 | .1/309 | .10313 | .10204 | 07050. | 5000° | 40104 | 040140 | 1.10849 | 1.090/3 | 1.21500 | 1.20/00 | 1.60554 | 1.07990 | 4630 | 7.6 | 3 | 4401 | 6,11 | to c | 7 | 77 |
| | 2000 | 7.10 | .41344 | 101 | 755 | 111 | 700° | 404 | 152 | 100 | 401 | 0107 | Jan | 304, | .30017 | くささら | 773 | 16 | C 7 | 7 | 43 | ٦, | 20 | 5 | 2 | 22 | 2 | 0 | 0 | 5 | 5 | 65 | Ĵ | 0 | 5 | 470 | 477 | 144 | 2011 | 2285 | 066 | 731 | 2 | 37 C | びさい | 08/ | 421 | ~ | ۲0۲ | 21, |
| > | - 3 | 1.30 | 24, | 7 | 549 | 6.5 | 644 | 7 | 7 | 646 | 49 | .549cd | 2,5 | 63 | 5.4 | 7 | 4 | | 1 | 1 | 4 | ちゃら | 4. | 2 | (. 54 5) | 2 | 6-6 | 543 | 5.55 | 543 | 7 | 7 | 2 | 7 | 7 | 4 | 649 | 7 | むなび | 7.7 | 4 | 4.5 | 7 | 7 | 6. | 7 | 3 | 4 | 7.7 | ý. |
| , | .14161 | | | | .02603 | | | | .91876 | . 90657 | .84326 | .83203 | .74973 | .73978 | .65240 | •64424 | .50014 | .55271 | .47307 | .46738 | 240055 | 3 | .32801 | .32366 | 2 t | ζ, | 7 | - | Ξ | .13664 | .00141 | .00032 | •05556 | .02522 | .93526 | •91676 | .89172 | .87408 | | .80226 | .72707 | .71327 | .63363 | .62115 | 7 | 4.1 | 4.3 | .45003 | ~ | 20 |
| 2 FLUW | | 52 | 53 | 54 | 55 | 96 | 57 | 58 | 59 | 09 | ¢.1 | 62 | 63 | 64 | 65 | 90 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 42 | 75 | 92 | 77 | 78 | 62 | 90 | <i>د</i> 1 | 82 | 83 | 40 | c 5 | 96 | 2.5 | 99 | 60 | O7 | 91 | 42 | 66 | 76 | 55 | 96 | 26 | 96 | 66 | 100 |



| | V NUMMAL | S | 1 of | 90 PE | 5 | 7 | , Æ | 9 bt-05 | 906 | 97E | .97E | 906° | 90E | .30E | 30E | BUE | aue. | 8 o E | 8 V E | 3 | 9 8 E | 9 / E | 97E-05 | 10E | 10E-04 | 106 | 99E-05 | 1 CE | 1 CE-04 | ä | 100 | 95E | 95E | .97E | | 9 to E | 9 | .97E | 9.7E | 96 | . 96E | 30E | 2×E-05 | 3 % L | 7 & E | .84 | 89E-0> | 3 | 9E- | .97E-0 | 97E-05 |
|--------|----------|--------|---------|---------|---------|--------|----------|---------|---------|---------|---------|---------|---------|-----------|---------|----------|---------------|---------|---------------|---------|---------|---------|---------|--------|--------|--------|---------|---------|---------|--------|----------|----------|----------|---------|----------|------------|---------|---------|---------|--------|---------|--------------|---------|--------|--------|---------|--------|---------|--------|----------------|----------|
| | SUURCE | 546T. | 1989 | 51 6T | 1971 | 1990 | 987 | 686 | 986 | 666 | .19966 | 946 | 93 | 432 | 30 | .11/77 | .11702 | .15453 | . 15425 | 17567 | 542 | .18457 | 839 | 616 | 606 | 42 | 937 | 905 | 096 | 985 | 1981 | 1961 | 963 | 90 | 960 | 983 | 979 | 43 | 686 | 066 | 90 | 475 | 420 | 159 | 148 | 533 | 526 | .17471 | 736 | 832 | 878 |
| | ر | 1- | .75034 | \sim | رند | بد | .87100 | .92243 | 07404. | ٠. | 5 | 5 | .93518 | サイカサル・サー | 7 • 4 | (7) | 3.3 | 1.5 | 1 . c | 77107 | 30 | 15971 | Γ. | •22200 | .18949 | .40595 | .43439 | •61226 | .58356 | .72791 | \$0.669. | .80107 | .77422 | .84945 | .82203 | .88247 | \$9569. | 61506* | 979/8. | .91303 | ~ | 7 • 4 | 1 2 | 3. | 3.4 | χ | 7 ° 5 | 84950 | Ur. | \sim | 28597 |
| | Absov | 480 | 770 | 5 | 4100 | 336 | . 350 U4 | . 27080 | . 50071 | . 23720 | . 47383 | .21771 | . 25460 | 43455 | 2.44078 | 2.07360 | <.0801b | 1.07/77 | 1.00000 | 1.33082 | 1654501 | . 0.7 | ٦, | .0280. | 62004. | .73079 | 1975201 | 677200 | .64232 | 29175. | . 54059 | 10044. | 47517 | 38 | 19176. | 34 | 3 | . 31114 | . 35177 | 16467. | .33076 | | .4451 | .0802 | • | . /01 | | 4495 | .3746. | .110 | 1.13401 |
| | v 2 | 40440- | 1501. | 66473 | .071 | 044/3 | .051 | 03125 | 000 | 02204 | | D | 970. | 0.65.7 | . ~ | -1.74440 | $\overline{}$ | _ | $\overline{}$ | 71422 | 72800 | 400 i.4 | 946/4- | 31304 | 32667 | 21599 | 26032 | 15673 | 16830 | 11170 | 12267 | • | | 06061 | | 0 . | ٥, | 0. | 40. | 03404 | 7 | 4.346 | 2645.7 | 1.707 | 1.7030 | 59 | 1.1010 | 7455 | .7010 | 1 | |
| | > | 100220 | 60002. | .21627 | 01007. | 06012. | 01477. | 6/517. | . 22242 | . 41430 | . 25221 | . 41413 | . 25150 | .11440 | .12072 | 04812. | .31003 | .32615 | .31012 | .33000 | .31702 | .32403 | 30405. | .315/2 | 3005. | 500000 | .35179 | . 30353 | .34630 | .278/1 | .34120 | . 64503 | 33795 | . 67341 | 34456. | .27232 | . 33412 | .23129 | .33362 | .64156 | . 33637 | .14666 | . 15705 | 10646. | 50405. | 20614. | 7.5 | 64674. | 6) | :D -4 | .41109 |
| | × > | 41014 | 9 | 100.00 | . 36351 | 017+2. | 21016 | 11,507 | .1/203 | .1021t | 10257 | 10000 | .02001 | .4/003 | 40316 | | 1.0/342 | • | | • | .004 | 2 | ろつら | 701 | 00161. | 15070. | 479 | .52601 | 217 | .41291 | 411 | . 32300 | 341 | 740 | .24536 | 7/1 | .1/134 | 1063 | 1015 | 301 | 167 | 1664 | .4720 | 20cu. | 1900. | 1.17239 | · 1547 | 1.65402 | .0410 | 010 | |
| | 4 | 30425. | 40000 | 130 | 41,1 | -5 | دادز | 071 | 2004 | 201 | 014 | 123 | 5 | 60000 | 40 | 11136 | `` | 617 | 2 | o | 10 | 34 | 52 | 5 | 3 | .3,440 | 5 | 77 | 2 | 7 | 614 | Ω: | 7 | 74 | ن 5 : | 5 | 3 | 50 | 430 | 25 | 39 | 043 | 74 | \sim | 1.7 | Š | 010 | 160 | Ω | <i>5</i> -4 | ·3 UC 36 |
| | >- | 4 46 | 3 | 4.70 | 9.64 | 649 | 06.5 | 7.75 | 064 | 490 | 2,4 | 3/5 | 440 | 1 4,5 | 16.5 | 15. | 164 | 1 64 | 164 | 164 | 765 | 1.5 | 497 | 1.64 | 168 | 76 | 7.55 | 16.6 | 165 | 7.65 | 6.5 | <u> </u> | 65 | 755 | ~ : | 164 | 7 7 | 16.5 | | 4 | 1646. | 4,40 | .1490 | 1650. | .1440 | 1640. | .1496 | 1650 | .1490 | . 04.7 | 1.14904 |
| | ~ | .31835 | .312 05 | 61.202. | .24745 | .15213 | .18839 | .13440 | .11175 | .07901 | .07745 | .02431 | .02432 | 8 4 5 1 5 | .87019 | .85347 | 89678. | .78335 | .76151 | .62646 | •67704 | .60651 | 0.5886. | •52034 | .50583 | .44001 | 47.174. | .37211 | .30174 | .30471 | .29621 | 01242. | 65 55 55 | .16345 | .17862 | 12804 | .12505 | -0/505 | .07352 | .023/4 | .02308 | .84159 | 98898. | .80241 | .77130 | .73648 | .70793 | 62469. | 04679. | .5 /022 | .54811 |
| Z FLUW | | 0 | 102 | 103 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 | 171 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 150 | 131 | 132 | 133 | 134 | 135 | 136 | 137 | 138 | 139 | 140 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 |



| | V NUKMAL | _ | 1 UE-04 | 5 | _ | 7 | 9 | • 10E | .10E | 94E | 95E-05 | 97E | 97E-05 | 96E-05 | 96E | 37E | 386 | 90t-05 | 97E | 2 y E | Z & E | 7 0 E | 77E-05 | 8 y E | ЫBE | 10E | 7.7E | 97E-05 | 3 & E | 1 1 1 | ۳ د | • 10E | | 100. | , . | - 1 OF -0 4 | 2 5 | 956 | 986 | 98E | 906 | 96 | 96. | 44E-05 | 7 | 7 E | 27E | • 20E | ш | .n |
|--------|------------|---------|---------|--------|----------|--------|---------|---------|---------|---------|---------|--------|---------|---------|--------------|--------|------------|----------|---------|--------|--------|-------|----------|---------|---------|---------|---------------|---------|--------|-------------|------------|------------------|-----------|---------|---------|-------------|---------|---------|-----------|---------|--------|--------|-----------|--------|-----------|------|--------|-------|-------|--------|
| | SOURCE | 5 | . 18995 | 2 | 2 | .19582 | 71661. | . 19759 | . 19728 | .19579 | .19540 | .19740 | . 19710 | .19738 | 0 | 5 | .19404 | 2 | +19174 | .04133 | 2 | 11 | .11175 | .15120 | 07441. | .17283 | .17118 | 18 | Ð | 18 | ဆ | > : | 61 | 61 | 7 . | 7 - | C | 19 | 19 | 61 | 0 | 61 | ~ | 6 | 2 | 5 | 3 | 3 | 0 | J |
| | S.P. | 51 | ~ | 7,00 | 634460 | 48 | 7 | 0 4 | 19 | 6 | 96 | 30 | 45 | 7 7 | 000 | 43 | -4 | N | 911 | 666. | 9.016 | 3.453 | ^ | 2.020 | 2.105 | 97411 | .063 | - | 39 | 950 | 043 | 0 / 7 | ກ : | 447 | 30.4 | 700 | ם מ | 563 | 609 | 17 | 7 | 51 | .74603 | 7.4 | 57 | 999 | 5.039 | 6.3 | 3.595 | 3.700 |
| | 2 | .72120 | 3 | \sim | \circ | 477200 | .70623 | .57081 | *61054 | .51007 | . 55045 | 774640 | .50400 | . 42213 | 60006 | 12060. | 19644. | . 58,141 | 43 | • 44 | 4.5 | 77. | -15 | .73 | 9/• | 0 4 0 | • 43 | 1.100/4 | ٠1، | • | 1.02144 | 26240. | V 20 22 . | 79967 • | 56061. | 00200 | 10011. | 46045 | .55082 | . 61887 | .52446 | 01065. | .50310 | 7 | 3 | 601 | 5/4 | 794. | .1436 | 0 |
| | 7 1 | V | .362 | 2430 | 021 | .1825 | 010 | 130 | 15443 | 5 | .123 | 3 | 024 | 07143 | 7 | 1700. | 44670 | 07800- | 67537 | | | | -1.02663 | | | 794 (1 | 83004 | 54321 | 5//05 | 38679 | .4175 | 66,607. | s Lo 6 9 | 65579- | -,2550/ | - 20743 | 20102- | 1/541 | 12452 | 10344 | 11009 | • | 10122 | 1770 | 94.0. | 1252 | 2.4170 | 4240 | 1.855 | |
| | <u>,</u> , | ~ O | 4401. | 32906 | 47004. | .37216 | £0555. | 30108. | .437/1 | 10500. | .43326 | .30064 | .43014 | . 51463 | 67074. | .31708 | 90/24. | .31716 | . 42033 | .1/447 | 61110 | 47764 | 5+815· | .54575 | *5000¢ | 01056. | • to 0 3 c to | 50000 | .57627 | . 516.5 | 100000. | 7700A. | .57371 | 1020C• | 00100 | 1000 | 30000. | . 22240 | 3 | . SJUld | .40430 | ည ည | 402 | 463 | ر د کا | 754 | 8 | 001 | ٥ | 01914. |
| | ×× | 1251 | 405 | 071100 | 66.6.40. | 11416. | 3,500,0 | 640017 | 07007. | 37876 . | 11716. | .24400 | 477470 | 011/10 | .10134 | 17101. | .10054 | 9/670. | 95670. | 24675. | 041250 | 1.00% | 57/600 | 1.13327 | 1.10470 | 1.02013 | 1.00544 | 06700. | . 800J | (303) | 4047/ | 77700. | 10160 | 050000 | 27784. | 07706. | 45.45.6 | .31243 | . 14.657. | 300 | 080 | 27 | 101 | 180 | 47 | 067 | 1,4 | 140 | 77 | .87971 |
| | 7 | - | 330 | 7 | 200 | 7 | 123 | 0 | 2 4 0 | 040 | .373/3 | 777 |) | P07 | 0.40 | 730 | ~ | 250 | 200 | O . | 5/3 | 017 | 7 67 | 53 | ં 1 લ | 7400 | 33 | 100 | /2°C | 72 | ر ح | 70040. 0.4000 | 3610 | 7000 | 7000 | , , | 5.5 | 3550 | 010 | 200 | 854 | 140 | \approx | 071 | 0.0 | カエン | 35 | 31 | 0 | ノはた |
| | | 1.041/0 | • | • | • | • | • | • | • | • | • | • | • | • | • | • | • | • | • | • | | • | • | • | • | • | • | • | • | • | • | • | • | • | • | • | | | | • | | | 1.24957 | | • | • | | | 64443 | . 549 |
| | ~ | 7 | 20% | | | .34965 | | | | | | | | | | | | · n | 4 | _ | n . | φ. | 4 | 4 | 22 | 4 | 4 | ς, | 7 | ٥. | <u>ب</u> ر | J 1 | 0 0 | 0 1 | 7 6 | - ` | ٠. ٢ | 7 | 5 | ρ | ~ | Ġ. | | ٥ | 4 | 7 | 209 | 4.4 | 490 | 454 |
| Z FLUN | Pſ. | 151 | 152 | 53 | 54 | 55 | 56 | 57 | 98 | 66 | 00 | 0.1 | 5.5 | 63 | 40 | 55 | 96 | 107 | 168 | 169 | 170 | 171 | 1 /2 | 1 73 | 174 | 175 | 176 | 177 | 1/8 | 6/1 | 021 | 161 | 162 | 1 50 | r c | 186 | 167 | 108 | 189 | 190 | 191 | 192 | 193 | 194 | 195 | 196 | 147 | 178 | 199 | 200 |



| - 2 | 67E-0 | 85E-0 | 9 dE -0 | 97E-0 | 9 /E-0 | .90E-0 | . 1 UE -0 | 0E-0 | •1 UE-0 | yE-0 | .97E-0 | . 93E-0 | 97E-05 | .90E-0 | 5E-0 | .95E-0 | .98E-0 | 97E-0 | .90E-0 | 0E-0 | .98E-0 | .98E-0 | 97E-0 | .97E-0 | 25E-0 | .22E-0 | .70E-0 | •65E-0 | . 8 3E -0 | 0E-0 | •95E-0 | .92E-0 | .95E-0 | • 9 JE -0 | .99E-0 | .97E-0 | . 95E-0 | • 6 /E -0 | 2E-0 | 90E-0 | .95E-0 | .93E-0 | 4E-0 | 7E-0 | 90E-0 | .94E-0 | 95E- | .93E-0 | .97E-0 | . 4 DE - 0 |
|--------|---------|---------|---------|--------|-----------|---------|-----------|------------|---------|------------|--------|---------|--------|----------|---------------|--------|---------------|---------------|---------------|---------|--------|--------|--------|--------|----------|--------|----------|----------|-----------|-------|------------|----------|--------------|-----------|--------------|--------|---------|-----------|-------|--------|----------|--------|-------|----------|---------------|--------|--------|---------|-----------|------------|
| SOURCE | . 14 | -3 | J | 9 | 17 | ~ | 18 | œ | æ | B T | 9 | P | 2 | ∞ | 61 | 0 | 6 | 2 | 61 | 7 | 57 | 7 | 61 | 19 | (L) | \sim | \circ | σ | LLJ. | = | 9 | 1 | 17 | 9 | 17 | 7 | P | 17 | 8 ₹ | 7 | ∞ | 18 | 9 | ∞ | ∞ | æ | - | œ | 2 | ∞ |
| ره | .22 | 307 | .161 | .340 | 303. | .711 | 151. | .300 | 011 | 033 | 90 | 122 | 301 | 539 | 70 | 321 | 518 | 52 | 558 | 4 20 | 615 | 445 | 545 | 457 | 860. | 5.148 | -3.82634 | 4.033 | 2.5/3 | 7.500 | 1.568 | .912 | 956. | 267. | .521 | 8 9 | .249 | 574 | •043 | 438 | 870 | 30852 | 1 16 | 718 | 176 | 4 | 77 | 112 | 4,2 | 0 5 7 |
| e S | 16/0 | 34 | 114. | . 524 | 147. | .300 | .073 | .140 | 743 | 10 | ძნი | 186 | /ar | 118 | J. | 623 | 27.7 | 786 | 490 | 09/ | .64081 | 144 | 3 | 30 | 494. | .474 | 7 | 647. | 069. | 404· | 70a• | • 700 | 166. | • 514 | . 233 | . 565 | . 11. | 797. | .040 | • 199 | 488. | JT. | 024. | 0.4 | $\overline{}$ | 146 | 346 | 6549 | 2012 | 747 |
| 7 ^ | 50 | .343 | 81F | 434 | .622 | 68404 | 704. | .522 | D | .410 | 29500 | . 352 | .247 | 30407 | 21505 | 45017 | 19236 | 24652 | 1/660 | 6 30 03 | 16774 | 22105 | 10291 | 21630 | -4.43578 | \sim | -1.94445 | \sim | _ | _ | 1.0 | - | • | л • | 61055 | • | 7, | 41 | 431 | 5 7 4 | 50 | .522 | 52 | 004. | ٠) | .460 | .311 | 644. | 2 | .433 |
| > | 77 | . 12303 | 4410 | ~ | .01133 | 0 | | ~ | Ω | 90 661. | 0 | 017171. | 4 | 67 | 627 | 4 | 63 | 2 | 7.7 | 5 | 12610. | 2 | 7 | 3 | . 24174 | 73 | 56970. | 010/9. | \sim | 2 | 0 | 77 | | 7 | 44640. | 001/6. | .83904 | 46436. | 175 | 010 | 157 | 3 | 1.61 | 014 | 17 670. | 151 | 151 | 104 | . 01103 | . 17461 |
| < > | 1.00000 | 10. | - | - 3" | 3/942. | - | 2 | | Э. | J |) | _ | , | 0 | -4 | J | 7 | 9 | 0 | 2 | 7 | | 7 | 61670. | .36716 | 8///7. | 975020 | 04040. | 30/46. | -37 | 0 | <i>-</i> | | > | | - | \$ | رب د | ٦. | 7 | \sim | `` | 7 | _ | V | -4 | 12/51 | 7 | _ | 04000. |
| , | 5 | 1,50 | 1117 | 1390 | 244 | 2334 | 2001 | 274 | 3005 | 2154 | 3430 | 2374 | 730 | 2160 | 313 | 3037 | 3300 | OBC | 3404 | 3.22 | 420 | 3143 | 3430 | 153 | 067 | 243 | 381 | 0754 | 1001 | 061 | 1/84 | 521 | 2000 2000 | (2) 1 | 301 | 1969 | 7947 | 700 | 2500 | 7 h | 2653 | 2-70 | 2/10 | 1,75 | 1 | 245 | 5 | 227 | 000 | Ç |
| > | . 44473 | . 5471 | 64443 | * 644° | .4443 | . 5491 | .4413 | . 5471 | .4493 | 1649. | 64463 | 1646. | .4443 | 7649. | .4443 | 1649. | .4493 | . 5491 | . 4443 | .5491 | 56443 | . 547L | . 4443 | .5491 | .6484 | .7484 | .6409 | .7434 | .6494 | .7484 | . 6487 | • 7484 | •6407 | . /464 | •6487 | • 7434 | .6487 | .7484 | .6437 | . 7484 | . 6487 | .7484 | .6407 | .7484 | 46464 | .7464 | 643 | 17-172. | € 3 F 9 • | . 74 54 |
| × | 2 | 546 | 256 | 405 | 2 | 423 | 5 | 363 | 334 | 306 | 233 | 5 | 31 | 212 | 104 | 108 | 139 | 28 | 240 | 089 | 57 | 052 | 1.8 | 016 | 3 | 477 | 32 | 455 | 89 | 7 | 434 | 7 | 3 / 8 | 363 | 5 4 | 211 | 5/7 | 234 | 232 | χ Σ | 167 | 162 | 0 | 67 | T 4 | 3 | .08021 | 00 | 47 | 0,5 |
| 7 - | - | \circ | 0 | 0 | \supset | \circ | 0 | $^{\circ}$ | \sim | | - | _ | - | - | $\overline{}$ | - | \rightarrow | $\overline{}$ | $\overline{}$ | \sim | \sim | \sim | V | 2 | \sim | \sim | \sim | 2 | \sim | 7 | 7) | າ | 7) (| ~ | 77 | າ : | √ · | 7 | 7 | 5 | \$ | J* | 4 | 4 | 4 | \$ | 247 | 4 | 4 | Δ. |



| | V NOKMAL | 90E-05 | 94E-05 | 2UE-05 | 13E-05 | 57E-05 | 6 1E -0 5 | 75E-05 | 69E-05 | 85E-05 | 80E-05 | 8 1E-05 | 8ut-05 | 82E-05 | 89E-05 | 62E-05 | 91E-05 | 84E-05 | 90E-05 | 87E-05 | 93E-05 | 86E-05 | 93E-05 | 60E-05 | 43E-05 | 8cE-05 | 93E-05 | doE-05 | 94E-05 | 65E-05 | 94E-05 |
|--------|----------|---------|---------|-----------|----------|----------|-----------|----------|----------|----------|--------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|---------|-----------|---------|----------|---------|----------|---------|----------|----------|----------|
| | SUURCE | . 18788 | .18453 | .02041 | .02130 | .08234 | . 06701 | .11775 | .09187 | .14056 | 48111. | • 15055 | .11908 | .15779 | .12550 | . 16275 | .12946 | .16057 | • 13131 | .16980 | .13394 | 10171. | •13526 | 17292 | .13599 | 69721. | • 13049 | .17300 | · 13/55 | •17304 | .13736 |
| | S S | . 25439 | 0/3c8 | -5.25212 | -0.07671 | -4.35307 | -5.42873 | -3.30025 | -4.71955 | -2.41712 | -4.02451 | -1.8/854 | -3.55162 | -1.47026 | -3.21175 | -1.23196 | -2.97359 | -1.00392 | -2.818.5 | 00875 | 90969-7- | 83303 | -2.60348 | 70855 | -2.53809 | 72218 | -2.49293 | 98469- | 4720407- | 68331 | -2.45302 |
| | ABS.V | 44690. | 1.03020 | 740047 | 7.06400 | 2.31307 | 2.63553 | 06760.7 | 7.39150 | 1.06470 | 5 CT 5 7 - 7 | 1.09003 | 4,13345 | 1.57005 | 2.05220 | 1.49398 | 1.49339 | 1.43063 | 1.95406 | 1.38874 | 1.42241 | 1.3535y | 1.09028 | 1.32487 | 1.00004 | 1.31232 | 1.86894 | 1.30187 | 1.06205 | 1.29 142 | 1.85023 |
| | 7 ^ | 25620 | C0874 | 026,24.7- | -2.65216 | -4.14411 | -2.43801 | -1.74561 | -4.19811 | -1.34968 | -1.97696 | -1.15925 | -1.61639 | -1.00140 | -1.70405 | 0.88.340 | -1.62597 | 82434 | -1.57455 | 77015 | -1.53420 | 73143 | -1.504.35 | 70518 | -1.40313 | 66666 | -1.40009 | 700100- | -1.45995 | 67058 | -1.45553 |
| | > | 04010. | 45445 | 22062. | ((777) | 0/000. | 10750. | 10404. | 001000 | 1.04119 | 1.00904 | 1.00636 | 1.0/1/0 | 1.10424 | 1.10609 | 1.11123 | 1.12508 | 1.11.394 | 1.13710 | 1.11.347 | 1.144/1 | 1.11200 | 1.14071 | 1.11237 | 1.15177 | 1.1118 | 1.10517 | 1.11037 | 1.15406 | 1.110 45 | 1.12510 |
| | Y x | 40220. | 20020. | .20103. | .10115 | 62766. | 10717. | 401700 | 34548 | 4) 263. | . 3.1001 | 077740 | 40626. | 40114. | .20711 | 44505 | 1+6+7. | .31014 | 99477. | 43006. | .1/806 | .24560 | .14269 | .10415 | ·lose? | .12654 | 50310. | 44410. | *0.55 B | .04262 | ·01422 |
| | ~1 | 0,1,1,0 | 171-7. | 14510. | 1/017 | 14960. | 26260. | .073Cc | .0 51 33 | .11942 | . 00500 | .13928 | .01697 | .1537R | .0041 | .10470 | 60966. | .1/100 | .09478 | .17724 | .0.7.11 | .101/6 | .10023 | .10400 | .10165 | .106/5 | .10299 | .167,8 | .10307 | .16600 | .10401 |
| | >- | 1.64074 | 1.74843 | 1.64725 | 1.93333 | 1.84125 | 1.43333 | 1.84725 | 1,93333 | 1.84725 | 1,93333 | 1.84724 | 1.93333 | 1.84725 | 1.90333 | 1.64725 | 1.93333 | 1.84/24 | 1.93333 | 1.847.5 | 1,93333 | 1.84765 | 1.93333 | 1.64/65 | 1.93333 | 1.84724 | 1.93333 | 1.44725 | 1.93333 | 1.84725 | 1.93333 |
| | ~ | .01401 | .01267 | .3 /344 | .20594 | .35606 | . 1,635 | .32689 | .18022 | .24055 | .10023 | .25302 | .13954 | .217u8 | .11971 | .10356 | .10123 | .15524 | .00501 | .12712 | .07010 | .10100 | 07540. | .07674 | .04232 | .05367 | .02960 | .03155 | .01740 | 156000 | .00546 |
| 7 FLUW | PT. | 251 | 252 | 253 | 554 | 255 | 256 | 257 | 258 | 529 | 200 | 261 | 292 | 203 | 204 | 205 | 206 | 267 | 268 | 569 | 2 70 | 271 | 272 | 273 | 2 74 | 275 | 276 | 277 | 278 | 579 | 280 |

XYZ PUTENTIAL FLOw PRUGRAM SEUTION 3, VERSION 4

SAMPLE PROBLEM IRIAXIAL ELLIPSOID

| | 7 | 00000 | 1.00000 | 000000 |
|------------------------------|---------------------|---------|---------|---------|
| | > - | 00000 | 00000 | 3.00000 |
| 33 | PLINTS x | 7.00000 | 00000. | 00000. |
| NORP = IEDIT5= IREAD = | UFF BODY PLINTS X X | 1 | 2 | 3 |



| SAMPLE P | SAMPLE PRUBLEM FRIRAIAL CL X FLOW | .t ertipsuiu | | | 0 FF B | OFF BLUY PUINTS | PAGE 1 |
|------------|--------------------------------------|--------------|----------------------|----------|----------|--|--------|
| PT. | × 6 | - | 7 | X | AA | 4 Z | CP |
| - (| 00000 | 60000 | 2000 | 6/106-1 | 00000. | 00000. | .10008 |
| 7 | 000000 | 00000. | 1・2000 | -1.0001 | 30300. | 00000. | 100/1 |
| m | 000000 | 3.00000 | . 03000. | 10670-1- | 00000. | 00000. | 00051 |
| | | | | | | te malitagen der gemeinsche Speller gerichte der Gemeinsche Gemein | , + |
| | | | | | | | |
| SAMPLE P | SAMPLE PROBLEM TRIAXIAL ELLIPSUID | L ELLIPSÖID | | | OFF 6 | OFF BODY POINTS . | PAGE 2 |
| Y F.O. | , | , | 7 | γ, | ¥ ^ | 7.4 | ٩٥ |
| P 1. | × 00 | 00000 | 2000 | 30000 | -1.03010 | 00000 | 00112 |
| 1 0 | 00000 | | 22000 | 300000 | -1.04121 | 00000 | 00425 |
| 3 € | 30000 | 3.0000 | • 00000 | 0,000. | 45125 | 00000 | 21640. |
| | | | | | | | |
| 1 | | | | | | | |
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| | | | | | | | |
| SAMPLE P | SAMPLE PROBLEM TRIAXIAL ELLIPSOLU | il Ethipsolo | | | U.F.F. B | OFF BOOT POINTS | PAGE 3 |
| P.T. | × | ~ | 7 | × . | ٨٨ . | ٠ ٧٧ | a. |
| - | 2.60000 | 00000 | 20000 | 00000 | 000000 | -1.10658 | 22452 |
| 2 | 00000 | 000000 | 4.50000 | 00000 | 00000 | VI 101.4 | 24774* |
| 3 | 00000. | 3.00000 | 00000 | 00000. | 00000. | -1.05/03 | 11/31 |
| XYZ PÜTE | XYZ PÜTENITAL FLOM PRUGKAR | | SECTION OF VERSION A | | | | |
| SAMPLE | SAMPLE PROBLEM TRIAXIML ELLIPSUID | L ELLIPSOID | | | | | |



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XYZ POTENTIAL FLOw PRUCNAM SECTION 7, VERSION 4



| | ON BODY STREAFLINES - IMPUT ONTA VXI = -1.00000 VYI = .00000 VYI = .00000 VZI = .00000 IMAX = 0 IMRITE = 1 MACH NO = .00000 STREAMLINE STARTING POINTS LINE A A .005000 | Y STREALINE -1.00000 .00000 .00000 .00000 D= .00000 LINE STARTIN | 0n b0DY STREALINES - IMPUT DATA VXI = -1.00000 VXI = .00000 VXI = .00000 NLIN= | PUT DATA 15 405000 | , nn n n n n | 8 | | | | | | | • |
|-----|--|--|---|---|---|--|---|-------------------------------|---|----------------------------------|-------------------------------------|----------------------------------|---------|
| 188 | SAMPLE UNSET LINE N | PRUBLEM FLUM, VX NU. 1 PA | SAMPLE PRUBLEM TRIAAIAL ELLIPJÜID UNSET FLUM, VXI=-1.000 ,YI= .0. LINE NU. I PASSING THKÜUGM JUAD | AMPLE PRUBLEM TRIAAIAL ELLIPJÖID UNSET FLUM, VXI=-1.000 ,Y1= .000 ,Z1= LINE NU. 1 PASSING THROUGH JUMÜRILAIENAL | J VŽI= .UUÛ LA Enal | * 11h 514 | alin stanting Pulnt, | * | 00000.1 | | . 05000 2 = | 90000. | |
| | I 1 2 3 3 13,27.2 | x •94940 •99403 •99403 20•UCLP | I x y y 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 09610. | VX 01227 02440 02440 442KLN3. | ************************************** | 7 72 1724 • U5/98 3434 • 14169 3434 • 14169 ** LNU UF LISTING | . 94614 . 97705 . 97705 | K1 -10.55732 -3.72631 -3.72831 | K6.67703 -5.80713 -5.80713 | H2 1.00000 1.42924 1.42924 | SL .00000 .05404 .05404 | > 0.7.4 |

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